Extended Fujita approach to the molecular weight distribution of polysaccharides and other polymeric systems

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\textbf{A B S T R A C T}

In 1962 H. Fujita ([1, Fujita, Mathematical Theory of Sedimentation Analysis, Academic Press, New York, 1962]) examined the possibility of transforming a quasi-continuous distribution $g(s)$ of sedimentation coefficient $s$ into a distribution $f(M)$ of molecular weight $M$ for linear polymers using the relation $f(M) = g(s)(ds/dM)$ and showed that this could be done if information about the relation between $s$ and $M$ is available from other sources. Fujita provided the transformation based on the scaling relation $s = \kappa M^{0.5}$, where $\kappa$ is taken as a constant for that particular polymer and the exponent 0.5 essentially corresponds to a randomly coiled polymer under ideal conditions. This method has been successfully applied to mucus glycoproteins ([S.E. Harding, Adv. Carbohyd. Chem. Biochem. 47 (1989) 345–381]).

We now describe an extension of the method to general conformation types via the scaling relation $s = \beta M^b$, where $b = 0.4–0.5$ for a coil, ~0.15–0.2 for a rod and ~0.67 for a sphere. We give examples of distributions $f(M)$ versus $M$ obtained for polysaccharides from SEDFIT derived least squares $g(s)$ versus $s$ profiles ([P. Schuck, Biophys. J. 78 (2000) 1606–1619]) and the analytical derivative for $ds/dM$ performed with Microlab ORIGIN. We also describe a more direct route from a direct numerical solution of the integral equation describing the molecular weight distribution problem. Both routes give identical distributions although the latter offers the advantage of being incorporated completely within SEDFIT. The method currently assumes that solutions behave ideally: sedimentation velocity has the major advantage over sedimentation equilibrium in that concentrations less than 0.2 mg/ml can be employed, and for many systems non-ideality effects can be reasonably ignored. For large, non-globular polymer systems, diffusive contributions are also likely to be small.

1. Introduction

Nearly five decades ago Fujita [1] provided the means for converting distributions of sedimentation coefficient to distributions of molecular weight for polydisperse systems with a quasi-continuous distribution of molecular weight. Besides synthetic polymers, natural polymers exhibiting polydisperse distributions include polysaccharides, nucleic acids and many other types of glycoconjugate such as mucin glycoproteins. Knowledge of molecular weight distribution is important – for example in the case of polysaccharides their performance in food materials as gelling and thickening agents is closely related to their molecular weight distribution, and in biopharmaceuticals their performance as excipients and hydrogels, and indeed their safety as vaccines is closely related to their molecular weight distributions. The original Fujita method provided only for the analysis of polymers possessing a random coil conformation. We now describe the extension of the method to other conformations and take advantage of improved and rapid ways of defining distributions of sedimentation coefficient from analytical ultracentrifuge experiments.

1.1. Background: molecular weight determination for polydisperse systems

The last two decades have seen a number of significant advances in the methodology for evaluating molecular weight distributions of polydisperse macromolecular systems in solution. These advances have centred around the coupling of chromatographic or membrane based fractionation procedures with a multi-angle laser light scattering photometer. Ever since the first application of SEC-MALLs (size exclusion chromatography coupled to multi-angle laser light scattering [2]) to polysaccharides [3,4] and to mucus glycoproteins [5,6] it has become, when applicable, the method

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of choice for the determination of molecular weight distributions of polymer systems. Although SEC columns have an upper limit of separation, the dynamic range can be increased by using an alternative separation strategy of field flow fractionation (FFF) in FFF – MALLS where the columns are replaced by a separation membrane [7]. One other major difficulty however has been that of non-inertness of such columns or membranes [8], and for cases where anomalous column or membrane interactions are suspected, procedures based on the analytical ultracentrifuge – which requires no separation media but relies on the inherent fractionation of a centrifugal field – can be used. Before we describe the extension of the Fujita approach based on sedimentation velocity we will briefly review some current approaches based on sedimentation equilibrium in the analytical ultracentrifuge. Sedimentation equilibrium offers the advantage that the optical records for solutions of polymer at sedimentation equilibrium are an absolute function of molecular weight without requiring assumptions or corrections to allow for ambiguities caused by conformation – but used by itself, suffers from poor resolution of components, and is based around the measurement of average molecular weights [9,10]. Nonetheless the ratios of the different averages can be used to describe a distribution.

