# Gravity *Redux*: Structural Estimation of Gravity Equations with Asymmetric Bilateral Trade Costs<sup>\*</sup>

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#### Abstract

Theoretical foundations for estimating gravity equations were enhanced recently in Anderson and van Wincoop (2003). Though elegant, the model assumes sym*metric* bilateral trade costs to generate an estimable set of structural equations. In reality, however, trade costs (and trade flows) are not bilaterally symmetric. To allow for *asymmetric* bilateral trade costs, we provide an alternative framework using the simple workhorse Krugman-type monopolistic-competition/increasing-returnsto-scale model of trade assuming only multilateral trade balance. A Monte Carlo analysis of our general equilibrium model demonstrates – in the presence of asymmetric bilateral trade costs – that the bias of the Anderson-van Wincoop approach (assuming either symmetric or asymmetric bilateral trade costs) is at least an orderof-magnitude larger than that using our approach for computing general equilibrium comparative statics. We then confirm empirically the difference of our approach and that of Anderson and van Wincoop in the Canadian-U.S. "border puzzle" case allowing asymmetric effects of national borders. Furthermore, we apply our approach empirically to the more general case of trade flows among 67 countries in the presence of asymmetric bilateral tariff rates.

**Key words:** International trade; Gravity equation; Trade costs; Structural estimation

**JEL classification**: F10; F12; F13

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## 1 Introduction

"Our analysis suggests that inferential identification of the asymmetry [in bilateral trade costs] is problematic." (Anderson and van Wincoop, 2003, p. 175)

For nearly a half century, the "gravity equation" has been used to explain econometrically the *ex post* effects of economic integration agreements, national borders, currency unions, language, and other measures of trade costs on bilateral trade flows, cf., Rose (2004). While two early formal theoretical foundations for the gravity equation with trade costs – first Anderson (1979) and later Bergstrand (1985) – addressed the role of "multilateral prices," Anderson and van Wincoop (2003) refined the theoretical foundations for the gravity equation to emphasize the importance of accounting properly for the endogeneity of prices. Two major conclusions surfaced from the now seminal Anderson and van Wincoop (henceforth, A-vW) study, "Gravity with Gravitas." First, a complete derivation of a standard Armington (conditional) general equilibrium model of bilateral trade in a multi-region (N > 2) setting with iceberg trade costs suggests that traditional cross-section empirical gravity equations have been misspecified owing to the omission of theoretically-motivated *multilateral* (price) resistance terms for exporting and importing regions. Second, to estimate properly the full general equilibrium comparative-static effects of a national border or an economic integration agreement, one needs to estimate these multilateral resistance (MR) terms for any two regions with and without a border or agreement, respectively, in a manner consistent with theory. Due to the underlying nonlinearity of the structural relationships, A-vW suggest a custom nonlinear least squares (NLS) program to account properly for the endogeneity of prices and to estimate the comparative-static effects of a trade cost.

However, though A-vW (2003) is elegant and motivated by only four assumptions, one assumption is that every pair of regions has *perfectly symmetric* bilateral trade costs.<sup>1</sup>

<sup>&</sup>lt;sup>1</sup>The other three assumptions are that all goods are produced in an endowment economy and are differentiated by origin, preferences are CES, and market clearance holds. This approach is summarized

Hence, in a world-trade setting with N countries, the tariff rate (and *ad valorem*-equivalent non-tariff rate) on products from Japan to the United States equals exactly that on products from the United States to Japan, and so forth. Clearly, this assumption is grossly at odds with reality; data supporting this is provided in Figure 1, using bilateral tariff data from the Global Trade Analysis Project (GTAP) on 67 economies in 2001. There is large heterogeneity bilaterally in tariff rates. In Figure 1, only 42 percent of the bilateral tariff rates are symmetric; 58 percent are not. Also, the figure illustrates that the asymmetry can be as large as 150 percent. Moreover, an important implication of this assumption is that every pair of countries' bilateral trade will be balanced. This is also grossly at odds with reality. However, the symmetric bilateral trade costs (SBTC) assumption was useful to derive an elegant system of structural equations that provided a logically-consistent formal theoretical foundation for proper estimation of a gravity model.

Since the SBTC assumption is often violated in the real world, we address three questions in this paper. First, is there a set of plausible *alternative* assumptions that can generate a theoretical foundation for the gravity equation without SBTC? Second, in a world where we know the true data-generating process, can this alternative theoretical foundation provide unbiased coefficient estimates and *precisely-estimated* general equilibrium comparative statics? Third, in a world with asymmetric bilateral trade costs (ABTC), does the A-vW approach yield biased coefficient estimates and comparative statics, and are such biases avoided under the alternative approach?

In this paper, we suggest two fairly standard assumptions as alternatives to SBTC to motivate a theoretical foundation for the gravity equation. First, we assume the simple Krugman (1980) model of increasing returns to scale with monopolistic competition (IR-MC), as summarized in Baier and Bergstrand (2001) and Feenstra (2004), that has become the workhorse for studying bilateral intra-industry trade. This workhorse IR-MC model pins down the relationship between the exporting country's economic size and the number of varieties consumed by the representative consumer in the importing country. The in equations (12) and (13) of A-vW (2003). We also discuss later the A-vW approach allowing asymmetric border barriers, equations (9)-(11).

second assumption is multilateral trade balance. Of course, this assumption has a long history in the pure theory of international trade, unlike the assumption of bilateral trade balance implied by symmetric bilateral trade costs. Even open-economy macroeconomics models assume multilateral trade balance in the long run. By assuming multilateral trade balance, we can address the endogeneity of prices raised by A-vW *without* assuming symmetric bilateral trade costs.

We show in this paper that replacing A-vW's endowment economy with a Krugman IR-MC economy assuming only multilateral trade balance generates a theoretical foundation for the gravity equation where structural estimation of the model yields both unbiased coefficient estimates and *even more precisely* estimated general equilibrium comparative statics than (either version of) A-vW's model – when bilateral trade costs are asymmetric. We demonstrate this in the context of a Monte Carlo analysis allowing either symmetric or asymmetric bilateral trade costs. Finally, we apply the approach in the context of two widely-recognized empirical examples with symmetric and asymmetric trade costs.

The remainder of this paper is as follows. Section 2 establishes the theoretical framework. Section 3 presents the Monte Carlo analysis. Section 4 provides empirical analyses. Section 5 concludes.

# 2 Gravity Redux

The purpose of this section is to show that the theoretical model of Krugman (1980), summarized in Baier and Bergstrand (2001) and Feenstra (2004, Ch. 5), generates a straightforward gravity equation for bilateral trade flows allowing for endogeneity of prices and GDPs without assuming symmetric bilateral trade costs.

### 2.1 Utility

Following Krugman (1980), Baier and Bergstrand (2001), and Feenstra (2004), there exists a single industry where preferences are constant-elasticity-of-substitution (CES). As typical to the Dixit-Stiglitz (1977) class of models, we assume that preferences are

determined by a "love of variety." We assume that utility of consumers in country j is given by:

$$U_j = \left[\sum_{i=1}^N \sum_{k=1}^{n_i} c_{ijk}^{\frac{\sigma}{\sigma-1}}\right]^{\frac{\sigma}{\sigma-1}},\tag{1}$$

where  $c_{ijk}$  is the consumption of consumers in country j of variety k from country i,  $n_i$  is the number of varieties of the single good produced in country i, which is endogenous in the model, and N is the number of countries (or regions).<sup>2</sup>

As typical, we assume iceberg transport costs and symmetric firms within each country, and hence all products in country i sell at the same price,  $p_i$ . Consequently, the utility function simplifies to:

$$U_j = \left[\sum_{i=1}^N n_i c_{ij}^{\frac{\sigma-1}{\sigma}}\right]^{\frac{\sigma}{\sigma-1}}.$$
(2)

Maximizing equation (2) subject to the budget constraint:

$$Y_j = \sum_{i=1}^N n_i p_i t_{ij} c_{ij},\tag{3}$$

where  $t_{ij}$  is one plus the iceberg trade costs (the latter a fraction) and  $Y_j$  is national income, yields the demand functions:

$$c_{ij} = \left(\frac{p_i t_{ij}}{P_j}\right)^{-\sigma} \frac{Y_j}{P_j},\tag{4}$$

where  $P_j$  is the CES price index:

$$P_{j} = \left[\sum_{i=1}^{N} n_{i}(p_{i}t_{ij})^{1-\sigma}\right]^{\frac{1}{1-\sigma}}.$$
(5)

As in Krugman (1980), Baier and Bergstrand (2001), and Feenstra (2004), the value

<sup>&</sup>lt;sup>2</sup>We begin with utility function (5.21) from Feenstra (2004, p. 152). We could easily introduce a country-specific preference parameter  $\beta_i$  to the function as in A-vW. However, A-vW effectively circumvent estimating  $\beta_i$  by treating prices for each good *i* as "scaled prices ( $\beta_i p_i$ )" in their solution, without loss of generality, cf., A-vW (2003, p. 175). Following Krugman (1980), Baier and Bergstrand (2001), and Feenstra (2004), we assume for simplicity that the  $\beta_i$  are unity for all *i*.

of aggregate exports from country *i* to country *j*,  $X_{ij}$ , equals  $n_i p_i t_{ij} c_{ij}$ . Substituting equation (4) into this expression for  $X_{ij}$  yields:

$$X_{ij} = n_i Y_j \left(\frac{p_i t_{ij}}{P_j}\right)^{1-\sigma},\tag{6}$$

which is identical to equation (5.26) in Feenstra (2004, p. 153).

