

# Monopolistic Competition: The Background

## Nottingham Lectures in International Trade 2012

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# Plan of Lectures

- 1 Monopolistic Competition: Introduction
- 2 Monopolistic Competition with CES Preferences
- 3 One-Sector Model with General Preferences

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  - 3 and 4 just like perfect competition

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  - Demand and Marginal Revenue
  - Average and Marginal Cost
  - Firm Equilibrium
  - The Chamberlin Tangency Solution: Figure
  - Technical Digression: Relative Curvature of AC and p
  - The Role(s) of  $\sigma$
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# Demand and Marginal Revenue

- Firms take income and the industry price index as given:

$$p_i = Ay_i^{-1/\sigma} \quad (1)$$

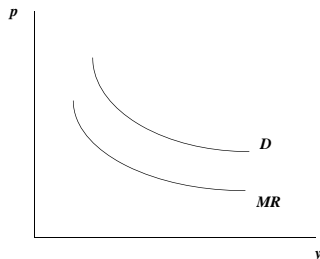
$$\text{where: } A \equiv P^{\frac{\sigma-1}{\sigma}} I^{\frac{1}{\sigma}} \quad (2)$$

- Hence their total and marginal revenue curves are (suppressing  $i$ ):

$$TR = Ay^{\frac{\sigma-1}{\sigma}} \quad (3)$$

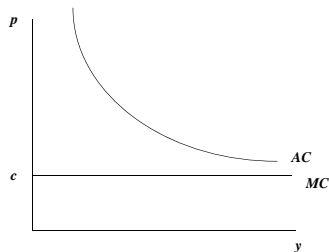
$$MR = \frac{\sigma-1}{\sigma} Ay^{-1/\sigma} = \theta p \quad (4)$$

- So the demand and MR curves are iso-elastic, with the latter a fraction  $\theta$  of the former.



# Average and Marginal Cost

- Homotheticity: Production uses a composite input, at unit cost 1
  - More on this later
- Overheads require  $f$  units; production  $c$  units per unit output
  - $TC = f + cy$
- Hence:  $MC = c$
- $AC = c + \frac{f}{y}$ 
  - A rectangular hyperbola



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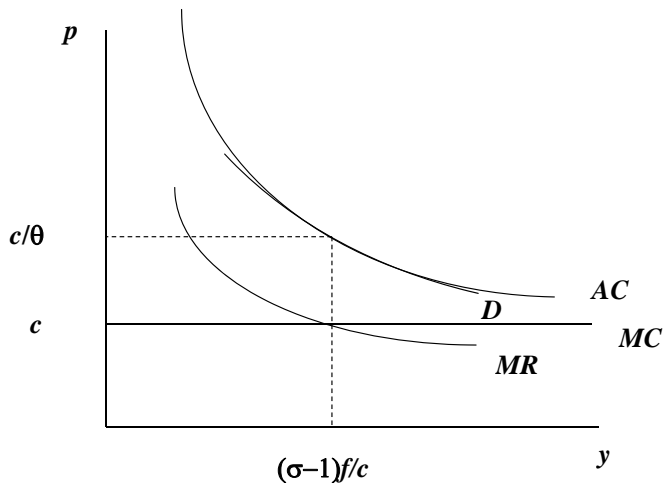
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  - i.e., Equilibrium  $A$  is also independent of  $P, I$ , and therefore  $n$

# The Chamberlin Tangency Solution: Figure



# Technical Digression: Relative Curvature of AC and p

- Proof that AC curve must be more convex than demand curve:

- Unit-free measure of convexity of  $y = f(x)$ :  $r \equiv -\frac{xf''}{f'}$

- Convexity of AC curve (or any rectangular hyperbola):

- $AC = c + \frac{f}{y} \rightarrow AC' = -\frac{f}{y^2} \rightarrow AC'' = \frac{2f}{y^3} \Rightarrow r = 2$

- Convexity of iso-elastic demand curve:

- $p = Ay^{-\frac{1}{\sigma}} \rightarrow p' = -\frac{1}{\sigma} Ay^{-\frac{\sigma+1}{\sigma}} = -\frac{1}{\sigma} \frac{p}{y}$

- $\rightarrow p'' = \frac{\sigma+1}{\sigma^2} Ay^{-\frac{2\sigma+1}{\sigma}} = \frac{\sigma+1}{\sigma} \frac{p}{y^2}$

- $\Rightarrow r = \frac{\sigma+1}{\sigma} \in (1, 2)$  provided  $\sigma \in (1, \infty)$

QED

- This is consistent with:

- Taste for diversity: Holds if and only if  $\sigma > 1$

- Second-order condition for any functional form:

- $\pi = (p - AC)y \rightarrow \pi' = (p - AC) + (p' - AC')y$

- $\rightarrow \pi'' = 2(p' - AC') + (p'' - AC'')y$

- $\Rightarrow \pi'' < 0$  IFF  $-\frac{yp''}{p'} < -\frac{yAC''}{AC'}$

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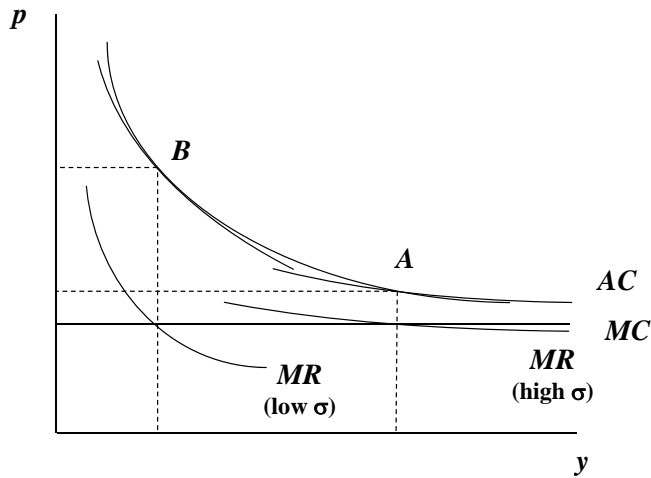
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- Low  $\sigma$ :
  - Different varieties are less close substitutes
  - (greater preference for diversity)
  - $p \gg c$  : so  $p$  and  $MR$  curves are steep and far apart
  - $y$  small: economies of scale are not highly exploited
  - More varieties, lower output of each

# The Role(s) of $\sigma$ : Figure



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- Strong properties of CES equilibrium:

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- 2 Assume heterogeneous firms: Melitz (2003)
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- 3 Relax CES assumption: Avoids all 3!
  - Krugman (1979), Melitz-Ottaviano (2008), Zhelobodko-Kokovin-Parenti-Thisse (2011)

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  - Additive Separability
  - The Elasticity of Demand
  - Firm and Industry Equilibrium
  - Firm and Industry Equilibrium: Figure
  - Labour-Market Equilibrium
  - Firm, Industry and Labour-Market Equilibrium: Figure
  - Effects of Globalisation
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  - However, provided  $N$  is large, each firm rationally takes  $\lambda$  as fixed.
  - Echoing Chamberlin, the demand curve a firm perceives for its own product depends on its price only.

# The Elasticity of Demand

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- i.e., higher consumption, or, equivalently, a lower price, makes households less responsive to price.

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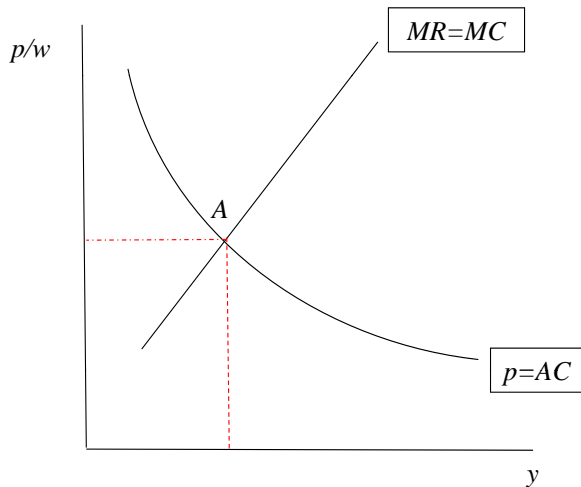
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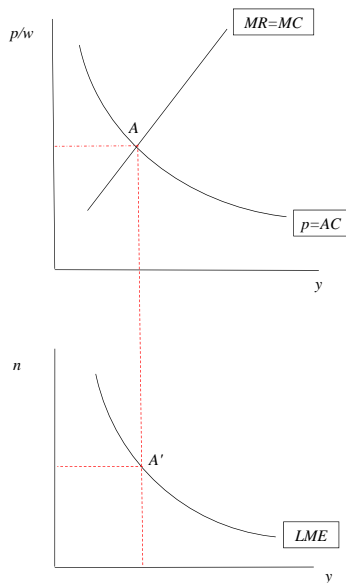
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- The full model then consists of the four equations (6), (7), (8), and (9), in four unknowns:  $p/w$ ,  $x$ ,  $y$  and  $n$ .

# Firm, Industry and Labour-Market Equilibrium: Figure



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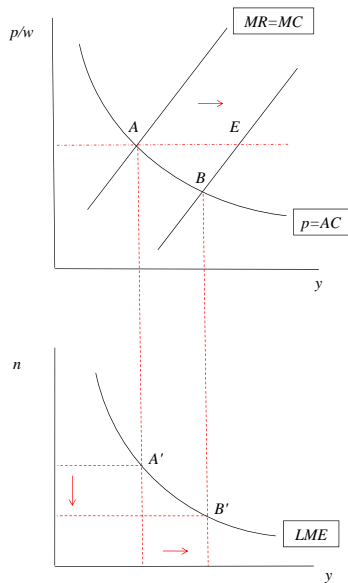
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- Hence, prices must fall and the new equilibrium must be at point  $B$ .

# Effects of Globalisation: Figure



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  - Competition effect (in home market) offset by market-size effect (expansion of world demand).

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  - CES special case de-emphasizes the implications of increasing returns; concentrates attention on the range of varieties available to consumers.

# The CES Special Case: Figure