1.2. $M_w$, $M_z$ and $M_w/M_n$ analysis from sedimentation equilibrium

Fig. 1 shows the optical record (registered using the Rayleigh Interference system) of a polymer system – a bronchial mucin glycoprotein at sedimentation equilibrium in the analytical ultracentrifuge: each of the curved fringes represents a plot of concentration of polymer relative to the meniscus. Provided the meniscus concentration can be determined the actual concentration as a function of radial position $r$ in the ultracentrifuge cell can be defined and various manipulations of the fundamental equation of sedimentation equilibrium can be used to obtain the weight average molecular weight $M_w$ for the distribution. A popular method for the analysis of monodisperse and interacting polydisperse systems is the SEDPHAT approach, which fits Boltzmann exponential corresponding to each species to multiple data sets from different rotor speeds and loading concentrations, and embeds various forms of mass conservation constraints, signal constraints, and mass action law [12]. The possibility to formulate a priori such a finite, discrete model of the distribution, leads to a well-conditioned global model which can be fitted to the available data and extrapolated to the cell base. Although this approach has also been extended to quasi-continuous distributions through the use of additional regularization constraints [12], the analysis of intrinsically continuous distributions with unknown shape and molecular weight range poses a more difficult problem. In particular, for polymer systems with a broad distribution of molecular weight – such as the mucin in Fig. 1 – a major problem is in registering the concentration across the entire range from the air/solution meniscus to the cell base, particularly if the fringes are showing strong upward curvature near the base (even though there is still a finite slope at the meniscus) and/or the radial position of the base is poorly defined. For such systems an operational point average molecular weight known as $M'(r)$ has proved useful which allows for a more robust evaluation of $M_w$, for the distribution [13–15] using the identity $M'(r \rightarrow r_b) = M_{w,app}$, the apparent weight average molecular weight for the whole distribution (from the meniscus $r = r_a$ to the base $r_b$). Subsequent correction for thermodynamic non-ideality then yields $M_w$. Other procedures which miss or ignore the contribution from material near the cell base will always lead to an underestimate for $M_{w,app}$ and hence $M_w$ for polydisperse systems.

The Schlieren optical system on the older generation analytical ultracentrifuges such as the Model E (Beckman Instruments, Palo Alto), MOM (Hungarian Optical Works, Budapest or Centriscan (MSE, Crawley, UK) permitted also the evaluation of the (apparent) $z$-average or $M_{z,app}$ for the distribution. Although this system is not available on the XL-I analytical ultracentrifuge it is nonetheless still possible to estimate $M_{z,app}$ from mathematical manipulations of the relations describing the distributions of solute recorded by Rayleigh Interference optics [16]. $M_{w,app}$ and $M_{z,app}$ differ from the actual molecular weights $M_w$ or $M_z$ because of the effects of thermodynamic non-ideality (see [17] and Refs. therein.). If the concentration, $c$, is sufficiently low then $M_{w,app} \approx M_w$ and $M_{z,app} \approx M_z$, otherwise measurement of $M_{w,app}$ or $M_{z,app}$ at several concentrations and extrapolation (of $1/M_{w,app}$ or $1/M_{z,app}$) to $c = 0$ is required.