### 2.2 Production: Alternative Assumption 1

The assumption of a monopolistically competitive market with increasing returns to scale in production (internal to the firm) and a single factor (labor) is sufficient to identify the exporting country's number of varieties, cf., Krugman (1980), Baier and Bergstrand (2001), and Feenstra (2004). The representative firm in country i is assumed to maximize profits subject to the workhorse linear cost function:

$$l_i = \alpha + \phi y_i,\tag{7}$$

where  $l_i$  denotes labor used by the representative firm in country i and  $y_i$  denotes the output of the firm.

Two conditions characterize equilibrium in this class of models. First, profit maximization ensures that prices are a markup over marginal costs:

$$p_i = \frac{\sigma}{\sigma - 1} \phi w_i,\tag{8}$$

where  $w_i$  is the wage rate in country *i*, determining the marginal cost of production.<sup>3</sup> Second, under monopolistic competition, zero economic profits in equilibrium ensures:

$$y_i = \frac{\alpha}{\phi}(\sigma - 1) \equiv \bar{y},\tag{9}$$

so that the output of each firm is a constant,  $\bar{y}$ .

<sup>&</sup>lt;sup>3</sup>The wage rate in country 1 serves as the numeraire.

An assumption of full employment of labor in each country ensures that the size of the exogenous factor endowment,  $L_i$ , determines the number of varieties:

$$n_i = \frac{L_i}{\alpha + \phi \bar{y}}.\tag{10}$$

We can now derive a gravity equation. First, we can show that the trade flow from i to j is a function of GDPs, labor endowments, and trade costs. With labor the only factor of production,  $Y_i = w_i L_i$  or  $w_i = Y_i/L_i$ . Using equations (8) and (10), we can substitute  $\sigma \phi w_i/(\sigma - 1)$  for  $p_i$  in equation (6) and substitute  $Y_i/L_i$  for  $w_i$  in the resulting equation to yield:

$$X_{ij} = Y_i Y_j \frac{(Y_i/L_i)^{-\sigma} t_{ij}^{1-\sigma}}{\left[\sum_{k=1}^N Y_k (Y_k/L_k)^{-\sigma} t_{kj}^{1-\sigma}\right]^{\frac{1}{1-\sigma}}}.$$
(11)

However, we can easily show that equation (11) is identical to the gravity equation in Feenstra (2004) with GDPs and prices. Using equation (8), we can substitute  $p_i/[(\sigma\phi)/(\sigma-1)]$ for  $w_i$  in  $L_i = Y_i/w_i$  and then substitute the resulting equation,  $Y_i/[(\sigma-1)p_i/(\sigma\phi)]$ , for  $L_i$  in equation (10) to yield:

$$n_i = \gamma \frac{Y_i}{p_i},\tag{12}$$

where  $\gamma = \phi \sigma / [(\sigma - 1)(\alpha + \phi \bar{y})]$ . Substituting equation (12) into equation (6) yields:

$$X_{ij} = \frac{Y_i Y_j p_i^{-\sigma} t_{ij}^{1-\sigma}}{\sum_{k=1}^N Y_k p_k^{-\sigma} t_{kj}^{1-\sigma}}.$$
(13)

which is identical to equation (5.26') in Feenstra (2004, p. 154).<sup>4</sup>

### 2.3 Multilateral Trade Balance: Alternative Assumption 2

Equation (13) is a standard representation of the gravity equation. Feenstra (2004) summarized the three methods that have been used up to this point in the literature to address the role of prices. The first approach, used in Bergstrand (1985, 1989) and Baier

<sup>&</sup>lt;sup>4</sup>To see this, note that – using our notation – the denominator of (13) is identical to  $\bar{y} \sum_{k=1}^{N} n_k (p_k t_{kj})^{1-\sigma}$ .

and Bergstrand (2001), was to assume that prices are exogenous and use available price index data to account for the role of prices. This method is now acknowledged to work poorly for two reasons, the first is that conceptually such prices are endogenous and the second is that available price indexes are crude approximations. The second approach has been to account for the price terms using region-specific fixed effects. While such fixed effects can account for the influence of the price terms in estimation, the shortcoming of this method is that – without estimates of the prices before and after the counterfactual experiment – one cannot calculate the appropriate general equilibrium comparative statics using fixed effects (or method 1 above). The third method is to estimate a structural set of nonlinear price equations – under the assumption of symmetric bilateral trade costs (SBTC) – which then generate multilateral price terms before and after the counterfactual experiment to conduct finally the general equilibrium comparative statics, cf., A-vW (2003, eqs. 12 and 13). While this approach provides unbiased estimates and general equilibrium comparative statics, it does so under the SBTC assumption, which also implies bilateral trade balance, cf., A-vW (2003, eq. 13) for  $x_{ij}$  and  $x_{ji}$ . Both considerations are typically violated in the real world.

An alternative assumption, which has a long history in the pure theory of international trade, is to assume *multilateral* trade balance. While also violated in the real world, it is less restrictive than *bilateral* trade balance. Multilateral trade balance is ensured by assuming N equations:

$$\sum_{j=1}^{N} X_{ij} = \sum_{j=1}^{N} X_{ji} \qquad i = 1, ..., N.$$
(14)

Hence, our gravity model is equations (11) subject to (14), analogous to A-vW's equations (12) and (13) for SBTC. Our N(N-1) equations (11) along with N equations (14) comprise a system of  $N^2$  equations in N(N-1) endogenous bilateral trade flows,  $X_{ij}$  (excluding as in A-vW a country's internal trade), and N GDPs,  $Y_i$ . However, unlike A-vW, we do not assume symmetric bilateral trade costs.<sup>5</sup> Rather, we arrive at our system

<sup>&</sup>lt;sup>5</sup>A-vW's (2003) equations (9)-(11) also comprise a structural system, but allowing ABTC. However,

of equations using the Krugman IR-MC market structure to identify  $n_i$  combined with the (less restrictive) multilateral trade balance assumption.<sup>6</sup>

# 2.4 Estimating Elasticities of Substitution and Comparative Statics

An important aspect of the recent gravity-equation literature is going beyond just estimation of unbiased coefficient estimates (or the partial effects of trade costs); country fixed effects can be used to obtain unbiased bilateral trade cost parameter estimates. Rather, the unique feature of this literature is calculating general equilibrium comparative statics – including potentially *welfare effects*. A-vW (2003) went beyond estimation to compute comparative statics using actual and counterfactual MR terms. However, estimates of comparative-static effects require an assumption regarding elasticities of substitution, because the elasticities could not be estimated, cf., A-vW (2001).

In our approach, the elasticities of substitution can be estimated. Given data on GDPs, populations and cif-fob factors and given estimates of trade-cost parameters, then in our model minimizing the absolute values of the differences of exports and imports for all N countries yields an estimate of the elasticity of substitution. These will be provided.<sup>7</sup> Consequently, the comparative-static effects of trade-cost changes can be estimated using the estimated elasticities that surface from our approach. Using the estimated elasticities of substitution, we provide estimates of two comparative statics. One is the change in trade relative to the products of GDPs,  $X_{ij}/(Y_iY_j/Y_W)$ . The other is the welfare effect

as their footnote 11 explains, if bilateral trade costs are asymmetric across countries, the interpretation of their border barrier's effect is restricted to be only an "average" of the barrier's effects in both directions. We will contrast the implicitons of our model with those of A-vW's equations (12) and (13) assuming SBTC and A-vW's equations (9)-(11) allowing ABTC using Monte Carlo analyses in section 3.

<sup>&</sup>lt;sup>6</sup>While the assumption of bilateral trade balance is very restrictive, some recent evidence that the assumption of multilateral trade balance is not very restrictive is found in Dekle, Eaton and Kortum (2007). In that paper, the authors use a calibrated general equilibrium model of world trade to consider how much wage rates and prices would have to change from current levels if all multilateral trade balances were eliminated (the counterfactual). The authors find that wage rates and prices do not change very much. For instance, elimination of China's and the United States' large multilateral trade imbalances requires wage rate adjustments of less than 10 percent.

<sup>&</sup>lt;sup>7</sup>Appendix A describes an alternative method; both approaches yield consistent estimates.

due to a change in trade costs, based on the equivalent variation for country i ( $EV_i$ ), defined as:

$$EV_{i} = 100 \cdot \left[ \frac{Y_{i}^{c}}{Y_{i}} \left( \frac{\sum_{k=1}^{N} Y_{k} (Y_{k}/L_{k})^{-\sigma} (t_{ki})^{1-\sigma}}{\sum_{k=1}^{N} Y_{k}^{c} (Y_{k}^{c}/L_{k})^{-\sigma} (t_{ki}^{c})^{1-\sigma}} \right)^{\frac{1}{1-\sigma}} - 1 \right],$$
(15)

where superscript c indicates counterfactual values of trade costs and GDP.

The remainder of our paper demonstrates our approach under both symmetric and asymmetric bilateral trade costs. In the following section, we provide a Monte Carlo analysis to demonstrate our approach relative to A-vW's (to avoid data measurement issues). Section 4 applies our approach to two widely-recognized empirical contexts.

## 3 Monte Carlo Analysis

To avoid data measurement issues, we conduct a large-scale Monte Carlo study to evaluate our approach relative to several alternatives: A-vW, a traditional OLS gravity specification without multilateral resistance terms (labeled, for brevity, OLS), and a recent linearapproximation approach suggested by Baier and Bergstrand (2006) (described below and referred to henceforth, for brevity, as BV-OLS).

