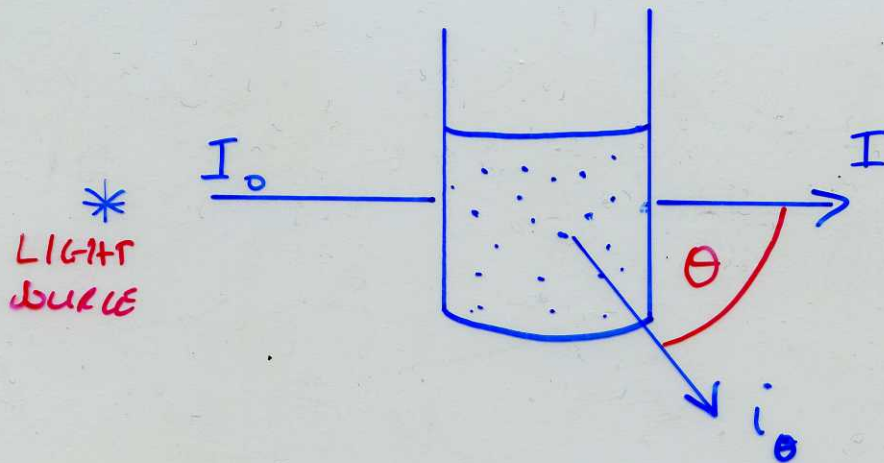


# LIGHT SCATTERING



## 2 MAIN TYPES

### ① CLASSICAL or "STATIC" LIGHT SCATTERING

- Measure scattered intensity  $i_\theta$  as a function of angle  $\theta$   $\longrightarrow$   $M_w$  (weight average molecular weight)  
 $R_g$  (radius of gyration)

### ② DYNAMIC or "QUASI-ELASTIC" LIGHT SCATTERING

- Measure rapid fluctuations of  $i_\theta$  as a function of time  $t$   $\longrightarrow$   $D$  (diffusion coefficient)

# CLASSICAL LIGHT SCATTERING

..... for characterisation of biomolecular  
molecular weights and conformations (via  
"radius of gyration,"  $R_g$ )





TYNDALL IN 1864

From a drawing by G. Richmond, R.A., at the Royal Institution

The blue colour of the sky and the polarisation of skylight . . . constitute, in the opinion of our most eminent authorities, the two great standing enigmas of meteorology. Indeed it was the interest manifested in them by Sir John Herschel in a letter of singular speculative power that caused me to enter upon the consideration of these questions so soon.

J. Tyndall, 1969

# Historical

17<sup>th</sup> C

SNELL  
NEWTON  
HUYGENS  
FERMAT

} NATURE OF LIGHT;  
GEOMETRIC OPTICS

19<sup>th</sup> C

YOUNG  
FRESNEL

} DIFFRACTION / INTERFERENCE

1865 : MAXWELL - ELECTROMAGNETIC  
THEORY

1869 : TYNDALL - LIGHT SCATTERING ;  
"THE 2 GREAT STANDING  
ENIGMAS"



From a drawing by --



J.C. MAXWELL





JOHN WILLIAM STRUTT (LORD RAYLEIGH)  
In 1872, aged 28, photographed by himself with a wet collodion plate



1881 : RAYLEIGH - SINGLE PARTICLE  
THEORY {SMALL  
SCATTERERS }

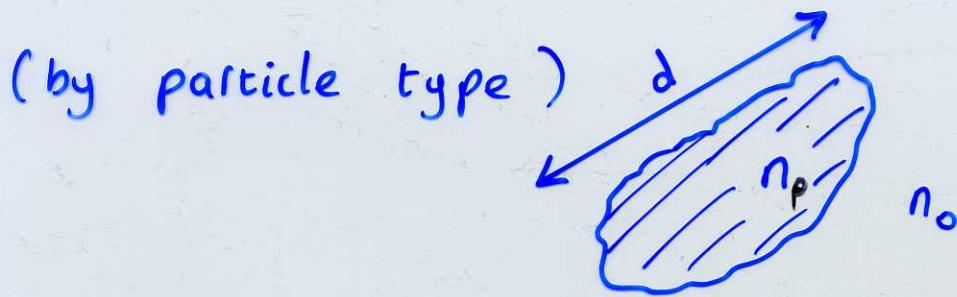
1890 : LORENZ }  
1908 : MIE } GENERAL THEORY  
DEBYE }

