



University of  
**Nottingham**

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Reliability Meeting

Thursday 9 June

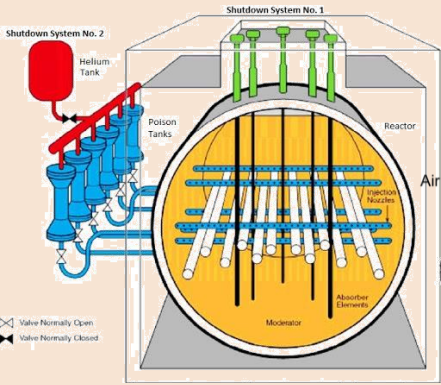
Durham

# Dynamic and Dependent Tree Theory for Event Trees

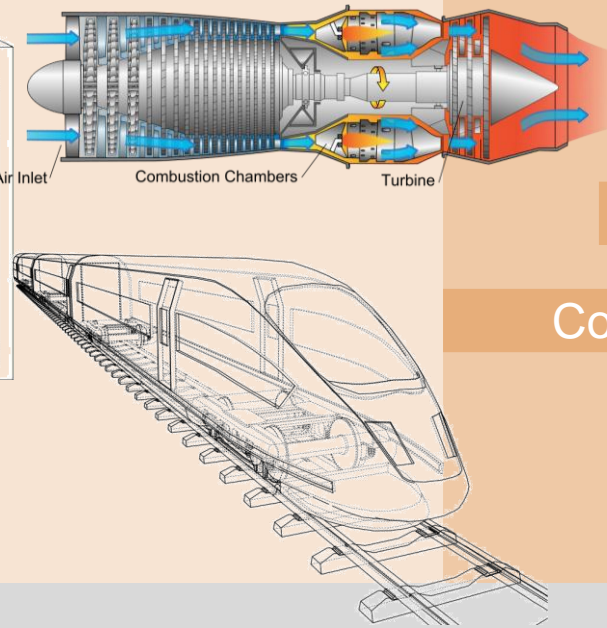
Silvia Tolo



## FAMILIAR MODELLING LANGUAGE



## REALISTIC RISK MODELLING



Dependencies

Non-Constant Failure Rates

Complex Maintenance Strategies

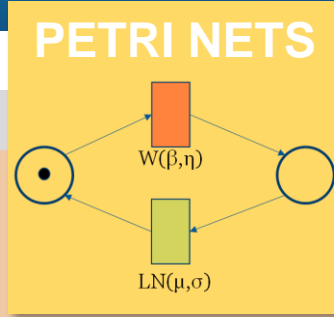
## ANALYSIS ACCURACY

- System Safety Metrics
- Failure Probability
- Failure Frequency
- Component Importance

## COMPUTATIONAL FEASIBILITY

# Methodology Overview...

Non-Constant Failure Rates



FT Modelling

BDD

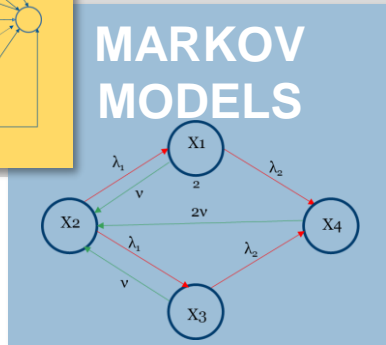
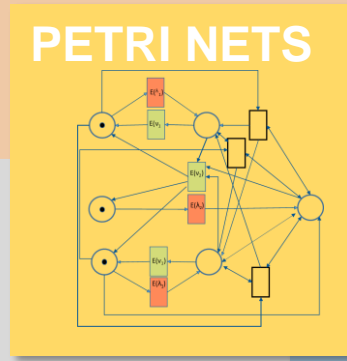
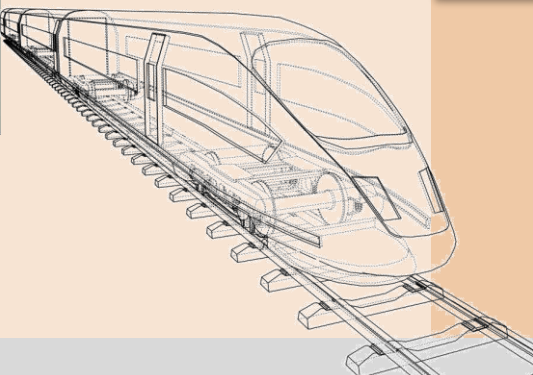
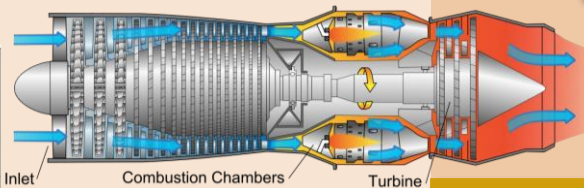
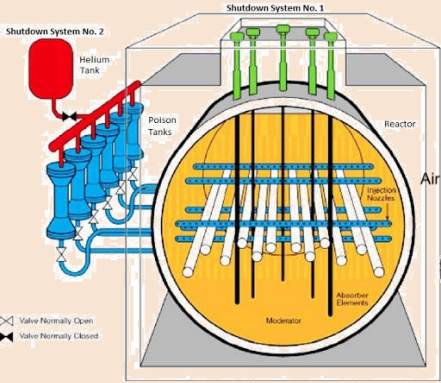
- System Safety Metrics
- Failure Probability
- Failure Frequency
- Component Importance