A major drawback with regards measurement of $M_w$ (or $M_z$) of polymer systems by sedimentation equilibrium has been the restriction to an optical path length limit of no more than 12 mm in cells used in the XL-I analytical ultracentrifuge (compared with 30 mm in the older Model E analytical ultracentrifuges). This has meant that a minimum concentration of \~0.5 mg/ml has been required (compared with the former 0.2 mg/ml) to ensure a sufficient Rayleigh fringe increment between $r_a$ and $r_b$ to facilitate a measurable $M$. This requirement has had serious resonances for polymeric systems. Whereas at 0.2 mg/ml $M_w \sim M_{w,app}$ has been a reasonable approximation for many polysaccharides and mucins for example, the same approximation can lead to serious underestimates of $M_w$ at 0.5 mg/ml [17]. However the availability now of longer \~20 mm path length cells by Nanolytics Ltd. (Potsdam, Germany), has meant that measurements as low as 0.3 mg/ml are possible and for most systems that is acceptable – by “acceptable” we mean underestimates of no more than 10% (see Table 1). For other systems an extrapolation to $c = 0$ is mandatory. Once $M_w$ and $M_z$ have been defined and non-ideality has been adequately catered for then the ratio of the measured $M_w$ and $M_z$ can be used to define the polydispersity of a distribution. Furthermore these ratios can be related to the width or standard deviation of a distribution (whatever form this may take, e.g. log-normal, Schulz) – the weight average $\sigma_w$ or number average $\sigma_n$ using the Herdan relations [16,18], and Table 2 gives three examples.
of relatively narrow (elution volume) band width are isolated from the eluate and their $M_w$ values evaluated by low speed sedimentation equilibrium. In the usual way: the SEC columns can thereby be “self-calibrated” and elution volume values converted into corresponding molecular weights -- a distribution can therefore be defined and in a way which avoids the problem of using inappropriate standards. This method was described in 1988 and applied to alginate [20], and subsequently dextrans and pectins [21,22] -- with the latter excellent agreement with a comparative off-line SEC-light scattering procedure was observed [22]. With the optical path length restrictions of the XL-I compared to the Model E as mentioned above this approach has fallen into disuse over the last two decades, although the ability to run 7 × 20 mm path length cells simultaneously in a multi-hole rotor now renders this method as an attractive alternative to procedures using SEC-MALLS.

However a much more convenient alternative is now possible based on sedimentation velocity data for polymers with a random coil conformation.

In 1962 Fujita (pp. 182–192 of Ref. [1]) had examined the possibility of transforming a (differential) distribution $g(s)$ of sedimentation coefficient $s$ into a (differential) distribution $f(M)$ of molecular weight $M$ for linear polymers and concluded that the sedimentation velocity determination of $g(s)$ allows the evaluation of the molecular weight distribution $f(M)$ versus $M$ of a given material if information about the relation between $s$ and $M$ is available from other sources. $g(s)$ is defined as the population (weight fraction) of species with a sedimentation coefficient between $s$ and $s + ds$ and $f(M)$ is defined as the population (weight fraction) of species with a molecular weight between $M$ and $dM$. Historically, $g(s)$ profiles could be defined using procedures based on conversion of concentration gradient (Schlieren) optical records by Rinde [19] and later Bridgman [23].

Essentially the transformation from $g(s)$ versus $s$ is simple and is as follows [1]:

$$g(s) ds = f(M) dM,$$

and so,

$$f(M) = g(s). (ds/dM).$$

### Table 1
Comparative non-ideality of polysaccharides (adapted from Ref. [11] and references therein).

<table>
<thead>
<tr>
<th>Sample</th>
<th>$M_m$ (kDa)</th>
<th>$M_w$ (kDa)</th>
<th>$M_z$ (kDa)</th>
<th>$\sigma_w$ (kDa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alginate (manucol DM)</td>
<td>115</td>
<td>136</td>
<td>1.18</td>
<td>50</td>
</tr>
<tr>
<td>Glycoconjugate ASA, Z</td>
<td>215</td>
<td>315</td>
<td>1.5</td>
<td>150</td>
</tr>
<tr>
<td>Glycoconjugate ASA, Z&quot;</td>
<td>240</td>
<td>375</td>
<td>1.6</td>
<td>190</td>
</tr>
</tbody>
</table>

* From Ref. [17].