1914 : RAYLEIGH }  
1915 : DEBYE } APPROXIMATE THEORY  
1925 : GANS }

1908 : SMOLOCHOWSKI }  
1911 : EINSTEIN } THERMODYNAMIC THEORY  
OF SOLUTION SCATTERING

1947-50 : DEBYE }  
ZIMM } SCATTERING BY SOLUTIONS  
OF MACROMOLECULES

# Classification of Light Scattering



(1) Rayleigh  $d \lesssim \frac{\lambda}{20}$  (  $M \lesssim 40000$  )  
- Lysozyme, Myoglobin etc.

(2) Rayleigh - Gans - Debye (RGD)  $d \sim \lambda/20 \rightarrow \lambda$   
 $\frac{n_p}{n_0} - 1 \ll 1$  } OF MOST INTEREST!

(3) Mie  $d \gtrsim \lambda$  LARGE VIRUSES, BACTERIA etc.



# RAYLEIGH - GANS - DEBYE (RGD) SCATTERING.

- for biomolecules of  $M = 40000 \rightarrow 20 \times 10^6$

MEASURE A PARAMETER 'RAYLEIGH RATIO'

$$R_{\theta} = \frac{I_{\theta}}{I_0} \cdot \left[ \frac{r^2}{1 + \cos^2 \theta} \right]$$

*dir. of particle from detector*

LIGHT SCATTERING BY A SOLUTION OF MACROMOLECULES CAN BE SUMMARISED BY THE EQUATION:

$$\frac{KC}{R_{\theta}} \approx \left\{ 1 + \frac{16\pi^2 R_g^2}{3\lambda^2} \sin^2 \frac{\theta}{2} \right\} \left( \frac{1}{M} + 2BC \right)$$

$k$  is a collection of constants:  $\frac{2\pi^2 n_0^2 (dn/dc)^2}{N_A \lambda^4}$

$B$ : 2<sup>nd</sup> virial coeff. ;  $C$ : concentration

$R_g$ : "radius of gyration".

If  $B$  is known, or  $C$  is small enough ( $2BC \approx 0$ )

a plot of  $\frac{KC}{R_{\theta}}$  vs  $\sin^2 \frac{\theta}{2} \rightarrow$  Mol. wt &  $R_g$ .

ZIMM PLOT : ALGINATE POLYSACCHARIDE (M ~ 200,000)