Dependencies

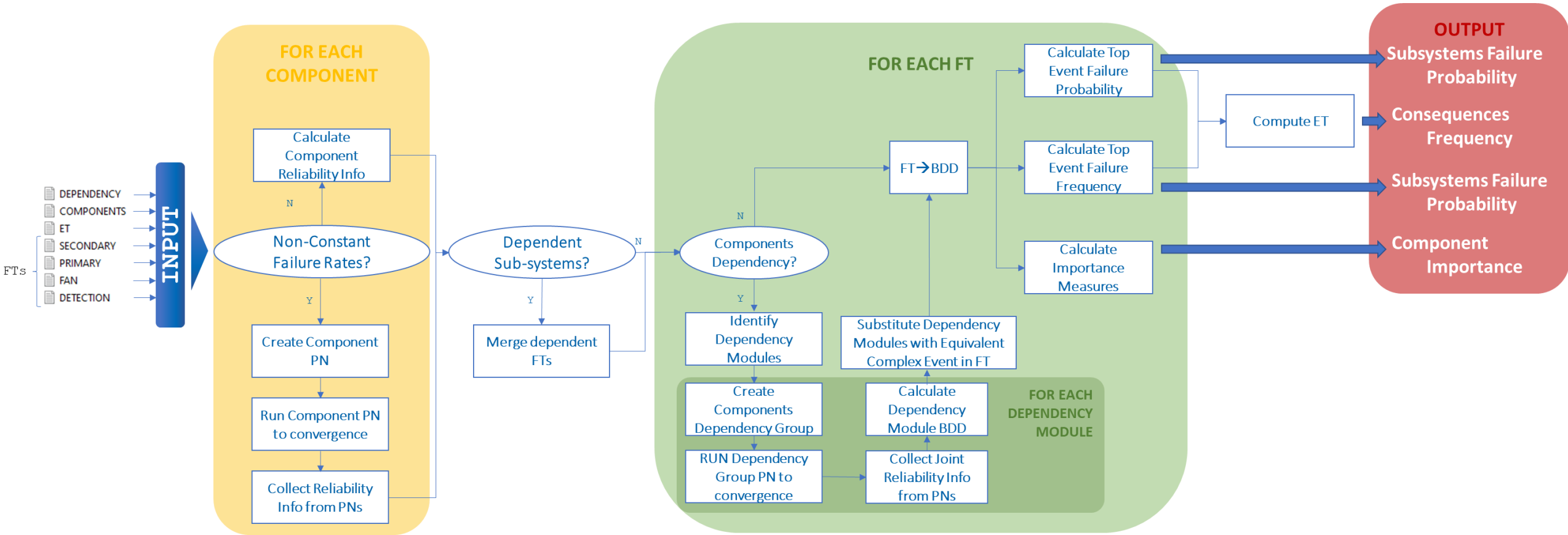
PETRI NETS

MARKOV MODELS

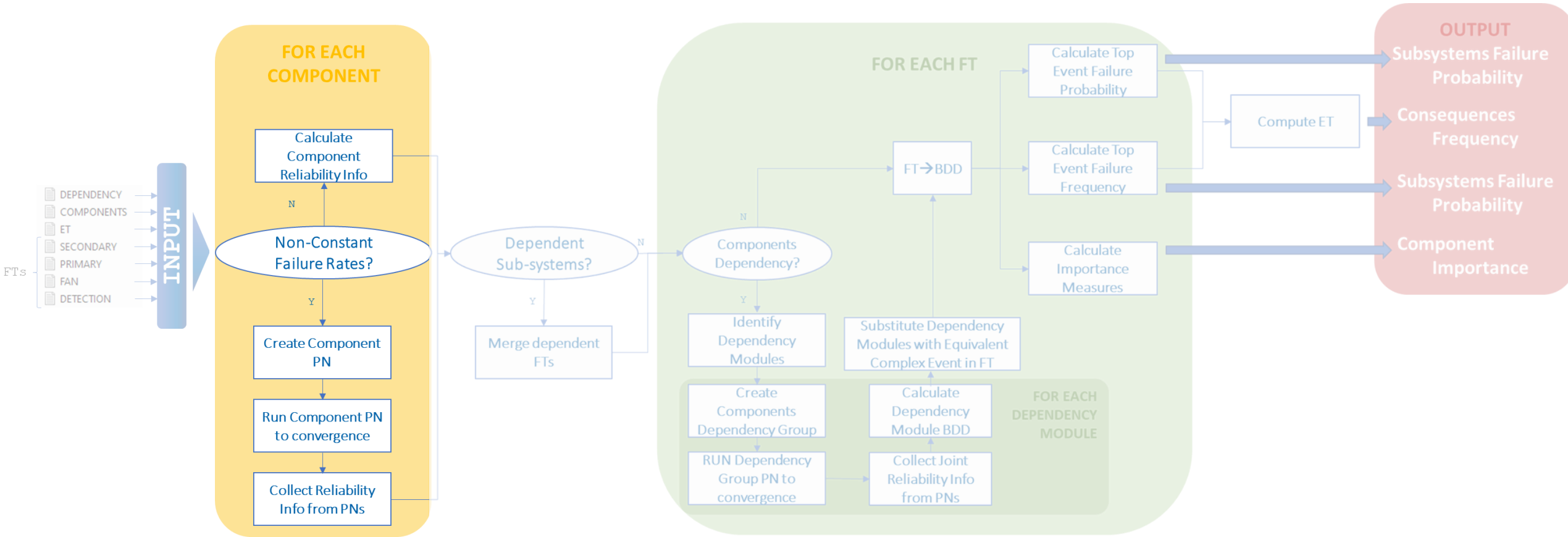
Complex Maintenance Strategies



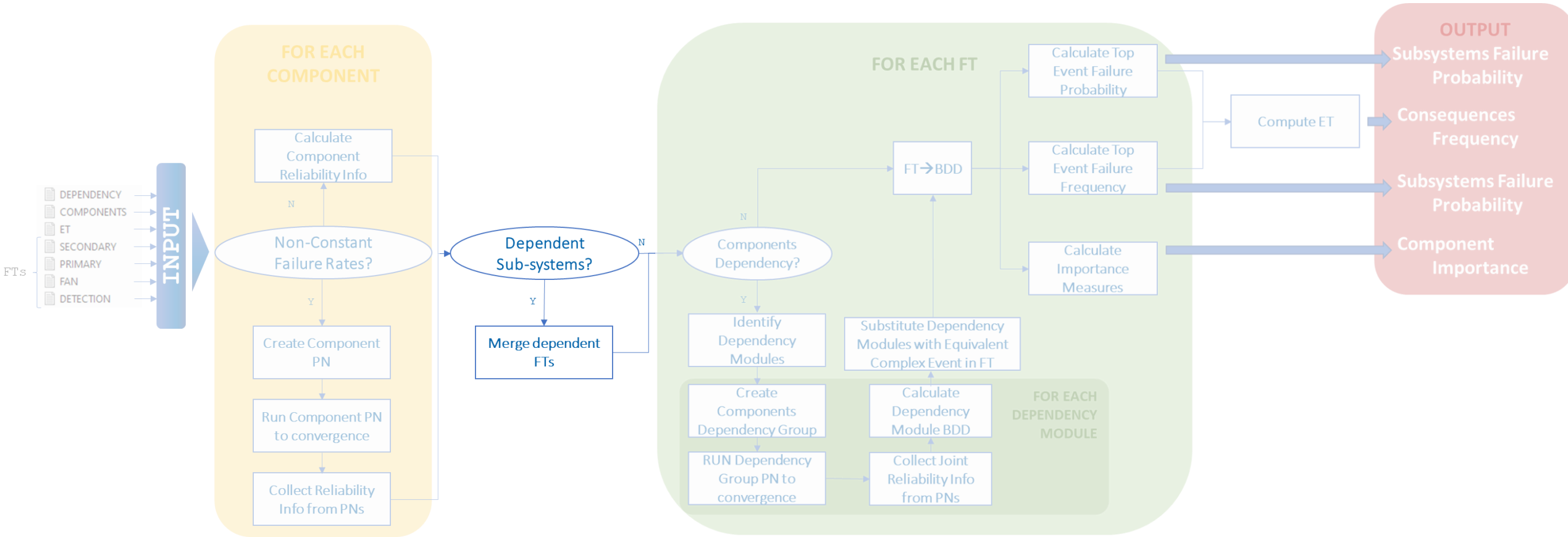