The Monte Carlo analysis proceeds in two steps. First, we use alternative sets of parameter values described in detail below to generate sets of all endogenous variables of the theoretical model  $(Y_i, p_i, w_i, n_i, X_{ij})$  as functions of the model's exogenous variables,  $L_i$ , and  $t_{ij}$ , in a baseline general equilibrium. Then, we change exogenous bilateral trade costs  $t_{ij}$ , holding the model parameters and all  $L_i$  constant to obtain counterfactual values for all the endogenous variables.

In a second step, we use these generated general equilibrium data and add a stochastic error term as in traditional Monte Carlo studies.<sup>8</sup> The major advantage of this procedure

<sup>&</sup>lt;sup>8</sup>An additive log-linear error term is conventional to the general-equilibrium-based literature on gravity-model estimation, cf., Anderson and van Wincoop (2003). In particular, it seems to be a suitable assumption in the absence of zero trade flows, as in our application. We have chosen to add the stochastic error term in only the trade flow equation. GDP (and also  $n_i$ ) could potentially have measurement error as well. However, because we estimate the trade flow equation with country-specific fixed effects, country-specific measurement error will not bias our parameter estimates.

is that the true parameters and the comparative static effects are known so that one can infer the biases of alternative estimation strategies and the consequent comparative statics in a "laboratory" setting.

For robustness, we consider three alternative configurations of the world to capture the typical contexts for gravity equations – analyzing world trade flows. We consider three world sizes of N equal to 10, 20 and 40; this allows us to study the performance of alternative techniques for estimation and comparative statics as sample size increases. There are only three parameters in the theoretical model  $(\sigma, \alpha, \text{ and } \phi)$ ; without loss of generality, we set the fixed cost ( $\alpha$ ) and marginal cost ( $\phi$ ) parameters equal to unity ( $\alpha$  =  $\phi = 1$ ). However, we will consider three alternative values for the elasticity of substitution  $(\sigma)$  – 3, 5, and 10 – to allow us to study the role of "curvature" for estimation and comparative statics. Hence, with three alternative elasticity values and three alternative numbers of countries, we have nine alternative combinations of N and  $\sigma$ . For each of these nine, we use 10 different draws from the set of empirical values for populations,  $L_i$ , and (observable) bilateral trade costs – bilateral cif-fob factors,  $cf_{ij}$  – where we assume  $t_{ij} = c f_{ij}^{\rho}$ , with  $\rho$  denoting the "tariff-equivalent" parameter for  $c f_{ij}$  which is assumed to be  $\rho = 2$ . Population endowments  $(L_i)$  are drawn from the empirical realizations of population data for the year 2003 across 207 economies covered by the World Bank's World Development Indicators (2005).<sup>9</sup> Bilateral cif-fob factors are drawn from the empirical realizations of the cif-fob factors in the 25th-75th percentiles of the distribution using the cif and fob bilateral trade flows from the International Monetary Fund's Direction of Trade Statistics (2003).<sup>10</sup> These data generate 90 (9 scenarios  $\times$  10 draws) alternative baseline equilibria of bilateral trade flows, GDPs, prices, wage rates and numbers of varieties consistent with general equilibrium (before any counterfactuals are introduced).

<sup>&</sup>lt;sup>9</sup>Average population size across the 207 economies is 30,042,094, the standard deviation is

<sup>119,909,488,</sup> and the minimum and maximum are 20,000 and 1,290,000,000, respectively. <sup>10</sup>The average cif-fob ratio is  $\frac{1}{N(N-1)}\sum_{i}^{N}\sum_{j\neq i} cf_{ij} = 1.196$ , the standard deviation of that measure is 0.067, and the corresponding minimum and maximum are 1.010 and 1.455, respectively.

### 3.1 Symmetric Bilateral Trade Costs (SBTC)

Initially, we evaluate our approach ("Suggested model") relative to the approaches of A-vW, BV-OLS and traditional OLS under the case of symmetric bilateral trade costs. Hence, for each of the 90 alternative baseline equilibria, we ensure that the restriction  $cf_{ij} = cf_{ji}$  (and, hence,  $t_{ij} = t_{ji}$ ) holds in the draws from the empirical distribution. Also, we ensure the same restriction holds when altering the trade cost for the counterfactual exercise.

We consider two alternative error structures in the Monte Carlo simulations. We assume that the error terms,  $u_{ij}$ , are given by  $u_{ij} = \mu_i + \nu_j + \xi_{ij}$ . We assume in all cases that  $\xi_{ij}$  is normally distributed  $\mathcal{N}(0, 0.35s_{\xi}^2)$ , where  $s_{\xi}^2$  denotes the variance of  $\xi_{ij}$ . First, we assume that the error terms  $(u_{ijt})$  are uncorrelated with the right-hand-side variables. In the tables, this error structure is labeled "uncorrelated." In this case,  $\mu_i$  and  $\nu_j$  are each distributed as  $\mathcal{N}(0, 0.15s_{\xi}^2)$ . We made 2000 draws for the error terms under this structure. Second, we also consider an error structure where we know the  $u_{ij}$  are correlated with the bilateral trade cost variable,  $t_{ij}$ . To do this, we define two terms,  $\ln cf_i$  and  $\ln cf_j$ , where  $\ln cf_i = (1/N) \sum_{j=1}^N \ln cf_{ij}$  and  $\ln cf_j = (1/N) \sum_{i=1}^N \ln cf_{ij}$ . To generate correlated error terms, in the second case we assume  $\mu_i$  is distributed  $\mathcal{N}(\ln cf_i, 0.15s_{\xi}^2)$  and  $\nu_j$  is distributed  $\mathcal{N}(\ln cf_j, 0.15s_{\xi}^2)$ . In the tables, this error structure is labeled "correlated." We made 2,000 draws for the error terms under this structure also.

Table 1 (assuming  $\sigma = 5$ ) provides the Monte Carlo results for the alternative world configurations of 10, 20, and 40 countries. The table has three panels top to bottom corresponding to alternative configurations of 10, 20, and 40 countries, respectively. Each panel has four rows. The first row provides estimates of the coefficient of  $\ln c f_{ij}$ ,  $(1 - \sigma)\rho$ . The second row shows estimates of  $\sigma$ . The third row is for estimates of the effects on bilateral trade flows relative to GDP products, or "scaled trade flows," of changing trade costs exogenously. The fourth row is for the change in welfare (measured by equivalent variation) of the same change in trade costs. Values in the third and fourth rows in each panel of these tables are the results of a change in trade costs represented by two random draws from the world distribution of cif-fob factors described earlier.<sup>11</sup> Since we do 20,000 draws (10 draws from the empirical distribution of  $L_i$  and  $cf_{ij}$  times 2,000 error-structure draws), we report only mean effects, their standard deviations, and their average absolute bias.

Table 1 has 12 columns. The first column provides the names of the four estimates of interest for each panel (corresponding to the four rows). The second column indicates the "true" values. For  $(1 - \sigma)\rho$  and  $\sigma$ , these are the true values specified a priori (hence, no standard deviation or bias is relevant). For the bilateral trade-flow-effect and equivalent-variation estimates, the "true" values are the means and standard deviations of the comparative statics in response to the change in trade costs based upon the calibrated general equilibrium model. The remaining columns 3-12 present the estimates of the two parameters  $(1 - \sigma)\rho$  and, if retrievable,  $\sigma$ , and the two comparative-static effects (trade, welfare) using each of five alternative techniques, with each technique applied twice: first with our uncorrelated error structure (odd-numbered columns) and second with correlated errors (even-numbered columns). Columns (3) and (4) present the estimates using our "suggested" model. For consistent parameter estimates of  $(1 - \sigma)\rho$  in the first stage, we use fixed effects, as has become the standard in the literature. Given a consistent estimate of  $(1-\sigma)\rho$ , we then use this parameter estimate with the N (nonlinear) multilateral trade balance equations to obtain estimates of N GDPs, and then obtain estimates of  $\sigma$  (see Appendix A). Using exogenous changes in  $cf_{ij} = cf_{ji}$ , we can then generate the counterfactual GDPs and trade flows to estimate the two comparative statics.

Columns (5) and (6) present the estimates using the A-vW technique.<sup>12</sup> In this case, we use the same "structural" (iterative) estimation technique as in A-vW, under both error structures, from which N multilateral resistance terms are estimated. Then using exogenous changes in  $cf_{ij} = cf_{ji}$ , we can generate the counterfactual multilateral resistance terms and trade flows to estimate the scaled trade-flow comparative statics, given

<sup>&</sup>lt;sup>11</sup>Note that this implies that some country-pairs will have larger and others smaller trade barriers in the counterfactual situation than in the benchmark equilibrium. Moreover, the associated changes in trade costs are eventually quite large for some of the dyads.

<sup>&</sup>lt;sup>12</sup>Since  $\sigma$  is unknown under A-vW, we assume (as in A-vW) a value for  $\sigma$  of 5, irrespective of the true value of  $\sigma$ . So in this case, we expect A-vW to perform well.

an assumed value of  $\sigma$  (say, 5). Finally, one can estimate the equivalent variation based on the same set of assumptions. In the case of uncorrelated errors, coefficient estimates using fixed effects in the first stage will generate asymptotically identical parameter estimates of  $(1 - \sigma)\rho$  to A-vW; this is not the case for correlated errors.

Columns (7) and (8) present the estimates using one of two techniques described in Baier and Bergstrand (2006), referred to here as BV-OLS-1. Columns (9) and (10) present the estimates using the other of the two techniques described in Baier and Bergstrand (2006), referred to here as BV-OLS-2. Baier and Bergstrand (2006) present two techniques for estimating gravity equation parameters and comparative statics accounting for the endogenous price terms by using a first-order log-linear Taylor-series expansion of the nonlinear price equations. The method results in estimating the coefficients using a (reduced-form) gravity equation and calculating the MR terms without having to solve a structural system of nonlinear equations. Finally, columns (11) and (12) present the estimates using the traditional OLS gravity equation ignoring the role of endogenous prices.