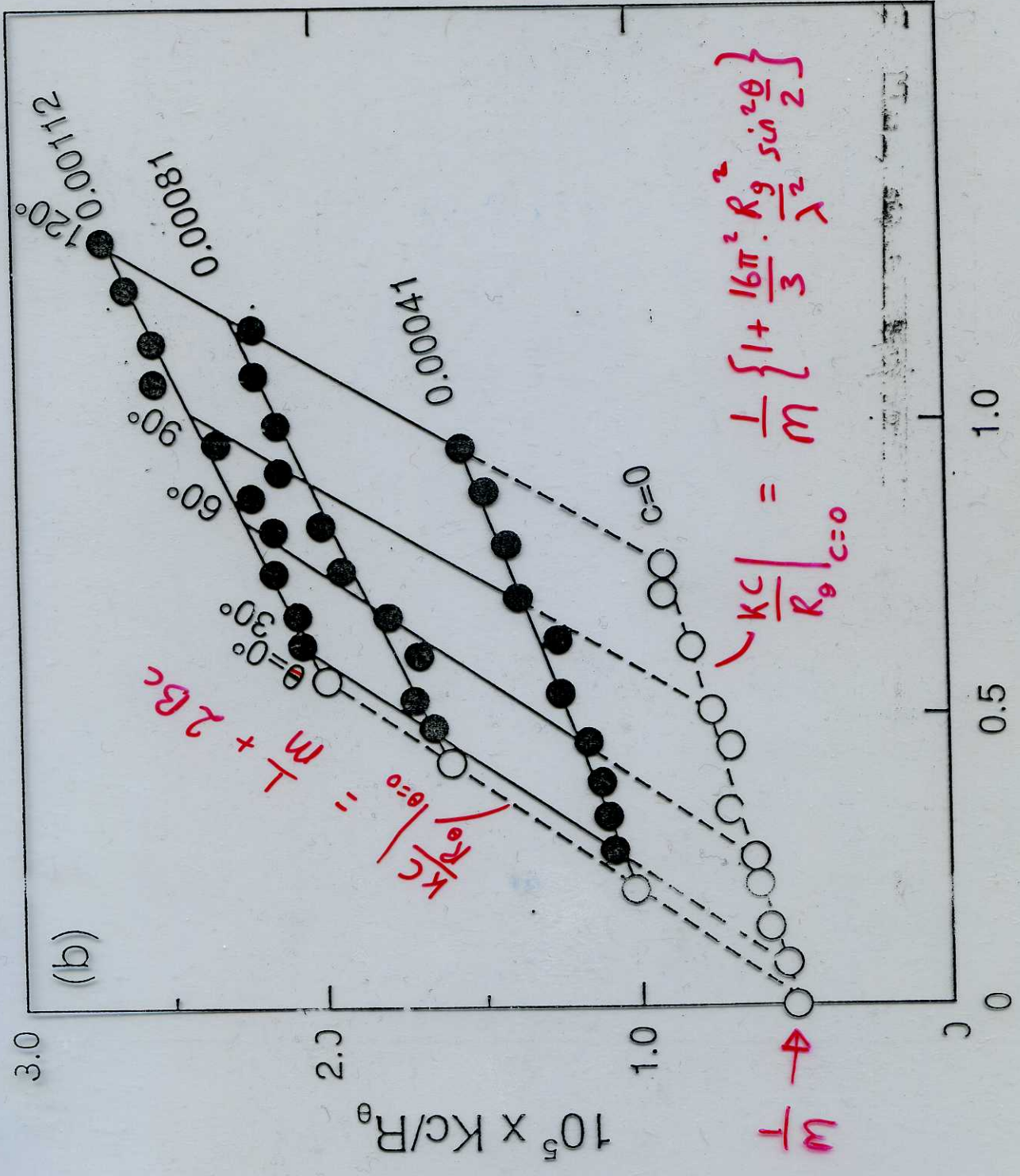