# ...in 5 Steps



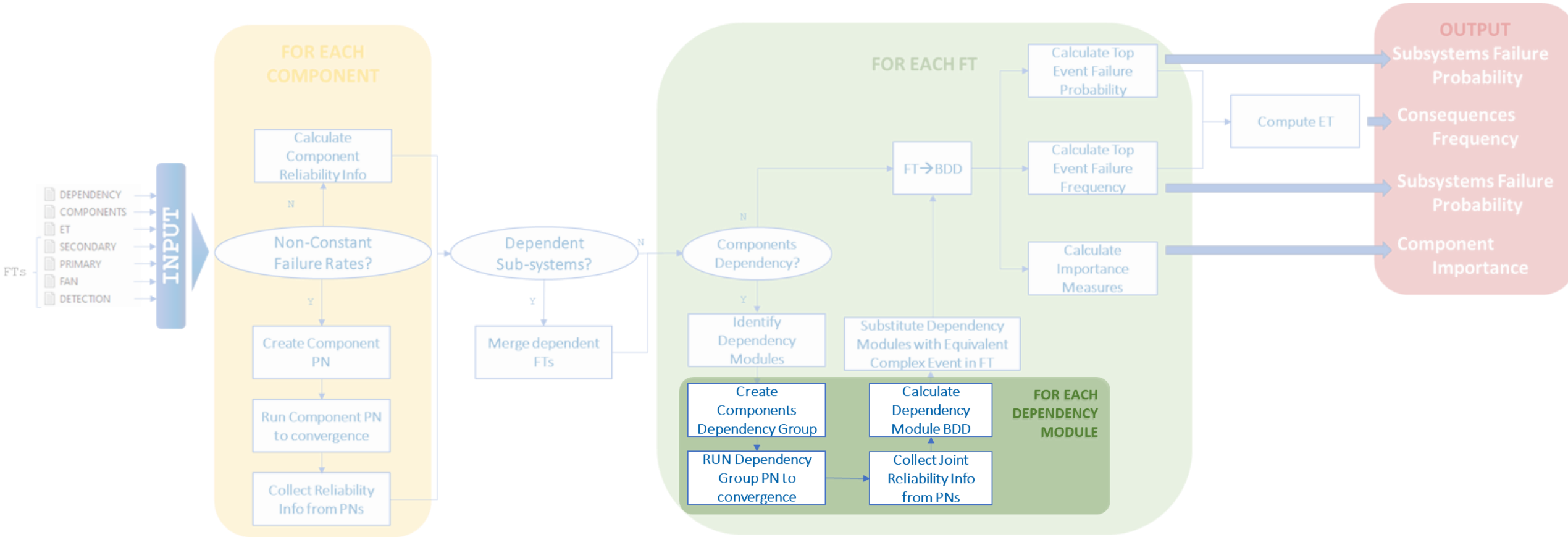
# Step 1: Component Reliability



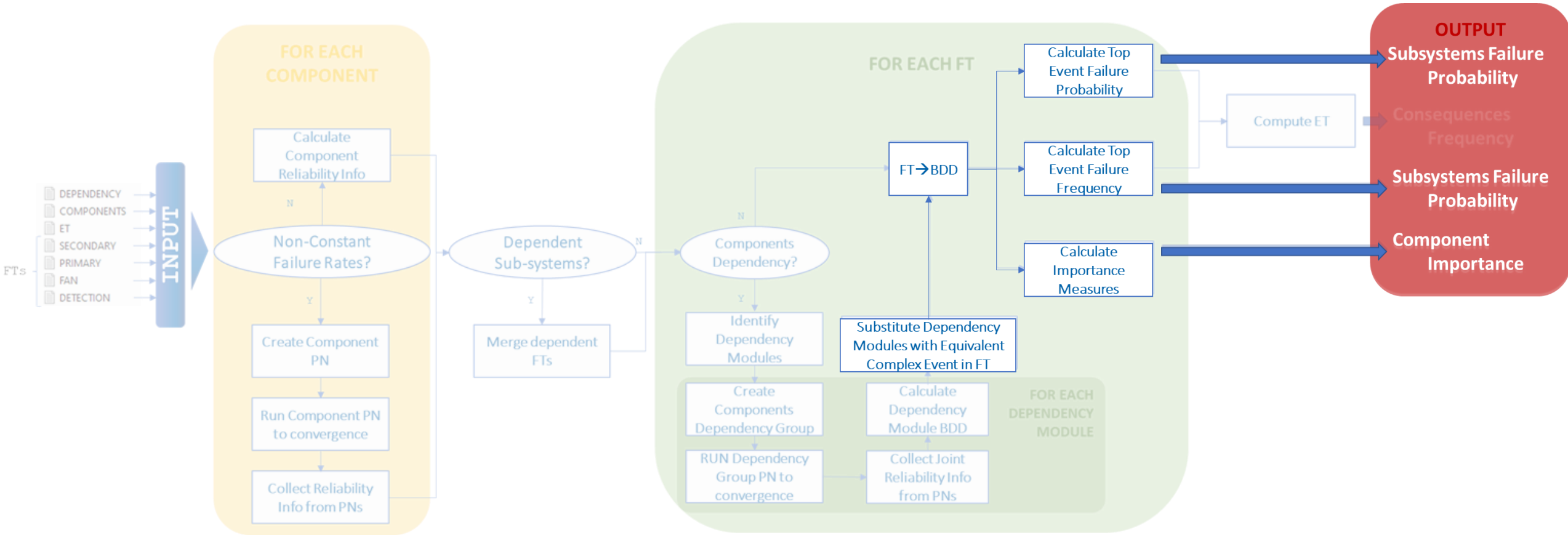
# Step 2: Independent FTs Definition