* From SEC-MALLS for comparison.

### Table 2
Estimates of $M_m$, $M_w$ and $\sigma_w$ from sedimentation equilibrium.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$M_m$ (kDa)</th>
<th>$M_w$ (kDa)</th>
<th>$M_z$ (kDa)</th>
<th>$\sigma_w$ (kDa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pullulan P5</td>
<td>0.0053</td>
<td>10.3</td>
<td>5.5</td>
<td>1.003</td>
</tr>
<tr>
<td>Pullulan P50</td>
<td>0.047</td>
<td>5.5</td>
<td>25.9</td>
<td>1.015</td>
</tr>
<tr>
<td>Xanthan (fraction)</td>
<td>0.36</td>
<td>2.4</td>
<td>86</td>
<td>1.053</td>
</tr>
<tr>
<td>β-glucan</td>
<td>0.17</td>
<td>6.1</td>
<td>104</td>
<td>1.063</td>
</tr>
<tr>
<td>Dextran X50</td>
<td>0.42</td>
<td>3.4</td>
<td>143</td>
<td>1.086</td>
</tr>
<tr>
<td>Pullulan P800</td>
<td>0.76</td>
<td>2.3</td>
<td>175</td>
<td>1.105</td>
</tr>
<tr>
<td>Chitosan (Proton 203)</td>
<td>0.44</td>
<td>5.1</td>
<td>224</td>
<td>1.135</td>
</tr>
<tr>
<td>Pullulan P1200</td>
<td>1.24</td>
<td>2.2</td>
<td>273</td>
<td>1.164</td>
</tr>
<tr>
<td>Mucin glyco-protein CFPθ</td>
<td>2.0</td>
<td>1.5</td>
<td>300</td>
<td>1.180</td>
</tr>
<tr>
<td>Pectin (citrus fraction)</td>
<td>0.045</td>
<td>50.0</td>
<td>450</td>
<td>1.270</td>
</tr>
<tr>
<td>Speroglucan</td>
<td>5.7</td>
<td>0.50</td>
<td>570</td>
<td>1.342</td>
</tr>
<tr>
<td>Alginate</td>
<td>0.35</td>
<td>29.0</td>
<td>1015</td>
<td>1.609</td>
</tr>
</tbody>
</table>

* Based on the lowest possible concentration in a 20 mm centrepiece (-0.3 mg/ml).

* From the bronchial secretion of a patient with Cystic Fibrosis.
In Fujita [1] the sedimentation coefficient $s$ was given for the case of random coils.

$$s = \kappa_c M^b,$$

(8)

where the pre-exponential factor $\kappa_c$ is taken as a constant for that particular polymer under a defined set of conditions and the exponent 0.5 corresponds to a randomly coiled polymer under theta solvent or "pseudo-ideal" conditions (i.e. conditions where exclusion volume effects are matched by associative effects – see e.g. Ref. [24]). The differential is then:

$$ds/dM = \kappa_c^2/2s.$$

(9)

Fujita [1] provided distributions for polystyrene samples in cyclohexane based on sedimentation data of McCormick et al. [25], and these are reproduced in Fig. 3.

The method was later applied to biological materials – mucin glycoproteins – by Harding [26] based on data of Pain [27]. Using a sedimentation coefficient distribution for pig gastric mucin [27] and the assumption of a random coil conformation under ideal conditions ($b = 0.5$), and a known pair of values for $s$ and $M$, namely an $s$ value of $33 \times 10^{-13} \text{ s}$ is approximately equivalent to a molecular weight of 2.5 million, it was possible to perform the transformation to obtain the equivalent molecular weight distribution. The form of the distribution was shown also to be similar to that of the distribution of contour lengths estimated from electron microscopy studies on this polymer [28,29]. In a later publication Bernhard and Oppermann [30] used data from the XL-A ultracentrifuge to estimate a molecular weight distribution for 4-chlorophenyl cellulose-tricarbinol with the calibration made using molecular weights obtained using the MSTAR procedure [13–15]. Although those researchers did not transform the $y$-axis via Eqs. (7) and (9) reasonable agreement with calibrated SEC (cf. Section 1.3 above) was still obtained.