Table 1 provides the results for an elasticity of substitution of 5 (which is chosen specifically to correspond to the assumed  $\sigma$ ). Several points are worth noting. First, when the true value of  $(1 - \sigma)\rho = -8$ , our suggested approach (both error structures), A-vW (with uncorrelated errors), and BV-OLS-1 (both error structures) provide coefficient estimates for  $cf_{ij}$  that are virtually identical to the true value (see all panels). Moreover, both our approach and BV-OLS-1 share the minimum average absolute bias. Both BV-OLS-2 and traditional OLS gravity equations have notably larger biases.<sup>13</sup> We note that these same relative results hold as sample size grows from 10 to 20 to 40 countries, although as expected average absolute biases decline with N.

The second row of each panel provides estimates of the elasticity of substitution, but only for our approach. Across sample sizes of N countries, our approach provides very accurate estimates of  $\sigma$ . Moreover,  $\sigma$  cannot be *estimated* using the other approaches.

<sup>&</sup>lt;sup>13</sup>BV-OLS-1 tends to have less bias because it uses approximations around the "mean," consistent with least squares estimation, cf., Baier and Bergstrand (2006).

The third row provides estimates of the comparative-static effect on scaled trade flows of a common trade-cost change. The most notable result is that in all three panels our suggested approach provides the *lowest biases* for the general equilibrium trade-effect estimates. We note three further results. First, the trade-effect comparative-static biases for our suggested approach and for A-vW are not notably different; this is to be expected since – under assumed symmetric bilateral trade costs – the two approaches should yield similar results. Second, BV-OLS-2 biases are much smaller than BV-OLS-1 biases (or OLS biases) for N = 40, since the former uses a GDP-weighted approach whereas the latter does not. Third, while the comparative-static estimates using BV-OLS-2 are considerably higher than using either our suggested approach or A-vW, they are also considerably less than those from ignoring multilateral resistance terms – as is typically done by empirical researchers.

In the fourth row of each panel, we provide two pieces of information. For our approach, we use the *estimated* elasticities of substitution to generates estimates of welfareeffect comparative statics. These are very close to the true values, not surprisingly, since the elasticity estimates using our approach are precise. The second piece of information is that – assuming  $\sigma = 5$  (as in A-vW) – A-vW estimates of the welfare effects are also accurate. Again, this is not surprising because these estimates are based upon *assuming* the true value of  $\sigma$ , 5.

For robustness, we also ran the same Monte Carlo analysis for true values of  $\sigma$  of 3 and 10. These estimates are provided in Appendix Tables A1 and A2. For brevity, we note three key findings. Most importantly, the overall findings summarized above hold also for the cases of  $\sigma = 3$  and  $\sigma = 10$ ; the results are robust. Second, the estimated welfare effects using our approach are now considerably less biased than those using A-vW. There is a simple explanation. Our approach uses *estimated* values of  $\sigma$ , and our method generates  $\sigma$  estimates very close to the true values. By contrast, A-vW welfare estimates use an assumed value of  $\sigma$ . If the assumption for  $\sigma$  is incorrect – in both tables for A-vW,  $\sigma$  is assumed to equal 5, as in A-vW – the estimated welfare effects are very biased. This is another advantage of our approach. Third, when  $\sigma = 10$ , the trade-effect

comparative-static estimates are slightly smaller using A-vW's approach than ours.

In summary, we note two important conclusions regarding the comparative-static estimates from this Monte Carlo analysis. First, under the assumption of symmetric bilateral trade costs, neither our approach nor A-vW provides trade-effect estimates that are economically different from the true values. But this is not surprising: under SBTC, A-vW should be efficient. However, under *asymmetric* bilateral trade costs, we will see that things change. Second, our approach provides precise *estimates* of the true elasticity of substitution, so that our welfare-effect estimates are also very precise. By contrast, A-vW assume a value of  $\sigma$ , so that if the  $\sigma$  assumption is considerably different from the true value, A-vW welfare-effect estimates will be considerably biased.

### **3.2** Asymmetric Bilateral Trade Costs (ABTC)

We performed the same set of Monte Carlo simulations as before except now we admit *asymmetric* bilateral trade costs in the draws from the empirical distributions for cif-fob factors. Every other aspect was identical in these simulations as before, including the alternative error structures, configurations of countries, and parameter values.

We summarize the results in Table 2 for the case of  $\sigma = 5$  (where A-vW assume the correct value); similar results hold for the two other elasticities (not reported, for brevity). Moreover, for brevity we focus on the results for our approach versus A-vW (2003), ignoring the results for the two BV-OLS techniques and traditional OLS. Also for brevity, we report the results only for uncorrelated errors. Columns (3), (4) and (5) in Table 2 provide estimates from our approach and two versions of A-vW's, respectively. The results in column (4) are based on A-vW's equations (12) and (13) assuming SBTC, whereas those in column (5) are based upon A-vW's equations (9)-(11) allowing ABTC.

Several points are worth noting. First, our method provides unbiased estimates of  $(1-\sigma)\rho$  and  $\sigma$  – even in the presence of ABTC. Second, the trade-effect comparative statics and EV estimates using our approach *always* have a lower bias than A-vW assuming SBTC (even though A-vW assumes the true  $\sigma$ ), cf., column (4). Moreover, the biases

using A-vW's equations (12) and (13) in the presence of asymmetric bilateral trade costs are always at least one order-of-magnitude greater than those using our approach. Third, for trade-effect estimates, the bias tends to increase (decrease) as the number of countries in the world increase for the A-vW (our) approach. Thus, our approach – with a Krugman market structure and multilateral trade-balance condition – performs better overall in the presence of ABTC relative to the A-vW technique assuming SBTC, cf., column (4).

The fifth column in Table 2 provides comparable estimates using A-vW's approach allowing *asymmetric* multilateral resistance (MR) terms equations (A-vW, 2003, eqs.(9)-(11)). Instead of solving a set of N nonlinear price equations for  $P_i$ , we solve a set of 2N nonlinear price equations for  $P_i$  and  $\Pi_i$  according to equations (10) and (11) in A-vW (2003). Footnote 11 in A-vW cautions us about the potential pitfalls of using A-vW's approach if indeed the MR terms ( $P_i$  and  $\Pi_i$  in A-vW) are asymmetric. They note:

> There are many equilibria with asymmetric barriers that lead to the same equilibrium trade flows as with symmetric barriers, so that empirically they are impossible to distinguish. . . . Our analysis suggests that inferential identification of the asymmetry is problematic (A-vW, 2003, p. 175).

The fifth column of Table 2 confirms this issue. When we run A-vW allowing for 2N price equations, the third row in any of the three panels reveals that the estimated trade-effect estimates are grossly biased, even more biased than using A-vW's approach assuming symmetric bilateral trade costs.<sup>14</sup>

## 4 Empirical Evidence

We now apply our technique and A-vW's technique to actual trade flow data. We consider two popular contexts: the U.S.-Canadian "border puzzle" case and a traditional gravity-

<sup>&</sup>lt;sup>14</sup>For completeness, we note that, in the case of ABTC, both BV-OLS techniques and OLS yielded biases more than the suggested approach, but considerably less than A-vW's techniques.

equation case of world trade flows in the presence of asymmetric trade costs (in particular, asymmetric bilateral tariff rates).

### 4.1 The U.S.-Canadian Border Puzzle

McCallum (1995) inspired a cottage industry of gravity-equation analyses of the effects of a national border on the trade of Canadian provinces and U.S. states, including the seminal A-vW (2003). This section has two parts. We re-estimate the same specifications addressed in that literature, initially assuming SBTC (as assumed there). In the second part, we assume *asymmetric* national border barriers for Canada and the United States.

#### 4.1.1 Symmetric Canadian-U.S. National Border Barriers

In this section, we present the results of re-estimating the analysis of A-vW using their nonlinear estimation technique, fixed effects, and our approach. The first panel of Table 3 presents the coefficient estimates (standard errors in parentheses) under the three alternative estimation procedures. First, we confirm in the second column of the first panel of Table 3 the A-vW (2003) structural estimates of -0.79 and -1.65. Second, we confirm the fixed effects estimates of -1.25 and -1.55 found in that study; later estimates in column (3) use the A-vW approach to solve for MR terms, but based upon coefficient estimates using fixed effects. Third, our approach yields identical coefficient estimates to those in column (3), as we use fixed effects also; however, later estimates in column (4) are based upon our suggested approach. Of course, fixed effects estimation avoids coefficient estimate bias introduced using the SBTC-based A-vW method on actual trade data (which likely suffers from correlation of country-specific errors with explanatory variables in the model). Fourth, the table reminds one that our method also generates an estimate of  $\sigma$ from the data. Our method implies an estimate of  $\sigma$  equal to approximately 12. While such an estimate is at the higher end of the range of recent estimates of  $\sigma$ , we will show shortly that – by allowing for *asymmetric* Canadian and U.S. national border coefficient estimates – the estimate of  $\sigma$  falls right in the middle of the range of recent cross-country

estimates of  $\sigma$ .

The second panel of Table 3 summarizes the trade-effect comparative-static estimates for pairings of provinces-provinces, states-states, and provinces-states. The important conclusion to draw from this panel is that — under the restriction that the border effect is symmetric — the standard deviation of the trade effects of border barriers is high using all estimation procedures.