# Step 3: Dependency Groups Computation



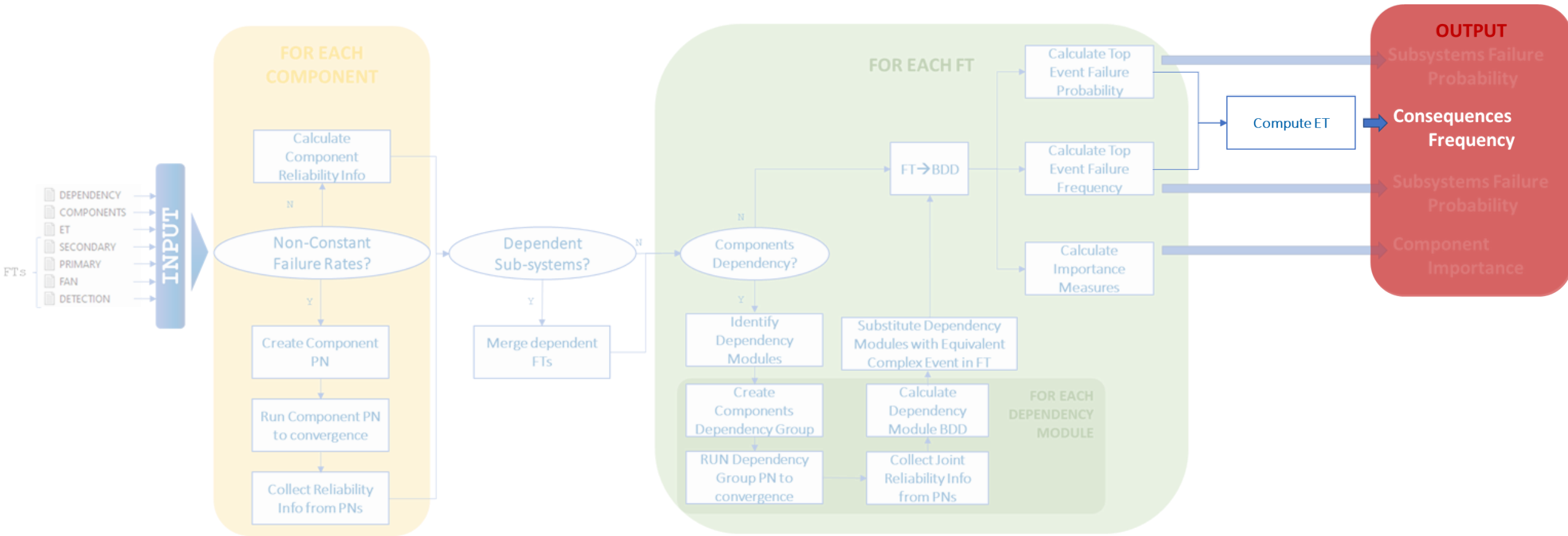
# Step 4: FTs Computation







# Step 5: ET Computation





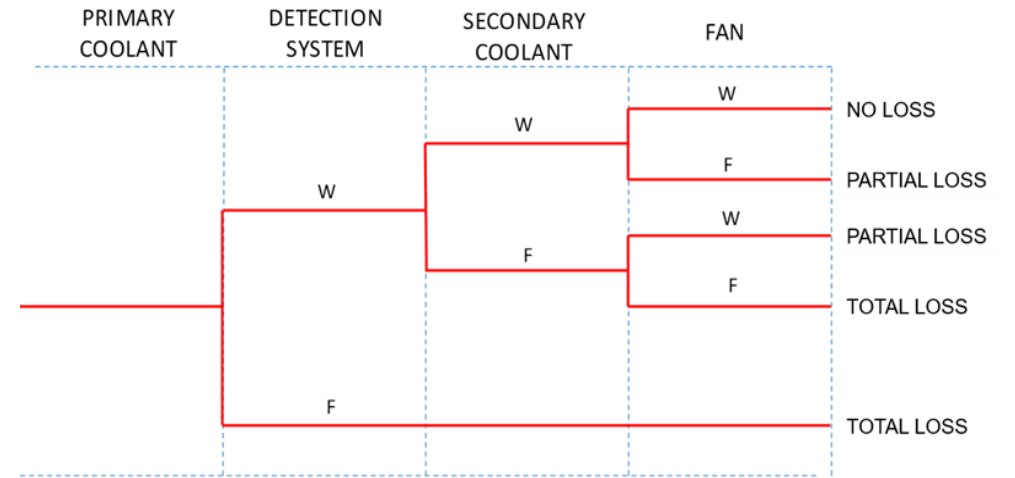