These methods have been based on the assumption that diffusion broadening to the width of the apparent $g(s)$ versus $s$ distribution have been negligible.

3. Extended Fujita method: $f(M)$ versus $M$ distribution from sedimentation velocity data for general conformation types

A straightforward extension of the Fujita method is possible based on use of the general scaling relation (see, for example Ref. [31])

$$s = \kappa_c M^b,$$

(10)

where $b = 0.4$–0.5 for a coil, $\sim 0.15$–0.2 for a rod and $\sim 0.67$ for a sphere [31], and hence

$$ds/dM = b \cdot \kappa_c^2 \cdot s^{(b-1)/b}.$$  

(11)

For $b = 0.5$ Eq. (11) reduces to Fujita’s formula (Eq. (9)).

To do the transformation the conformation type or $b$ needs to be known under the particular solvent conditions and at least one pair of $s$–$M$ values is needed to define the $\kappa_c$ from Eq. (10). Furthermore the method applies to the infinite dilution or non-ideality free sedimentation coefficient distribution, so is only valid for values of $s$ (or a distribution of $s$ values) extrapolated to zero concentration or $s$ values measured at low enough concentrations where non-ideality effects are small. This is indeed possible since sedimentation coefficients can be measured at much lower concentrations than those needed for a sedimentation equilibrium experiment. With 12 mm path length cells it is possible to get reliable measurements at $0.1 \text{ mg/ml}$ and below – the new 20 mm path length cells allow us now to go to even lower concentrations: at such concentrations non-ideality may not be an issue. In the unlikely event that non-ideality effects are still suspected then the determination should be repeated at different loading concentrations.

4. Modern implementation

One approach is to first of all generate a differential sedimentation coefficient distribution $g(s)$ versus $s$. The current generation of XL-I analytical ultracentrifuges do not have the concentration gradient or “Schlieren” optical system so the methodology as outlined by Rinde [19] and Bridgeman [23] is not directly applicable. The last decade however has seen the development of accurate and reliable numerical solutions of the fundamental equation describing the concentration (as registered by Rayleigh interference or uv-absorption optics) versus radial displacement and time and have been implemented in the SEDFIT software [32–38]. For single solute and polydispersity systems the $c(s)/c(M)$ family of models in
SEDFIT also provides a reliable means for correcting for the contribution of diffusion broadening to the apparent width of a peak by taking into account the relationship between the sedimentation coefficient and diffusion coefficient. Initially, this was introduced for compact macromolecules such as folded proteins, for which $b \sim 0.67$ can be fixed and the pre-exponential factor $\kappa_c$ in Eq. (10) is related to the translational frictional ratio (a measure of the asymmetry of the particle); for these systems a weighted-average frictional ratio can still be reliably defined (implemented as a model termed for ORIGIN and applying the transformation and differentiation of this extended Fujita approach is envisioned for polymers with essentially continuous molecular weight distribution (as opposed, for example, to the discrete molecular weights of most proteins), therefore Tikhonov-Phillips regularization [38] is to be preferred over maximum entropy algorithms which perform better for discrete distributions. In order to generate sufficient information in the experimental data, it is necessary to include into the analysis representative scans spanning the entire sedimentation process from the initial depletion near the meniscus at early times until the trailing edge of the sedimentation boundary has merged into the region of optical artifacts in the bottom region at later times. In contrast to methods like$ \delta c/\delta t$, no subset selection is necessary, and no limit for the steepness of the boundaries applies (other than those from artifact-free detection).

6. Examples

We now briefly illustrate application of the “extended Fujita” approach to a range of polydisperse biopolymer systems. We have chosen two neutral polysaccharides (glucomannan and pullulan), three polyionic polysaccharides of wide ranging molecular weight (pectin, alginate and xanthan), one polycationic polysaccharide (chitosan), a glycopoly peptide (from a mucin), and finally a large glycoconjugate vaccine, the latter molecule with a molecular weight distribution well beyond the range possible with SEC-MALLs.