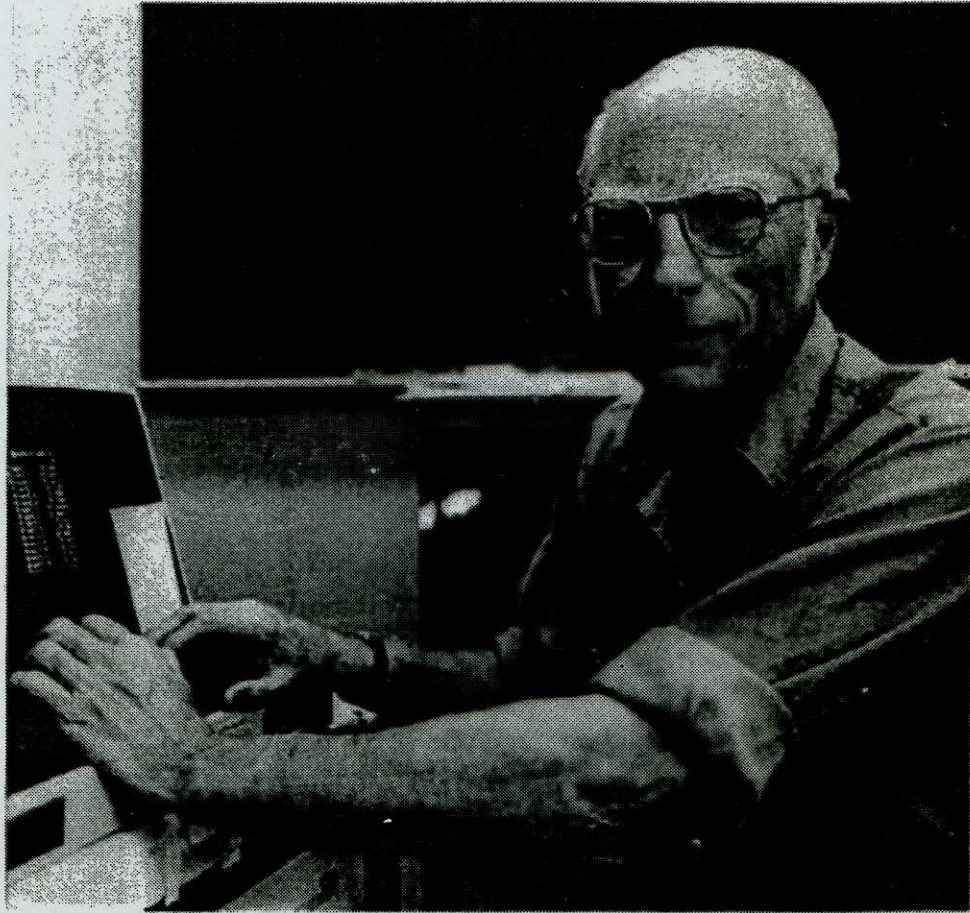