The third panel of Table 3 presents the welfare effects of symmetric border barriers. Note that our method generates much smaller welfare effects of national barrier eliminations than A-vW or fixed effects. The reason is that our approach estimated an elasticity of substitution of nearly 12, while the estimates using A-vW or fixed effects *assume* a much lower elasticity, 5.

The fourth, fifth and sixth panels provide further results regarding the estimated average MR terms and impacts of border barriers on trade. The key aspect to note is that our method provides virtually identical results to those implied using coefficient estimates based upon fixed effects (which are unbiased) and then calculating the "border effects" using the A-vW system of equations. Again, under SBTC, we would expect A-vW to work as well as our approach (using parameter estimates derived from fixed effects).

#### 4.1.2 Asymmetric Canadian-U.S. National Border Barriers

Table 4 reports the empirical results under the more plausible assumption that Canadian and U.S. national borders have asymmetric effects on trade. We introduce separate dummy variables for a Canadian national border and a U.S. national border. In this case, the estimate of  $(1 - \sigma) \ln b_{US}$  measures the effect of the Canadian-U.S. border on a flow from a Canadian province to a U.S. state. The estimate of  $(1 - \sigma) \ln b_{CA}$  measures the effect of the national border on a trade flow from a U.S. state to a Canadian province. Note that the coefficient estimates for the two dummy variables are economically and statistically significantly different from one another. The effect of a national border is asymmetric according to the flow's direction. The first panel indicates also that, as in the previous case, our method provides identical parameter estimates for the trade-cost variables' coefficients to fixed effects. However, note that with ABTC, the estimate of the elasticity of substitution from our model is equal to 6.4. This value is well within the range of recent estimates of this elasticity using cross-section trade data, cf., Baier and Bergstrand (2001), Head and Ries (2001), and Anderson and van Wincoop (2004).

The second panel of Table 4 confirms that - under an assumption of ABTC - our method yields border barrier effects that are *much* lower and have considerably lower standard deviations than using the A-vW approach which assumes SBTC.

The third panel of Table 4 provides welfare-effect estimates of border barriers. In the third panel, recall that A-vW and fixed effects assume an elasticity of 5, whereas our approach estimates the elasticity at 6.4. The lower welfare effects using our approach are partly explained by our coefficient estimates being unbiased, but also by the higher value of  $\sigma$ . Note that the estimate of the welfare gain from eliminating the effect of the national border is *considerably* lower in our approach, even when using coefficient estimates generated with fixed effects.

### 4.2 World Trade Flows and Asymmetric Bilateral Tariffs

In this final substantive section, we apply our estimation procedure on the case of world trade flows, tariffs, and dummy variables from the GTAP data set for the year 2001. Thus, we apply our approach to the most common context for the gravity equation, world trade flows. GTAP provides a data base of world trade flows among 67 countries, asymmetric bilateral tariff rates, populations, and numerous dummy variables to conduct general equilibrium comparative statics. This data set provides an excellent context in order to examine the usefulness of our procedure.

We run a country-fixed-effects gravity equation on "scaled" bilateral trade flows including, on the right-hand-side, the log of the gross bilateral tariff rate (*Tar*), the log of bilateral distance (*Dist*), and dummy variables for common language (*Comlang*), contiguity (*Contig*), former colony (*Colony*), and common colonial heritage (*Comcol*), often included in gravity specifications, cf., Rose (2004). Then, we employ the N multilateral trade balance conditions to conduct the trade-effect and welfare-effect comparative statics.

As conventional to the gravity-equation literature, we assume that the log of the gross trade-cost variable (t) is a linear function of the log of the gross bilateral tariff rate, log bilateral distance, and various dummies:

$$(1 - \sigma) \ln t_{ij} = -\sigma \kappa \ln(Tar_{ij}) + (1 - \sigma)\rho \ln Dist_{ij} + (1 - \sigma) \ln b_1 Comlang_{ij}$$
$$+ (1 - \sigma) \ln b_2 Contig_{ij} + (1 - \sigma) \ln b_3 Colony_{ij}$$
$$+ (1 - \sigma) \ln b_4 Comcol_{ij}.$$

The parameter of log gross import tariffs of importer j against exporter i,  $-\sigma\kappa$ , has two components. The use of  $-\sigma$ , rather than  $1-\sigma$ , reflects an assumption of tariff-revenue redistribution to consumers. The term  $\kappa$  reflects the influence of measurement error of de*jure* tariff rates.<sup>15</sup>

Table 5 presents the results. The first panel in Table 5 provides the coefficient estimates from the first stage fixed-effects regression. We obtain plausible parameter estimates and statistically significant effects, as is typical in such specifications. The top panel reports an estimate of  $\sigma$  of 7.38, which is in the range of plausible estimates discussed earlier.

The second panel reports the "trade-effect" estimates from a complete elimination of bilateral tariff rates. Not surprisingly, given the sizable negative shock on tariffs, the increase in trade on average is fairly large. Also the standard deviation of the effects is quite large relative to the mean effect, indicating that the variation in tariffs among the developed and the developing economies is large.

The third panel reports the welfare-effect estimate of a complete elimination of bilateral tariff rates. This elimination raises welfare by about 6.6 percent. Such an estimate – *based upon empirical evidence* – is not out-of-line with estimates generally provided by CGE computations (see Francois and Martin, 2007, for a recent survey). Thus, our empirical

<sup>&</sup>lt;sup>15</sup>The impact of high *de jure* tariffs tends to be dampened by the misclassification of goods. Hence, we would expect that  $\kappa < 1$ . Evidence on this issue has been provided by Fisman and Wei (2004) and, more recently, by Javorcik and Narciso (2007).

model provides a welfare effect quite in line with existing estimates based upon "theory with numbers."

## 5 Conclusions

Theoretical foundations for estimating gravity equations were enhanced recently in Anderson and van Wincoop (2003). Though elegant, the model assumes *symmetric* bilateral trade costs to generate an estimable set of structural equations. In reality, however, trade costs (and trade flows) are not bilaterally symmetric. We use the simple workhorse Krugman-type monopolistic-competition/increasing-returns-to-scale model of trade assuming only multilateral trade balance to allow for *asymmetric* bilateral trade costs. A Monte Carlo analysis of our general equilibrium model demonstrates – in the presence of asymmetric bilateral trade costs – that the bias of the Anderson-van Wincoop approach (assuming either SBTC or ABTC) is at least an order-of-magnitude larger than that using our approach for computing general equilibrium comparative statics. We then confirm empirically the difference of our approach from the one of Anderson and van Wincoop in the Canadian-U.S. case allowing asymmetric effects of national borders. Finally, we demonstrate that our approach works in the more general case of world trade flows in the presence of asymmetric bilateral tariff rates.

## Appendix A

Using  $t_{ij} = c f_{ij}^{\rho}$  in (11) results in:

$$X_{ij} = Y_i Y_j \frac{(Y_i/L_i)^{-\sigma} c f_{ij}^{(1-\sigma)\rho}}{\left[\sum_{k=1}^N Y_k (Y_k/L_k)^{-\sigma} c f_{kj}^{(1-\sigma)\rho}\right]}.$$
(16)

Estimation of equation (16) subject to the N multilateral trade balance constraints (14), after substituting in (16) for  $X_{ij}$  and its analogue for  $X_{ji}$  into (14), yields parameter estimates for  $\sigma$  and  $(1 - \sigma)\rho$  using a nonlinear estimation technique. However, in

empirical applications it will only rarely be the case that this iterative approach will not be rejected against a fixed country effects model, because the trade cost variables are typically correlated with the country-specific error terms.

Alternatively, one may employ fixed country effects in the estimation of (16); this is what we employ in the paper. This approach will obtain a consistent estimate of  $(1 - \sigma)\rho$ , irrespective of whether  $cf_{ij}$  is correlated with the country-specific error terms or not. However, with fixed effects  $\sigma$  can not be directly estimated but can be retrieved in the following way. Use equation (16) to determine relative aggregate bilateral demand of consumers in market j:<sup>16</sup>

$$\frac{X_{ij}}{X_{kj}} = \frac{Y_i}{Y_k} \left(\frac{Y_i/L_i}{Y_k/L_k}\right)^{-\sigma} \left(\frac{cf_{ij}^{\rho}}{cf_{kj}^{\rho}}\right)^{1-\sigma}.$$
(17)

Following Eaton and Kortum (2002), the latter obtains an alternative way of estimating the elasticity of substitution among varieties by using the expression:

$$\widehat{\sigma} = -\frac{1}{N^2(N-1)} \sum_{i=1}^N \sum_{j=1}^N \sum_{k\neq j}^N \left[ \left( \ln \frac{X_{ij}}{X_{kj}} - \ln \frac{Y_i}{Y_k} - \ln \frac{\widehat{cf_{ij}^{(1-\sigma)\rho}}}{\widehat{cf_{kj}^{(1-\sigma)\rho}}} \right) / \ln \left( \frac{Y_i/L_i}{Y_k/L_k} \right) \right].$$
(18)

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<sup>&</sup>lt;sup>16</sup>Of course, the approach is also applicable with more than a single trade cost variable. Then,  $cf_{ij}^{\rho}$  is a single element in a product which is represented by  $t_{ij}$  in the main text.