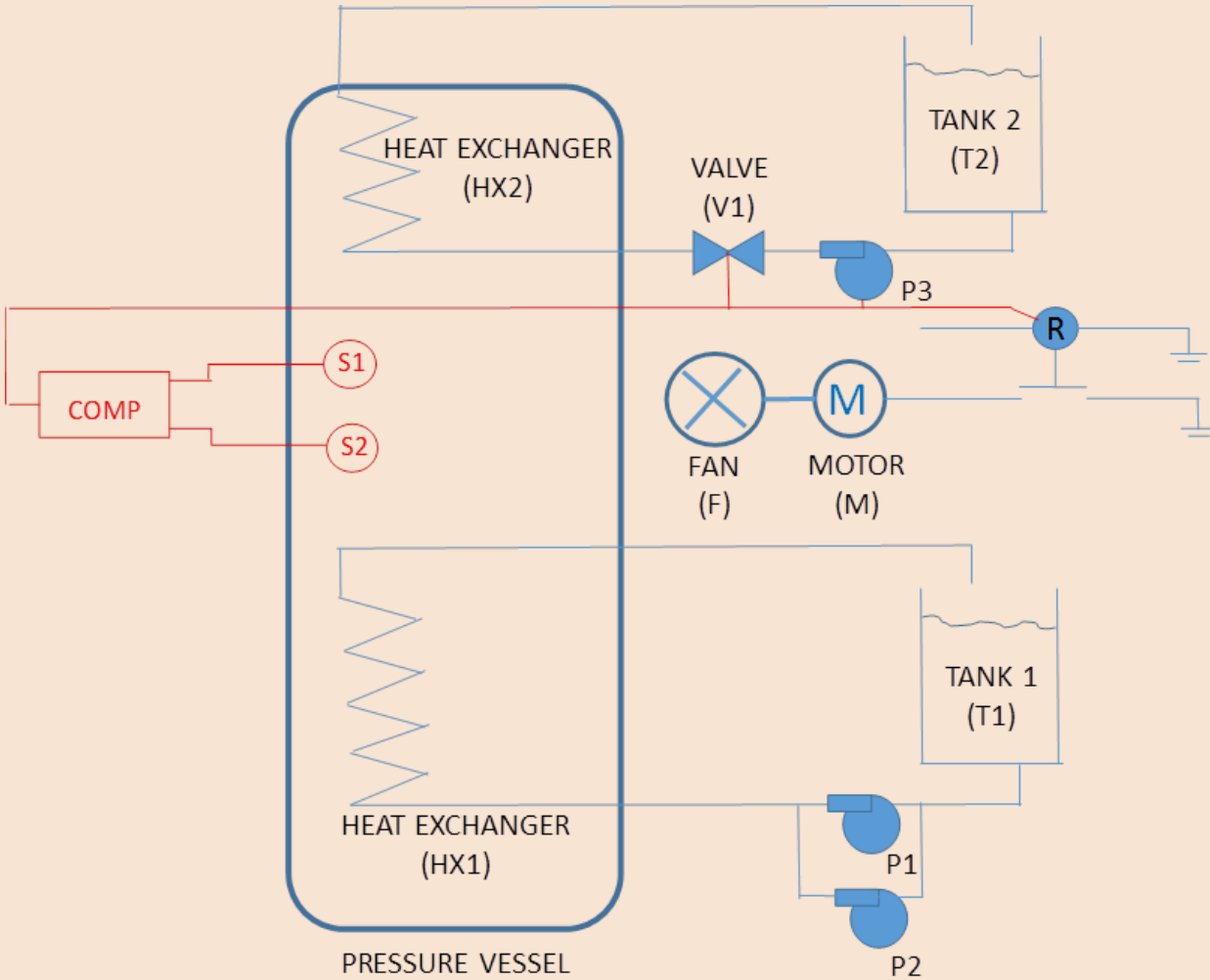
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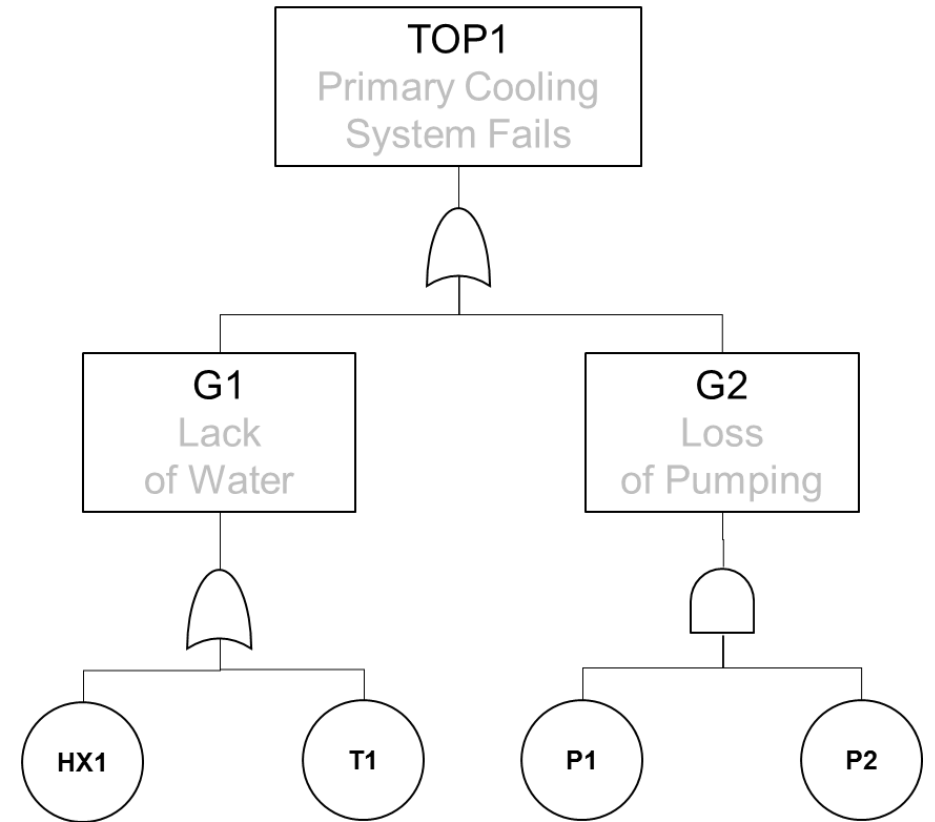
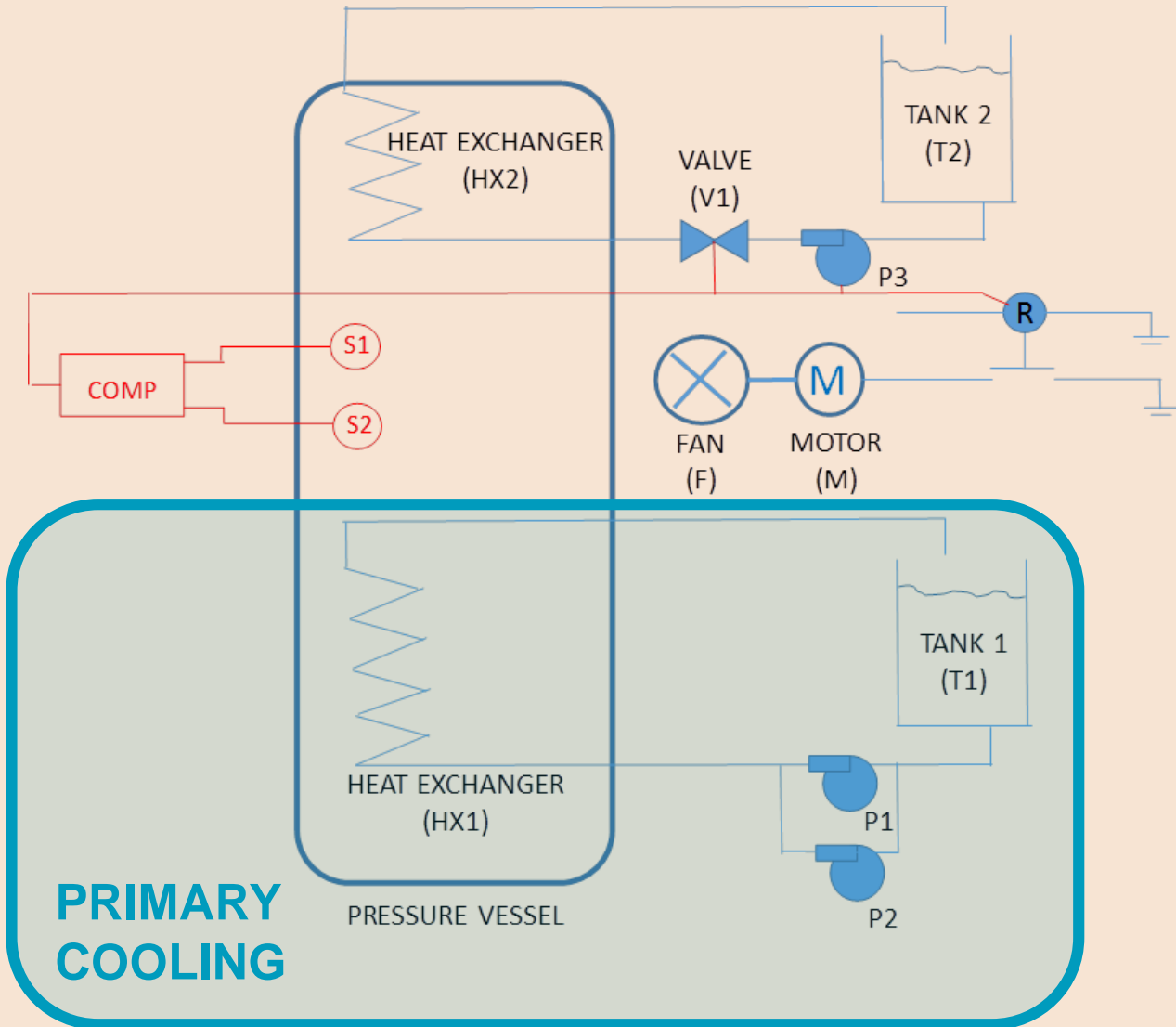
# Hands On