FIG 1(b)





*Bruno H. Zimm*

## CONFORMATIONAL ANALYSIS : "RADIUS OF GYRATION" $R_g$

Besides classical light scattering,  $R_g$  can also be obtained from solution x-ray scattering or neutron scattering. Why might these alternative techniques be more suitable for smaller biomolecules ( $M \lesssim 40000$ )?



# RADIUS OF GYRATION $R_g$



- root mean square  
distance of mass elements  
in a particle from centre  
of mass

SPHERE :  $R_g = \sqrt{\frac{3}{5}} R$   
(radius  $R$ )

ROD  $R_g = \frac{L}{\sqrt{12}}$   
(length  $L$ )

ELLIPSOID  $R_g = \sqrt{\frac{a^2 + b^2 + c^2}{5}}$   
(semi-axes  $a, b, c$ )

(nb. prolate  $c = b$   
oblate  $c = a$ )

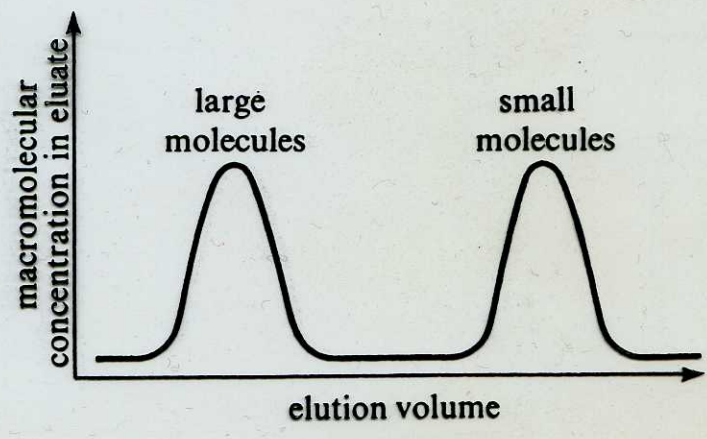
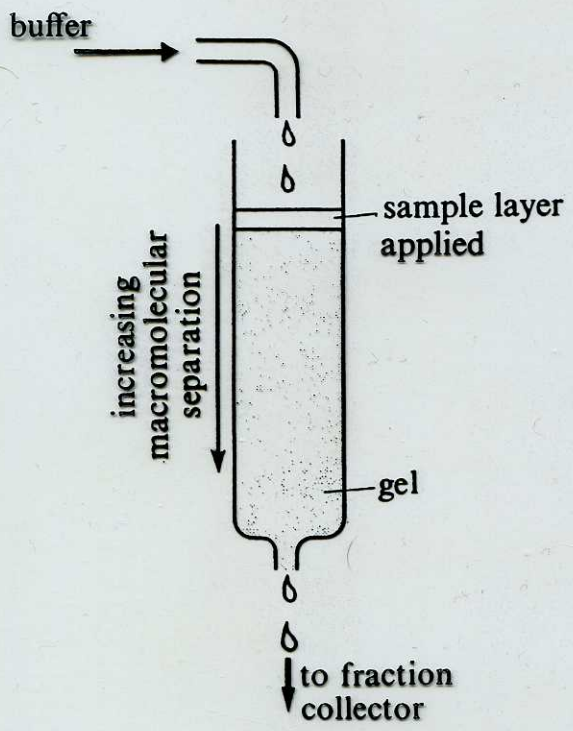
RANDOM COIL  $R_g = \frac{\langle R^2 \rangle^{\frac{1}{2}}}{\sqrt{6}}$   
(mean square end-to-end distance  $R^2$ )