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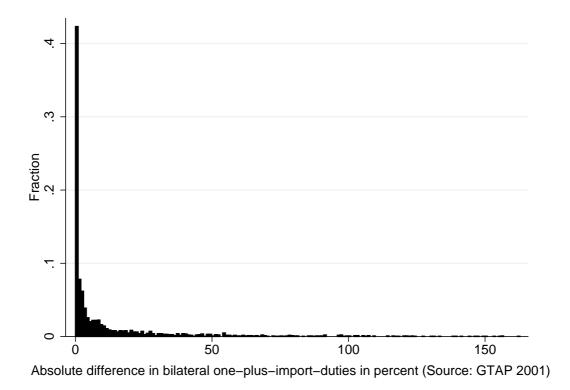


Figure 1: Asymmetry of bilateral import duties

Estimates	True		ested del	A-	vW	BV-C	DLS 1	BV-0	DLS 2	0	LS
(1)	(2)	uncorr. (3)	corr. (4)	uncorr. (5)	corr. (6)	uncorr. (7)	corr. (8)	uncorr. (9)	corr. (10)	uncorr. (11)	corr. (12)
					10-com	untry-world,	$\sigma = 5$				
$(1 - \sigma)\rho$											
mean std.	-8	-8.0214 0.3232	-8.0354 0.3205	-8.0149 0.4738	-7.5514 0.5197	-8.0214 0.3232	-8.0354 0.3205	-7.7444 0.6343	-7.8193 0.6395	-7.6241 0.5502	-6.831 0.678
bias	-	3.2207	3.2069	4.6685	6.7944	3.2207	3.2069	6.6943	6.5789	6.7748	14.708
$\sigma$ mean	5	5.0177	5.0264	_	_	_	_	_	_	_	
std.	-	0.2487	0.2467	-	-	-	-	-	-	-	
bias	-	3.7163	3.7071	-	-	-	-	-	-	-	
$X_{ij}Y_w$											
$\Delta \frac{X_{ij}Y_w}{Y_iY_j}$											
mean std.	15.6348 67.7946	$15.7586 \\ 68.2929$	$15.8197 \\ 68.4372$	$15.7720 \\ 68.4578$	$13.7475 \\ 62.1077$	$14.6863 \\ 63.0199$	$14.7388 \\ 63.1647$	$20.9057 \\ 81.6642$	$21.2467 \\ 82.1467$	$21.2083 \\ 73.8767$	16.948 61.30
bias	- 01.1940	1.8482	1.8396	2.5982	3.7948	19.0619	19.0723	22.7052	22.8996	26.4978	24.13
$EV_i$ mean	1.7030	1.7011	1.6972	1.7038	1.6365						
std.	9.1959	9.1915	9.1818	9.1918	9.0527	-	-	-	-	-	
bias	-	0.2234	0.2213	0.1483	0.2054	-	-	-	-	-	
					20-cou	intry-world,	$\sigma = 5$				
$(1 - \sigma)\rho$											
mean std.	-8	-8.0107 0.1558	-8.0087 0.1559	-8.0107 0.2570	-7.6167 0.2333	-8.0107 0.1558	-8.0087 0.1559	-7.8510 0.2712	-7.7691 0.2235	-7.7905 0.2655	-7.20
bias	-	1.5518	1.5545	2.5415	4.8903	1.5518	1.5545	3.0960	3.2839	0.2055 3.5705	9.96
mean	5	5.0092	5.0078	_	_	-	_	-	_	_	
std.	-	0.1249	0.1248	-	-	-	-	-	-	-	
bias	-	1.8199	1.8232	-	-	-	-	-	-	-	
$\Delta \frac{X_{ij}Y_w}{Y_iY_j}$ mean											
$- Y_i Y_j$	23.3920	23.4703	23.4569	23.4934	21.2079	19.0991	19.0883	26.1341	25.4988	24.3130	20.75
std.	90.5346	90.8372	90.7944	20.4334 90.9789	83.7935	80.1990	80.1646	20.1341 96.5163	94.8488	24.9150 84.9751	75.31
bias	-	1.1651	1.1674	1.8146	3.3970	17.9046	17.9053	14.7770	14.2352	22.2170	21.76
$EV_i$											
mean	0.8988	0.8984	0.8986	0.8997	0.8486	-	-	-	-	-	
std.	7.2242	7.2194	7.2202	7.2294	7.0372	-	-	-	-	-	
bias	-	0.0788	0.0789	0.0903	0.1692	-	-	-	-	-	
					40-cou	intry-world,	$\sigma = 5$				
$(1 - \sigma)\rho$ mean	-8	-8.0029	-8.0026	-8.0106	-7.8565	-8.0029	-8.0026	-7.7537	-7.7207	-7.7949	-7.43
std.		0.0764	0.0776	0.1359	0.1305	0.0764	0.0776	0.1944	0.2150	0.1205	0.15
bias	-	0.7633	0.7733	1.3514	2.0033	0.7633	0.7733	3.2803	3.5994	2.5981	7.12
,											
mean	5	5.0008	5.0003	-	-	-	-	-	-	-	
std.	-	0.0780	0.0789	-	-	-	-	-	-	-	
bias	-	1.0884	1.1039	-	-	-	-	-	-	-	
$\Delta \frac{X_{ij}Y_w}{Y_iY_j}$											
Y <sub>i</sub> Y <sub>j</sub> mean	23.8155	23.8488	23.8473	23.8913	22.944	19.2797	19.2779	25.0291	24.7589	18.9762	17.0
std.	89.7503	89.8462	89.841	23.8913 90.0318	87.0564	78.7351	78.731	92.7942	91.6696	78.7336	73.07
bias	-	0.71597	0.726	0.9867	1.4566	20.6474	20.6487	11.3734	11.2878	23.504	23.56
$EV_i$											
mean	-0.0880	-0.0906	-0.0909	-0.0878	-0.0941	-	-	-	-	-	
std.	7.7841	7.7875	7.7880	7.7914	7.6844	-	-	-	-	-	
bias		0.0658	0.0668	0.0587	0.0878	-	-	-	-	-	

Table 1: Monte Carlo results for model parameters, predicted trade flow changes and predicted welfare changes due to changing trade frictions in the case of a  $\sigma = 5$ 

Notes: For estimates of parameters  $(1 - \sigma)\rho$  and  $\sigma$ , the bias is expressed as a percent of the true value. For comparative statics, the bias is expressed in percentage points (as scaled trade flows and EVs are in percent already).

Table 2: Monte Carlo results for model parameters, predicted trade flow changes and predicted welfare changes due to changing trade frictions for asymmetric trade barriers

Estimates	True	Suggested model	A-vW	Asymmetric MR terms	BV-OLS 1	BV-OLS 2	OLS
(1)	(2)	uncorr. (3)	uncorr. (4)	uncorr. (5)	uncorr. (6)	uncorr. (7)	uncorr. (8)
(1)	(2)	(3)	(4)	(3)	(0)	(7)	(8)
(1)				10-country-wor	ld, $\sigma = 5$		
$(1 - \sigma)\rho$ mean	-8	-8.0109	-7.5044	-7.5044	-8.0109	-7.7438	-7.364
std.	-0	0.3367	0.7253	0.7253	0.3367	0.5553	0.656
bias	-	3.3200	8.2477	8.2477	3.3200	6.0877	9.127
$\sigma$ mean	5	5.0023	-	-	-	-	
std.	-	0.1568	-	-	-	=	
bias	-	0.4920	-	-	-	-	
$\Lambda \frac{X_{ij}y_w}{2}$							
$\Delta y_i y_j$							
mean	22.3160	22.4589	24.1205	215.4520	15.3214	31.2530	13.310
std. bias	86.8816	87.5805	$94.3536 \\71.9292$	238.2345 214.0877	70.2269 27.0730	$104.7547 \\ 19.6068$	69.657
DIAS	-	2.9881	71.9292	214.0877	27.0730	19.6068	32.732
$EV_i$	0 5 5 0 5	0.0100	0.0050	1.0504			
mean std.	-0.5725 8.1963	-0.6139 8.3581	-0.2673 11.0434	$1.2564 \\ 27.4305$	-	-	
bias	0.1903	0.2318	4.1761	19.4047	-	-	
bias	_	0.2010	4.1101	15.4041	_		
<i>.</i>				20-country-wor	ld, $\sigma = 5$		
$(1 - \sigma)\rho$	-8	-8.0046	-7.4694	7 4604	-8.0046	-7.6565	-7.661
mean std.	-8	-8.0046 0.1661	-7.4694 0.3396	-7.4694 0.3396	-8.0046 0.1661	-7.6565 0.3692	-7.66.
bias		1.6546	6.8180	6.8180	1.6546	5.0570	4.847
$\sigma$ mean	5	5.0022					
std.	-	0.0938	-	_	-	-	
bias	-	1.4822	-	-	-	-	
$\Lambda \frac{X_{ij}y_w}{x_{ij}y_w}$							
$\Delta y_i y_j$							
mean	26.8187	26.8728	20.4185	245.8379	18.4036	32.1303	16.66
std.	96.5832	96.7879	85.7540	248.5817	75.4258	106.7482	75.66
bias	-	1.3659	82.2296	245.4074	30.7439	16.1918	33.52
$EV_i$							
mean std.	-0.4462 7.6639	-0.4681 7.5996	$0.4835 \\ 10.4687$	4.2408 27.1873	-	-	
std. bias	1.0039	0.0523	4.3126	19.5352	-	-	
5145		0.0023	4.0120	13.0002	-	-	
(1)				40-country-wor	ld, $\sigma = 5$		
$(1 - \sigma)\rho$ mean	-8	-8.0018	-7.6168	-7.6168	-8.0018	-7.7064	-7.738
std.	-8	0.0774	0.1813	0.1813	0.0774	0.3294	0.110
bias	-	0.7717	4.8089	4.8089	0.7717	3.9873	3.28
σ							
mean	5	5.0011	-	-	-	-	
std.	-	0.0476	-	-	-	-	
bias	-	0.7560	-	-	-	-	
$\Lambda \frac{X_{ij}y_w}{2}$							
$\Delta y_i y_j$	00.10.1	00	05 1500	000 100-	10 001	00 00	
mean	22.1344	22.1512	25.1593	268.1988	19.3311	22.7766	18.64
std. bias	89.3596	$89.4200 \\ 0.5848$	88.2318 81.5282	253.0506 264.1394	79.2633 21.9378	$90.3994 \\ 10.9780$	78.63 25.08
$EV_i$ mean	0.1282	0.1278	-0.4662	3.3475	-	-	
std.	5.7528	5.7523	7.7350	29.3336	-	-	
bias	1	0.0200	3.8352	22.5496			

Notes: For estimates of parameters  $(1 - \sigma)\rho$  and  $\sigma$ , the bias is expressed as a percent of the true value. For comparative statics, the bias is expressed in percentage points (as scaled trade flows and EVs are in percent already).