6.1. Konjac glucomannan (KGM)

This is a neutral heteropolysaccharide extracted from the tubers of Amorphophallus konjac and is an important dietary fibre and food thickening ingredient, whose function is closely related to its molecular weight distribution – difficult to measure using SEC-MALLs because of anomalous reactions with column material [40]. Fig. 4 compares the distributions obtained from $g(s)$ versus $M$ and the derivative of Eq. (11) performed analytically to give $f(M)$ versus $M$, with the distribution determined directly using SEDFIT. The two distributions are \~ identical. The small difference in the resolution of a subpopulation at $\sim 150,000$ g/mol can be attributed to differences in the regularization level of fitting the sedimentation data. That the partial peak disappears in the current
f(M) analysis indicates that this feature is not essential in order to explain the experimental data within the noise of data acquisition.

6.2. Pullulan

This is an α(1-6)-linked microbial glucan – another neutral polysaccharide – and is used commercially in the formulation of pharmaceutical capsules and is commonly used as a “standard” polysaccharide for calibrating columns etc. as it can be obtained in narrow molecular weight fractions and behaves like a random coil in solution [41]. Fig. 5 shows the f(M) versus M distribution obtained for P200 pullulan (a standard pullulan where the “200” stands for the weight average molar mass in kg/mol).

6.3. Pectin

Pectin is a family of complex polyuronide-based and highly polyanionic structural polysaccharides and its molecular size and the conformation and flexibility of a pectin molecule is important to the functional properties in the plant cell wall and also significantly affects their commercial use in the food and biomedical industries [42]. Pectins vary in their degree of methyl esterification (DE) >50% are classified as high methoxyl (HM) pectins (Fig. 6a) and consequently low methoxyl (LM) pectins (Fig. 6b) have a DE <50%, although the two classes appear to have similar conformational characteristics [42]).

6.4. Alginate

Alginate is another family of polyanionic polyuronide polysaccharides from brown seaweeds and bacteria like Pseudomonas aeruginosa containing β(1-4)-linked β-mannuronic acid (M) and α(1-4)-linked α-guluronic acid (G) residues. Their conformational flexibility depends critically on the M:G ratio and the distribution of the residues. They are used widely in the food, pharmaceutical and printing industries, where many of their applications are dependent on not only their flexibility but on their molecular weight distributions. The alginates secreted by P. aeruginosa in the bronchial tract also contribute to the problems encountered in Cystic Fibrosis [43]. Fig. 7 shows the molecular weight distribution for an alginate extracted from the brown seaweed Laminaria digitata.

6.5. Xanthan

Xanthan is the large molecular weight extracellular and polyanionic polysaccharide from Xanthomonas campestris [43] It has a
β(1-4)-D-glucopyranose backbone with side chains of (3-1)-α-linked D-mannopyranose-(2-1)-β-D-glucuronic acid-(4–1)-β-D-mannopyranose on alternating residues. Xanthan is widely used in the food industry as a thickener and stabiliser and is also widely used in the oil industry. Fig. 8 shows the molecular weight distribution of an xanthan preparation obtained using the extended Fujita approach.

6.6. Chitosan

Chitosan is the generic name for a family of strongly polycationic (when solubilised) derivatives of poly-N-acetyl-D-glucosamine (chitin) extracted from the shells of crustaceans or from the mycelia of fungi and due to being in a unique position as the only "natural" polycationic polymer chitosan and its derivatives have received a great deal of attention from, for example, the food, cosmetic and pharmaceutical industries [44]. Because of its cationic nature, characterisation of its molecular weight has proven difficult with SEC-MALLs because of anomalous binding to column materials. Its characterisation by our method is by contrast relatively straightforward (Fig. 9).