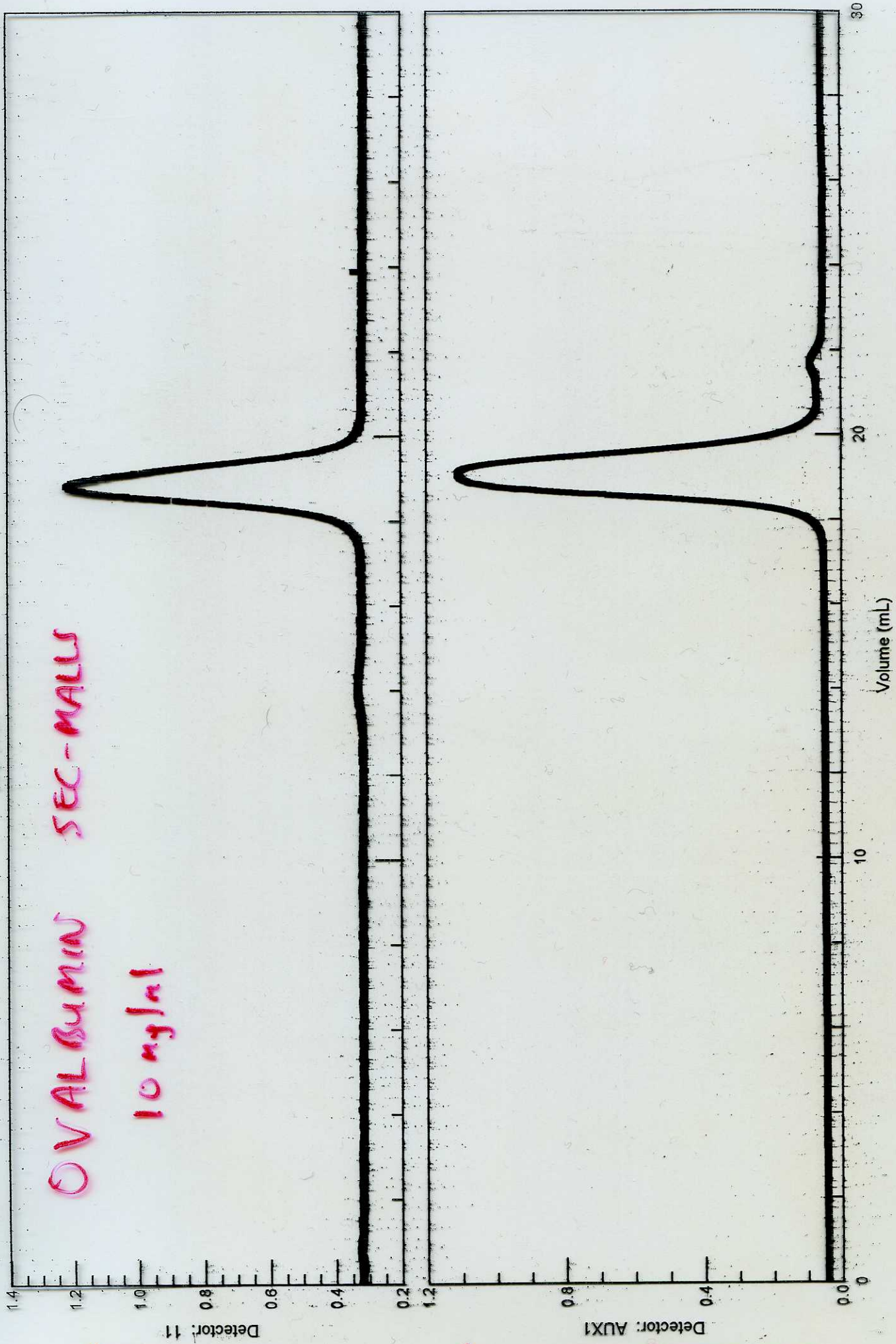
BEAD MODELS  $R_g = \text{some complicated function!}$