Toy Model and Case Studies

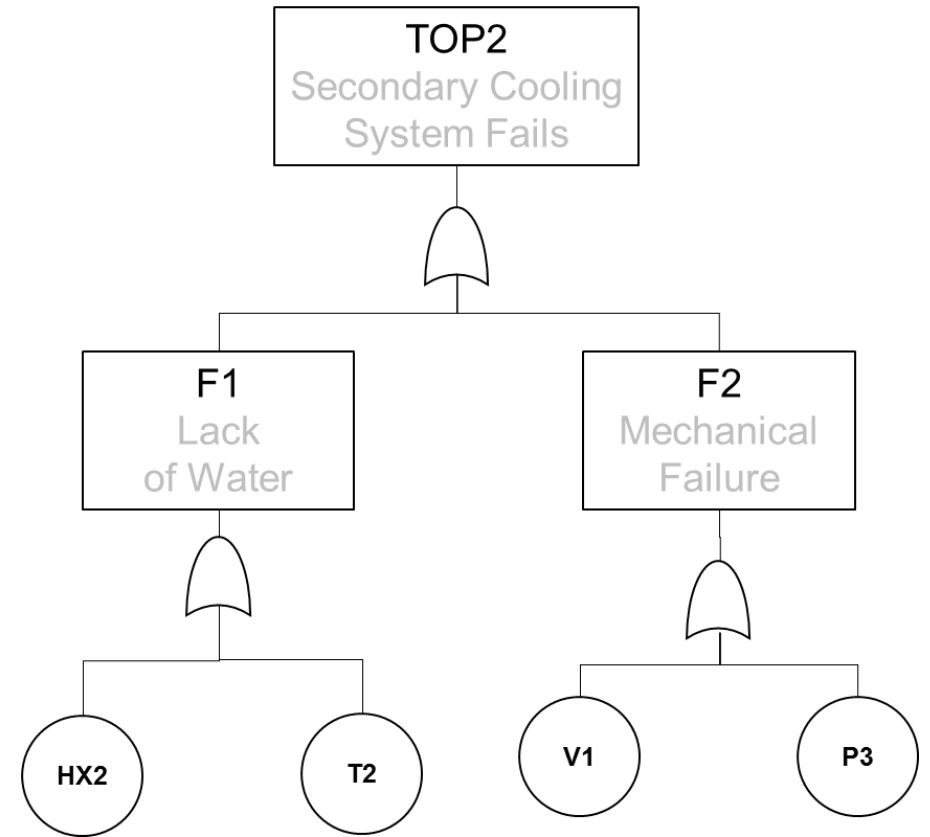
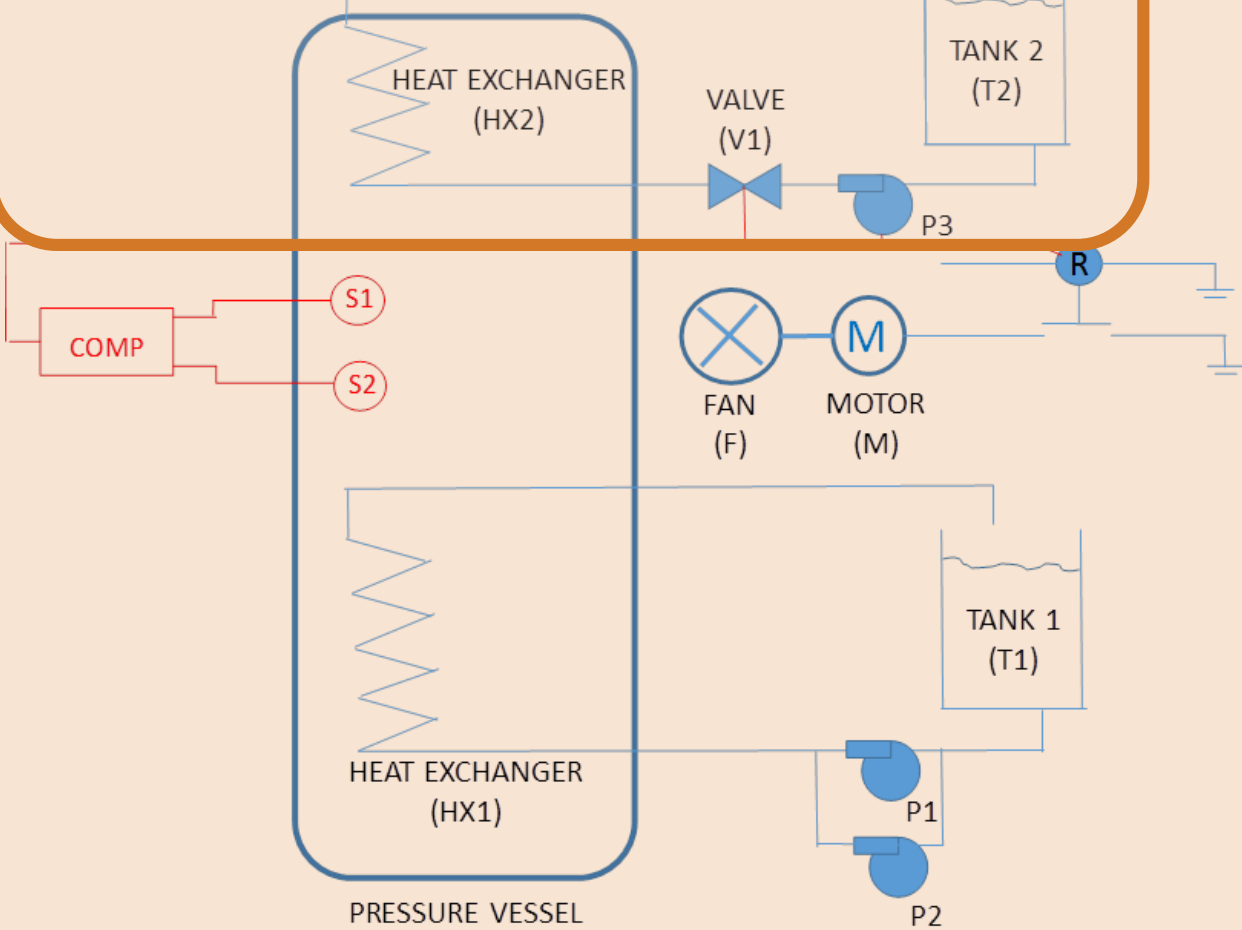
# System Overview