Estimates	A-vW	Fixed Effects	Suggested model
(1)	(2)	(3)	(4)
Parameters			
$(1 - \sigma)\rho$	-0.788	-1.252	-1.252
	(0.032)	(0.037)	(0.037)
$(1 - \sigma) \ln b_{US,CA}$	-1.646	-1.551	-1.551
	(0.077)	(0.059)	(0.059)
σ	· _	_	11.892
$R^2$	0.435	0.664	0.664
$\sigma^2$	1.062	0.841	0.841

Table 3: Estimation results for the A-vW data-set

Trade effects of border barrier abolition

Overall			
mean	42.806	61.388	72.157
min	-82.823	-71.685	-64.820
max	211.487	277.512	293.530
std.	79.300	99.307	112.366
Intra-US trade			
mean	5.924	10.430	58.541
min	-51.746	-35.178	-20.036
max	208.110	274.571	292.052
std.	39.599	52.280	103.419
Intra-CA trade			
mean	19.055	51.503	67.459
min	-82.823	-71.685	-63.599
max	209.755	263.328	293.530
std.	102.968	116.319	136.396
Inter trade			
mean	98.533	134.879	92.108
min	-82.823	-71.685	-64.820
max	211.487	277.512	293.530
std.	84.758	101.426	117.374

#### Welfare effects of border barrier abolition (equivalent variation)

Overall	10.984	6.660	1.847
US	1.428	1.179	0.541
CA	39.654	23.105	5.765

Average of  $P^{(1-\sigma)}$ 

With border barrier (BE	3)		
US	0.773	0.530	0.530
	(0.015)	(0.020)	(0.020)
CA	2.451	1.787	1.787
	(0.060)	(0.062)	(0.062)
Borderless trade (NB)			. ,
US	0.754	0.519	0.518
	(0.015)	(0.019)	(0.019)
CA	1.179	1.136	1.147
	(0.004)	(0.013)	(0.013)
Ratio (BB/NB)			
US	1.025	1.022	1.022
	(0.001)	(0.001)	(0.001)
CA	2.079	1.573	1.558
	(0.057)	(0.037)	(0.036)

Impact of border barriers on bilateral trade

Ratio (BB/NB)

US-US	1.050	1.044	1.045
	(0.002)	(0.002)	(0.002)
CA-CA	4.321	2.475	2.428
	(0.237)	(0.115)	(0.113)
US-CA	0.411	0.341	0.322
	(0.023)	(0.018)	(0.017)
Due to bilateral resis	stance		
US-US	1.000	1.000	1.000
	(0.000)	(0.000)	(0.000)
CA-CA	1.000	1.000	1.000
	(0.000)	(0.000)	(0.000)
US-CA	0.193	0.212	0.202
	(0.015)	(0.012)	(0.012)
Due to multilateral r	esistance		
US-US	1.050	1.044	1.045
	(0.002)	(0.002)	(0.002)
CA-CA	4.321	2.475	2.428
Table 3 continued on	next page		

Table 3	continued	$\operatorname{from}$	previous	page

Estimates	A-vW	Fixed Effects	Suggested model
(1)	(2)	(3)	(4)
	(0.237)	(0.115)	(0.113)
US-CA	2.130	1.608	1.592
	(0.060)	(0.039)	(0.038)

# Impact of border barriers on intranational trade relative to international trade

US	2.557	3.061	3.249
	(0.146)	(0.159)	(0.162)
CA	10.524	7.258	7.55
	(1.048)	(0.526)	(0.520)
McCallum param	eter implied by th	eory	
US	1.635	1.398	1.46
	(0.103)	(0.074)	(0.074)
CA	16.455	15.899	16.70
	(1.485)	(1.042)	(1.042)

Table 4: Estimation results for the A-vW data-set with asymmetric border barriers

Estimates	A-vW	Fixed Effects	Suggested model
(1)	(2)	(3)	(4)
Parameters			
$(1 - \sigma)\rho$	-0.792	-1.252	-1.252
	(0.032)	(0.037)	(0.037)
$(1 - \sigma) \ln b_{US}$	-1.378	-0.470	-0.470
	(0.086)	(0.046)	(0.046)
$(1 - \sigma) \ln b_{CA}$	-1.808	-0.825	-0.825
	(0.105)	(0.047)	(0.047)
$\sigma$		· _	6.340
$R^2$	0.444	0.664	0.664
$\sigma^2$	1.053	0.841	0.841

#### Trade effects of border barrier abolition

mean	45.794	81.561	16.097
min	-79.421	-8.429	-45.156
max	281.862	221.258	143.273
std.	88.427	54.886	44.586
Intra-US trade			
mean	2.164	55.093	-0.081
min	-48.986	26.220	-11.254
max	145.580	124.129	19.469
std.	27.978	13.579	5.808
Intra-CA trade			
mean	47.351	88.898	30.282
min	-79.421	-8.429	-44.184
max	279.564	220.568	143.273
std.	130.059	85.701	74.233
Inter trade			
mean	107.186	117.829	36.782
min	-79.421	-8.429	-45.1556
max	281.862	221.258	142.782
std.	99.553	63.499	58.153

#### Welfare effects of border barrier abolition (equivalent variation)

Overall	9.978	2.970	1.740
US	1.543	0.795	0.767
CA	35.281	9.493	4.660

Table 5: Estimation results for the GTAP data-set

	Estimates	Suggested					
	Estimates	model					
	(1)	(2)					
Par	ameters						
	$-\sigma\kappa$	-1.865					
		(0.063)					
	$(1 - \sigma)\rho$	-1.056					
		(0.029)					
	$(1 - \sigma) \ln b_1$	0.442					
		(0.079)					
	$(1 - \sigma) \ln b_2$	0.658					
		(0.135)					
	$(1 - \sigma) \ln b_3$	0.416					
		(0.125)					
	$(1 - \sigma) \ln b_4$	0.284					
		(0.157)					
	$\sigma$	7.380					
$R^2$		0.861					
$\sigma^2$		1.089					
Trade effects of world-wide abolition of import duties							
a	bolition of imp						
a	bolition of imp erall	ort duties					
a	bolition of imp erall mean	ort duties 167.594					
a	bolition of imp erall mean min	ort duties 167.594 -94.702					
a	bolition of imp erall mean	ort duties 167.594					
a Ove	bolition of imp erall mean min max	ort duties 167.594 -94.702 78921.000 2293.100 world-wide ort duties					