6.7. Glycopolypeptide from a mucin

Mucins are the major macromolecular component of mucus – nature’s natural lubricant – and have molecular weights from ~400,000 – 20 × 10⁶ g/mol [26]. They have a polypeptide backbone with branches of sugar chains (ranging from 3 to 30 residues) O-linked via serine or threonine residues along the chain. Fig. 10 shows the molecular weight distribution for a glycopolypeptide preparation from human gastric mucin.

6.8. Glycoconjugate vaccine

Finally Fig. 11 shows the molecular weight distribution for a very large glycoconjugate vaccine, too large to analyse by SEC-MALLs [17]. In this case there was some uncertainty in the value of the power law coefficient so two values were chosen to indicate the possible spread range for the distribution: as can be seen the differences do not lead to greatly different distributions.
7. Conclusions and perspectives

The SEDFIT software now with the extended Fujita algorithm is now freely available for download from sedfitsedphat.nibib.nih.gov/software. This complements the molecular weight distributions c(M) that have been widely applied for the study of polydisperse systems, in particular, interacting and non-interacting proteins [45,46]. The method currently assumes ideal conditions but the low concentrations – 0.2 mg/ml and below that are required renders this compensation negligible for most systems. Indeed, the provision of the new 20 mm optical path lengths – an extension of ~70% on what was previously possible with the XL-I ultracentrifuge means that the lowest concentration can be proportionally lower. This is fortunate as extrapolation of a distribution to zero concentration to eliminate non-ideality effects would be an extremely difficult but nonetheless useful challenge for future research. The method currently also assumes that translational diffusion effects are also negligible. Again – and fortunately – the types of macromolecule the method is primarily intended for – large, polydisperse and linear/ asymmetric molecules with high degrees of solvation – are very slow diffusing and hence the contributions to the width of the f(M) versus M distributions will be accordingly small. For example the translational diffusion coefficient for xanthan is some 20 × less than that for lysozyme.

The method does need calibrating for the particular conformational system. The conformation coefficient b and pre-exponential factor Ks need to be previously known. Ks can be defined by a known s–M pair, from sedimentation velocity and sedimentation equilibrium experiments or SEC–MALLS, respectively. If sedimentation equilibrium is used to obtain M, using for example MSTAR, advantage can again be taken of the large 20 mm optical path length cells. If b also is not known then 3 or 4 pairs of s–M values are needed and the parameters determined using Eq. (12) is required. The software provides for a weight-average conformation coefficient b to be extracted by linear regression from the experimental data, in analogy to the weighted-average frictional ratio for folded proteins, but this is applicable only for relatively small polymers that show significant diffusion during the sedimentation experiment. Calibration with a scaling law is essential since the description of the sedimentation data with a two-dimensional size-and-shape distribution [47] will lead to ill-defined results, especially in the absence of significant diffusion from large macromolecules (this is similar to studies of large nanoparticles) [35].

Experimentally, care has to be expressed in filling the cells – menisci in solvent and solution channels need to be carefully matched, otherwise necessitating extended models accounting for co-solvent re-distribution [48]. The scans to be included in the analysis should comprise representatively the entire sedimentation process, from the beginning of depletion near the meniscus from the sedimentation of the fastest species at early times up to the virtual complete sedimentation of the smallest species from the radial observation window. This ensures that a very wide range of sedimentation coefficients can be accurately described in a single experiment, typically spanning a 100fold to 1000fold range. This also improves accuracy and resolution by allowing optimal discrimination of the sedimentation signal from the systematic baseline signal profiles [33] and thereby lowers the detection limit, in principle, to signals less than 0.1 fringes. Solvent densities and partial specific volumes are required as with any ultracentrifuge experiment, and particular attention is required for copolymer systems.

The method should be seen very much as complementary or companion approach to SEC–MALLS, providing an alternative and rapid means for molecular weight determination particularly for cases where SEC–MALLS fails. Certainly in cases where column or membrane interactions are suspected and also where very large macromolecular systems are being analysed – such as the glycoconjugate vaccine materials – the sedimentation velocity method should become the method of choice.

Acknowledgments

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References