# System Overview

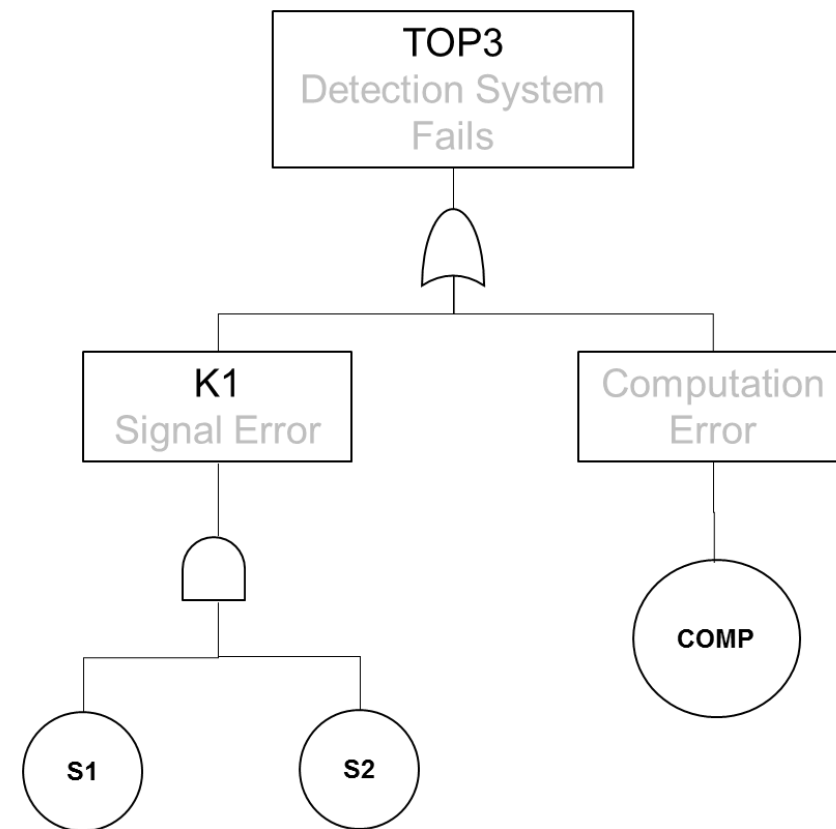
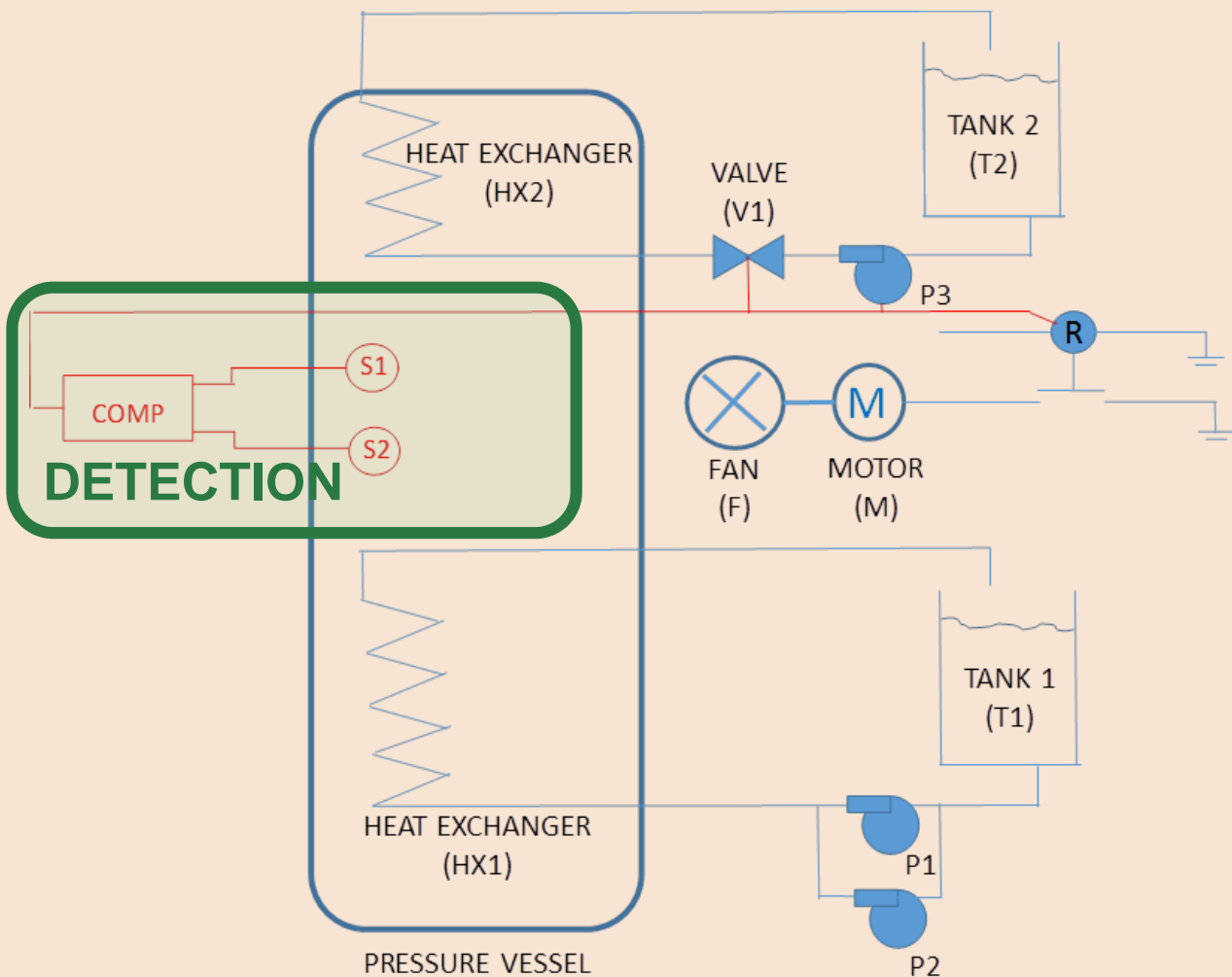