Estimates	True		ested del	A	vW	BV-C	DLS 1	BV-0	DLS 2	0	LS
(1)	(2)	uncorr. (3)	corr. (4)	uncorr. (5)	corr. (6)	uncorr. (7)	corr. (8)	uncorr. (9)	corr. (10)	uncorr. (11)	corr. (12)
	10-country-world, $\sigma = 3$										
$(1 - \sigma)\rho$ mean std. bias	-4 - -	-4.0136 0.1698 3.3738	-4.0194 0.1690 3.3803	-4.0119 0.3167 6.2824	-4.0035 0.2881 5.8070	-4.0136 0.1698 3.3738	-4.0194 0.1690 3.3803	-3.9321 0.3235 6.5394	-4.0462 0.3411 7.0723	-3.7571 0.2799 7.5737	-3.2041 0.3539 19.9271
$\sigma$ mean std. bias	3 - -	$3.0080 \\ 0.1153 \\ 3.0183$	$3.0129 \\ 0.1153 \\ 3.0335$	- -	- -	- -	- -	- - -	- -	- - -	-
$\begin{array}{c} \Delta \frac{X_{ij}Y_w}{Y_iY_j} \\ \text{mean} \\ \text{std.} \\ \text{bias} \end{array}$	6.6662 36.9948 -	6.7489 37.2688 0.9934	6.7416 37.2623 0.9887	6.6014 37.1356 1.6633	6.8860 38.1079 1.5481	3.5120 27.7128 15.2644	$3.5190 \\ 27.7392 \\ 15.2651$	8.2709 41.0057 4.4485	9.3040 44.4533 5.3880	3.2435 27.8818 17.8267	2.3500 23.5375 17.6405
$EV_i$ mean std. bias	0.2351 14.1707 -	$0.2304 \\ 14.1729 \\ 0.1355$	0.2317 14.1630 0.1352	-0.0611 7.4562 4.3464	-0.0875 7.5313 4.3028	- - -	- - -	- - -	- - -	- - -	-
					20-cou	ntry-world,	$\sigma = 3$				
$(1 - \sigma)\rho$ mean std. bias	-4 - -	-4.0034 0.0787 1.5676	-4.0043 0.0785 1.5565	-4.0033 0.1926 3.7673	-3.8925 0.1841 4.3525	-4.0034 0.0787 1.5676	-4.0043 0.0785 1.5565	-3.9528 0.2024 4.0657	-3.9859 0.1871 3.7943	-3.7878 0.1631 5.5451	-3.1911 0.2800 20.2220
$\sigma \ { m mean} \ { m std.} \ { m bias}$	3 - -	$3.0032 \\ 0.0926 \\ 2.1690$	$3.0044 \\ 0.0919 \\ 2.1483$	- -	- - -	- -	- - -	- - -	- - -	- - -	-
$\begin{array}{c} \Delta \frac{X_{ij}Y_w}{Y_iY_j} \\ \text{mean} \\ \text{std.} \\ \text{bias} \end{array}$	5.4797 35.3275 -	5.4923 35.3767 0.4772	5.4933 35.3852 0.4750	5.4408 35.4044 1.0460	5.1722 34.3500 1.1888	4.4173 31.3472 11.3259	4.4194 31.3551 11.3260	$\begin{array}{c} 6.0417 \\ 36.6611 \\ 3.7866 \end{array}$	6.0668 36.8558 3.7163	$3.7566 \\ 31.1362 \\ 13.1648$	2.5930 25.9515 13.4517
$EV_i$ mean std. bias	$0.1196 \\ 9.8557 \\ -$	$\begin{array}{c} 0.1184 \\ 9.8611 \\ 0.1346 \end{array}$	$\begin{array}{c} 0.1187 \\ 9.8581 \\ 0.1339 \end{array}$	-0.0231 5.2396 3.4358	-0.0290 5.1146 3.5203	- -	- - -	- - -	- - -	- - -	
					40-cou	ntry-world,	$\sigma = 3$				
$(1 - \sigma)\rho$ mean std. bias	-4 - -	-4.0021 0.0380 0.7595	-4.0017 0.0382 0.7626	-4.0011 0.0868 1.7105	-3.9242 0.0997 2.6967	-4.0021 0.0380 0.7595	-4.0017 0.0382 0.7626	-3.9462 0.0975 2.1731	-3.9459 0.0972 2.2230	-3.8842 0.0694 2.9590	-3.545 0.1030 11.369
$\sigma$ mean std. bias	3	$3.0016 \\ 0.0286 \\ 0.7539$	$3.0013 \\ 0.0288 \\ 0.7585$	- - -	- - -	- - -	- - -	- - -	- - -	- - -	
$\begin{array}{c} \Delta \frac{X_{ij}Y_w}{Y_iY_j} \\ \text{mean} \\ \text{std.} \\ \text{bias} \end{array}$	4.7364 33.7559 -	4.7431 33.7794 0.2050	4.7416 33.7748 0.2058	4.6834 33.7530 0.4662	4.5225 33.0860 0.7302	4.4345 31.4914 9.0524	4.4335 31.4874 9.0524	4.7299 34.1411 2.2595	4.7390 34.1706 2.2712	4.5261 31.2879 9.8183	3.774 28.254 9.945
$EV_i$ mean std. bias	0.4752 7.0784	$0.4748 \\ 7.0774 \\ 0.0190$	$0.4749 \\ 7.0777 \\ 0.0191$	$0.1975 \\ 3.7986 \\ 2.5146$	0.1907 3.7388 2.5626	-	- -	- -	-	-	

Table A1: Monte Carlo results for model parameters, predicted trade flow changes and predicted welfare changes due to changing trade frictions in the case of a  $\sigma = 3$ 

Notes: For estimates of parameters  $(1 - \sigma)\rho$  and  $\sigma$ , the bias is expressed as a percent of the true value. For comparative statics, the bias is expressed in percentage points (as scaled trade flows and EVs are in percent already).

Estimates	True			el A-VW		BV-OLS 1		BV-OLS 2		OLS	
(1)	(2)	uncorr. (3)	corr. (4)	uncorr. (5)	corr. (6)	uncorr. (7)	corr. (8)	uncorr. (9)	corr. (10)	uncorr. (11)	corr. (12)
					10-c	ountry-world	l, $\sigma = 10$				
$(1 - \sigma)\rho$ mean	-18	-18.1151	-18.0950	-18.0302	-17.3963	-18.1151	-18.0950	-16.4232	-16.3901	-18.0739	-17.439
std.	-10	0.7788	0.7756	0.8402	0.7863	0.7788	0.7756	2.6003	2.5866	1.0715	1.106
bias	-	3.4823	3.4579	3.7112	4.4491	3.4823	3.4579	13.1853	13.1519	4.7878	5.486
σ											
mean	10	10.0318	10.0207	-	-	-	-	-	-	-	
std. bias	-	$0.5865 \\ 4.1089$	$0.5889 \\ 4.0843$	-	-	-	-	-	-	-	
$X_{i,i}Y_{ij}$											
$\Delta \frac{X_{ij}Y_w}{Y_iY_j}$	100.0010										
mean std.	123.3248 469.3185	$127.7351 \\ 494.9210$	$127.5996 \\ 495.4916$	$125.6036 \\ 485.1469$	113.0115 432.9379	91.1245 293.4474	90.9670 293.1617	227.5535 1128.8546	233.1863 1204.7017	$129.9514 \\ 521.3890$	116.239 453.921
bias	-	17.5295	17.4202	15.3387	16.9658	74.4546	74.4805	214.5082	219.7298	92.7117	85.544
$EV_i$											
mean std.	$0.1390 \\ 7.0641$	$0.1034 \\ 7.0674$	$0.1056 \\ 7.0776$	$0.9072 \\ 15.5048$	$0.9780 \\ 15.6467$	-	-	-	-	-	
bias	7.0041	0.3054	0.3043	5.4158	5.6047	-	-	-	-	-	
					20-c	ountry-world	l, $\sigma = 10$				
$(1 - \sigma)\rho$ mean	-18	-18.0253	-18.0327	-18.0037	-17.5787	-18.0253	-18.0327	-15.6098	-15.5545	-17.6570	-17.061
std.	-	0.3721	0.3759	0.4886	0.5454	0.3721	0.3759	2.1116	2.0400	0.6485	0.682
bias	-	1.6554	1.6777	2.1710	3.1475	1.6554	1.6777	14.1517	13.9282	3.3918	5.658
σ	10	10 0001	0.0010								
mean std.	10	$     \begin{array}{r}       10.0001 \\       0.7965     \end{array} $	$9.9912 \\ 0.7933$	-	-	-	-	-	-	-	
bias	-	4.3285	4.3509	-	-	-	-	-	-	-	
$\Delta \frac{X_{ij}Y_w}{Y_iY_j}$											
$Y_i Y_j$ mean	137.9529	139.7014	139.9970	139.2621	129.7217	129.4379	129.5752	136.3740	133.9121	139.7465	125.707
std.	509.0532	516.9189	517.5073	516.0786	476.7905	471.1198	471.2312	531.6067	509.3490	536.1079	474.690
bias	-	11.2513	11.3483	10.0604	13.7876	80.4346	80.4387	116.1598	114.3426	79.3370	76.585
$EV_i$ mean	0.5568	0.5251	0.5120	1.6953	1.6870						
std.	6.5455	7.0969	6.6141	14.3039	14.3381	-	-	-	-	-	
bias	-	0.2931	0.2868	5.5801	5.6378	-	-	-	-	-	
$(1 - \sigma)\rho$					40-c	ountry-world	l, $\sigma = 10$				
mean	-18	-18.0035	-18.0024	-17.7132	-17.4493	-18.0035	-18.0024	-15.4103	-15.4223	-17.5999	-17.231
std. bias	-	$0.1831 \\ 0.8119$	$0.1838 \\ 0.8141$	$0.3260 \\ 1.9529$	$0.3568 \\ 3.1321$	$0.1831 \\ 0.8119$	$0.1838 \\ 0.8141$	$0.8177 \\ 14.3872$	$0.8364 \\ 14.3203$	$0.3311 \\ 2.3740$	$0.361 \\ 4.274$
Dias	-	0.8119	0.8141	1.9529	3.1321	0.8119	0.8141	14.3872	14.3203	2.3740	4.274
$\sigma$ mean	10	9.9974	10.0029	-	-	-	-	-	-	-	
std.	-	1.0969	1.0989	-	-	-	-	-	-	-	
bias	-	5.5566	5.5380	-	-	-	-	-	-	-	
$\Delta \frac{X_{ij}Y_w}{Y_iY_j}$											
mean	192.7730	196.6792	196.5124	185.2525	177.1900	154.7657	154.7352	177.6109	177.6029	160.0134	149.959
std.	714.2798	736.2606	735.6959	686.9376	652.4061	574.5780	574.4365	787.0798	792.4892	574.2420	532.356
bias	-	19.2990	19.1996	11.3912	17.6107	112.1997	112.2014	146.8040	146.9326	111.2852	111.364
$EV_i$ mean	0.2995	0.1826	0.1867	1.2536	1.2613	_	_			_	
std.	7.4031	7.6870	7.6855	16.2158	16.1786	-	-	-	-	-	
bias	-	0.5404	0.5367	6.5144	6.5101	-	-	-	-	-	

Table A2: Monte Carlo results for model parameters, predicted trade flow changes and predicted welfare changes due to changing trade frictions in the case of a  $\sigma = 10$ 

Notes: For estimates of parameters  $(1 - \sigma)\rho$  and  $\sigma$ , the bias is expressed as a percent of the true value. For comparative statics, the bias is expressed in percentage points (as scaled trade flows and EVs are in percent already).