## Typical $R_g$ values

Material	M	$R_g$ (nm)	
Lysosyme	14,100	1.52	} globular
Serum albumin	70,000	2.98	
Turnip yellow mosaic virus	$5 \times 10^6$	30.0	
Mycosin	493,000	46.8	≈ rod
DNA sample	$4 \times 10^6$	117.0	≈ flexible coil





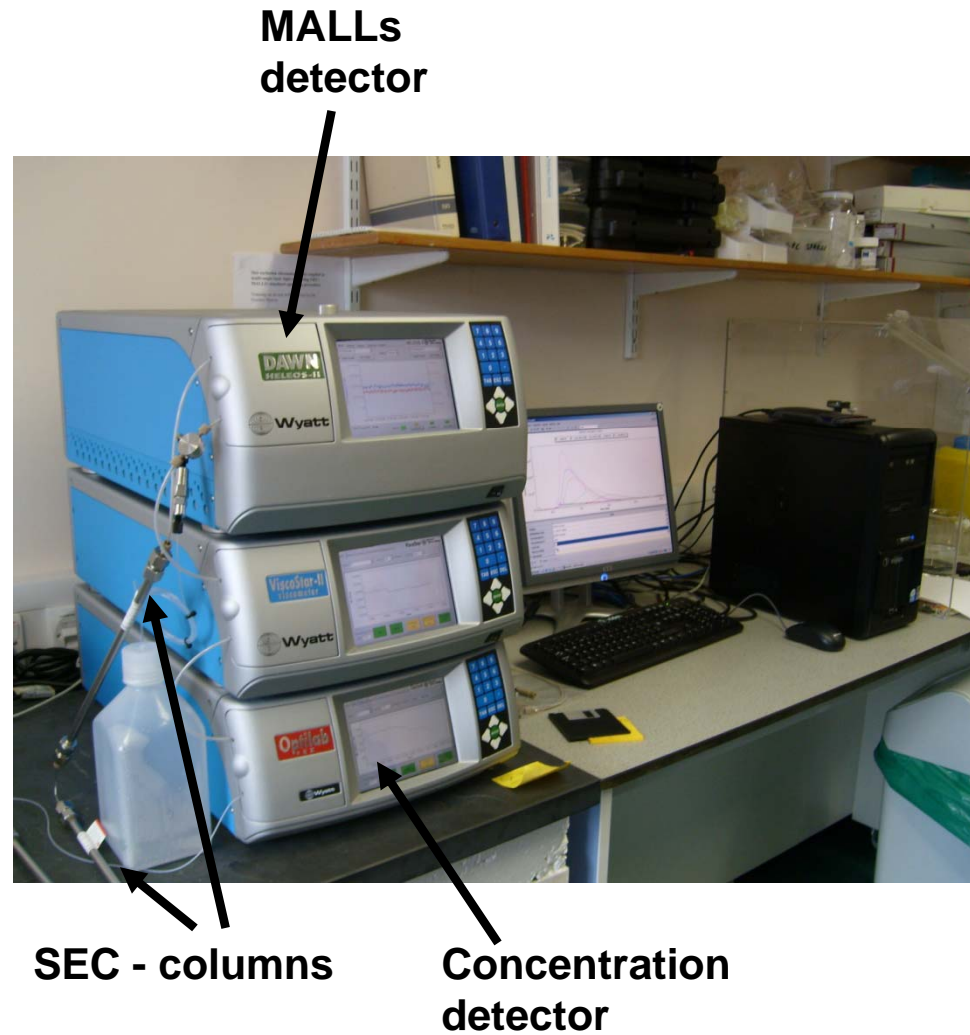


ovalbumin 10mg/ml  
C:\MARCIN\10OVAL.ADF  
ASTRA for Windows 4.73.04

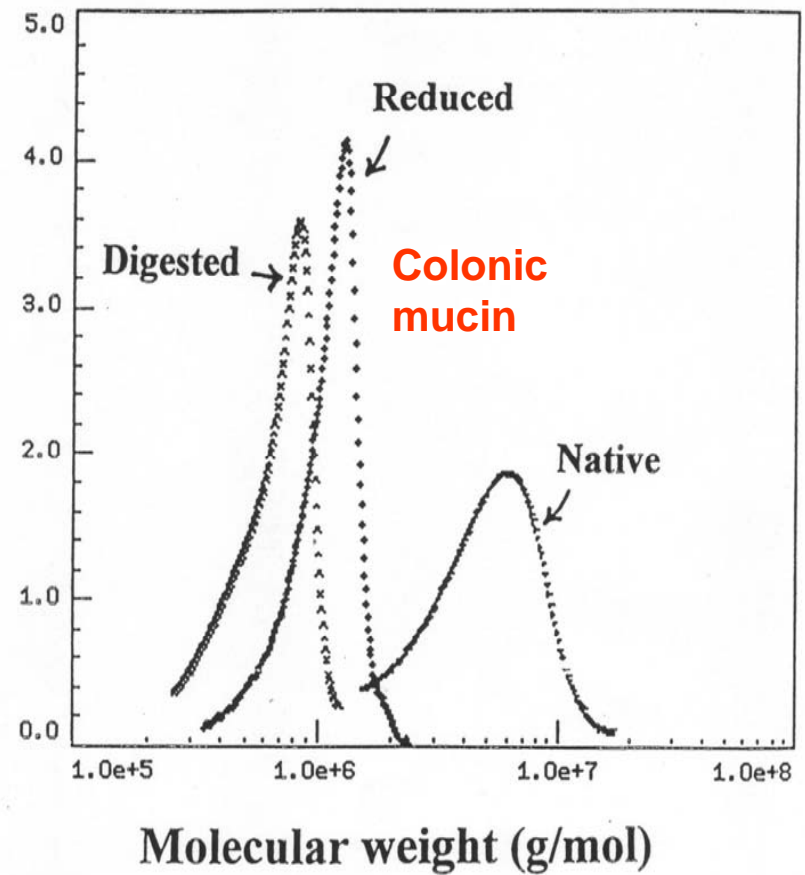
ELUTION VOLUME



# Molecular Weight: SEC-MALLS



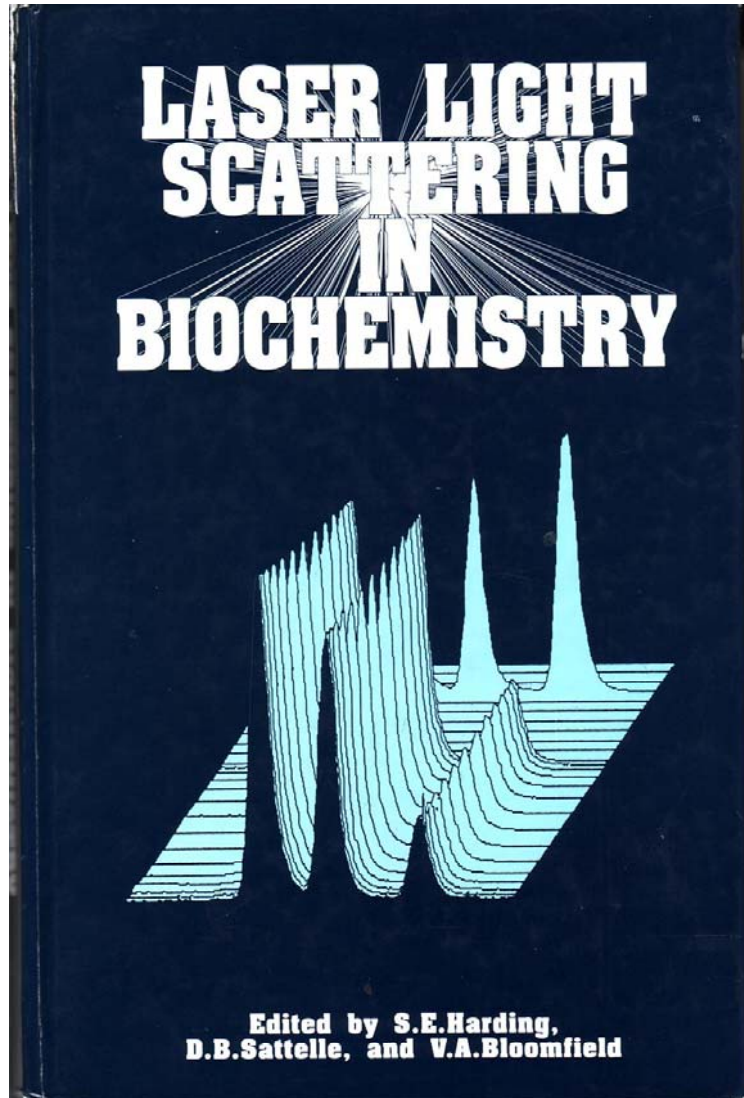
# Molecular Weight: SEC-MALLS



Fogg FJJ et al, *Biochemical Journal*.1996



# Molecular Weight: SEC-MALLS



3

## **Combined Differential Light Scattering with Various Liquid Chromatography Separation Techniques**

By Philip J. Wyatt

WYATT TECHNOLOGY CORPORATION, SANTA BARBARA, CALIFORNIA  
93130-3003, U.S.A.

### **1. INTRODUCTION**

The combination of light scattering measurements with various particle/molecular separation techniques often permits an unparalleled characterization of the separated particles. In a sense, this is but an application of the so-called "inverse scattering" problem<sup>1,2,3</sup> *i.e.* from measurements of the light scattering

Biochemical Society Transactions 19 (1991) 510-511

### **Gel permeation chromatography-multi-angle laser light scattering characterization of the molecular mass distribution of 'Pronova' sodium alginate**

J. C. Horton, S. E. Harding and J. R. Mitchell

University of Nottingham, Department of Applied Biochemistry and Food Science, School of Agriculture, Sutton Bonington, Loughborough, Leicestershire LE12 5RD, U.K.

A relatively recent innovation in total intensity laser light scattering has been to replace the isolated

fers of ionic strengths ( $I$ ) of 0.1 M and 0.3 M with concentrations ( $c$ ) in the range 0.5–5.0 mg/ml.

## Follow up bibliography:

1. On-line tutorials from: Wyatt Technology and Viscotek corporation (see their web sites)
2. Harding, S.E., Sattelle, D.B. & Bloomfield, VA. Eds (1992) *Laser Light Scattering in Biochemistry* Royal Soc. Chem. Cambridge – Particularly chapters by Wyatt and Rollings