## SECONDARY COOLING

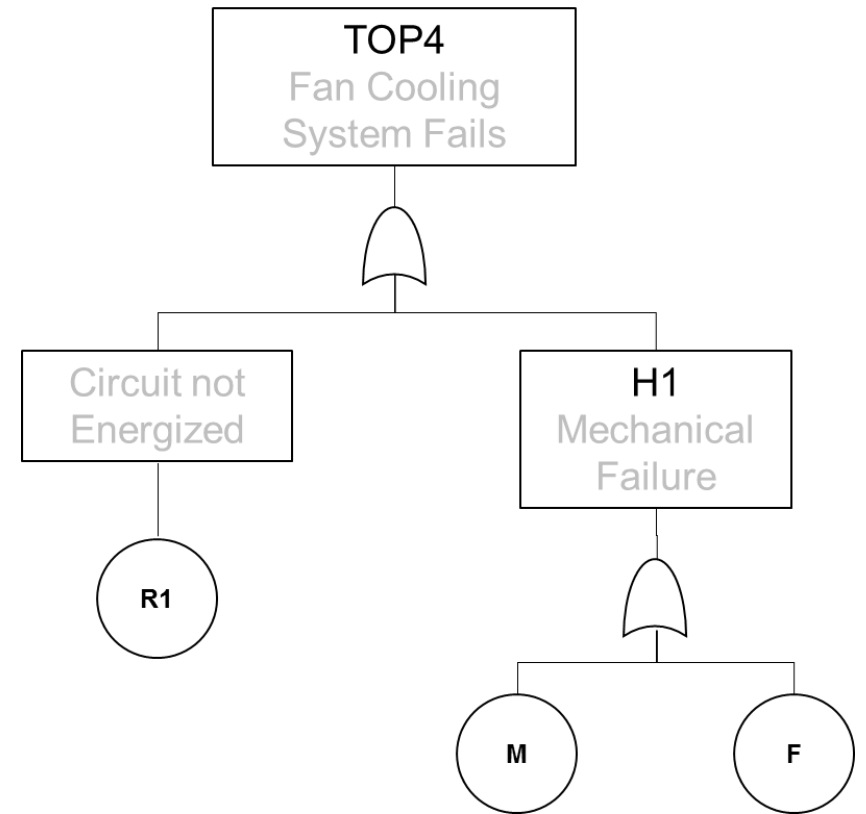
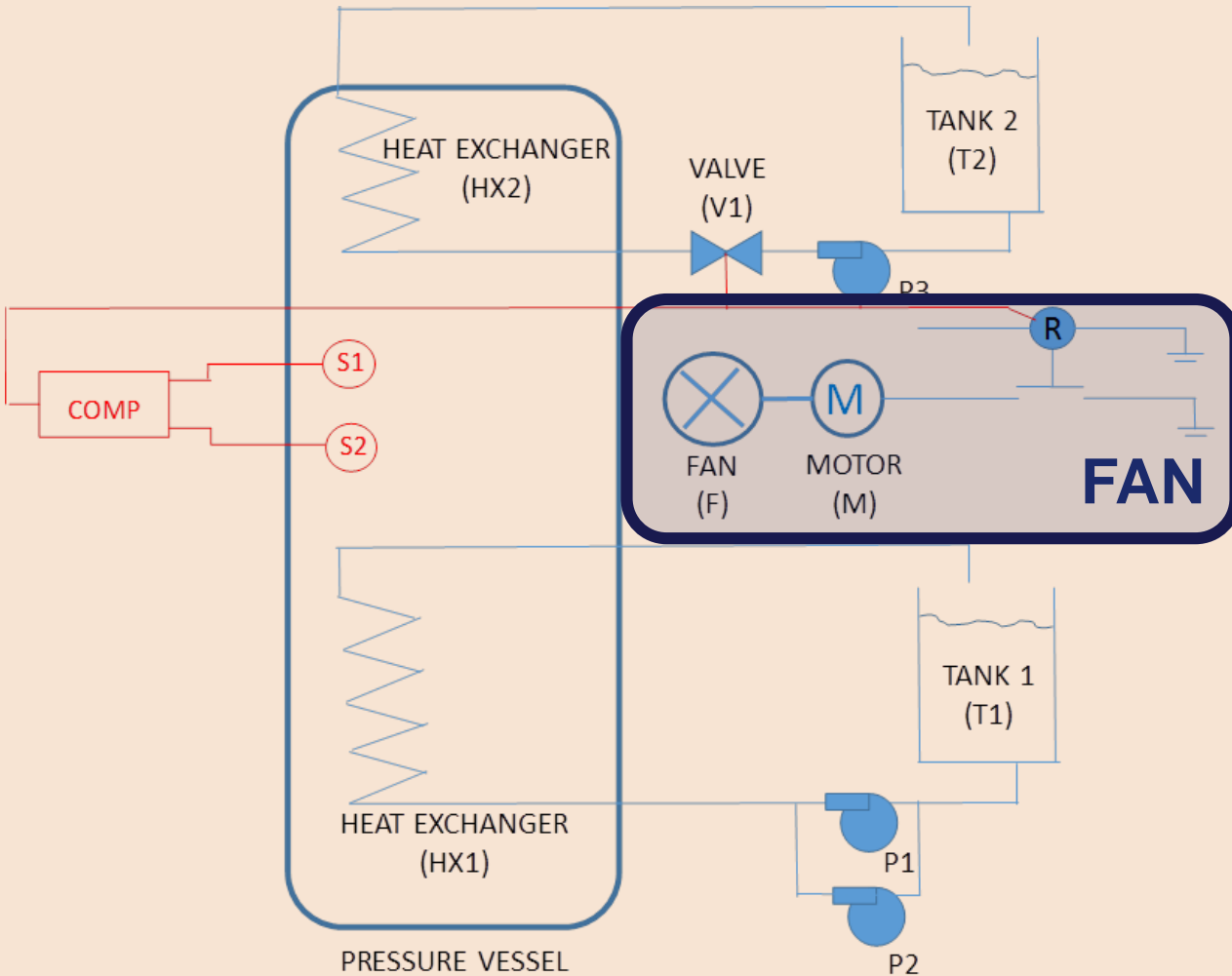




# System Overview



# System Overview





## 4 Case-studies:

a) Non-constant failure rates  
(full independence)

b) Hard dependency  
(component shared between subsystems)

c) Soft dependency  
(stochastic, between components due to secondary processes)

d) Complex dependency  
(soft+hard dependencies)





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# Case Study A

Non-Constant Failure/Repair Rates



# Non-constant Failure/Repair Rates

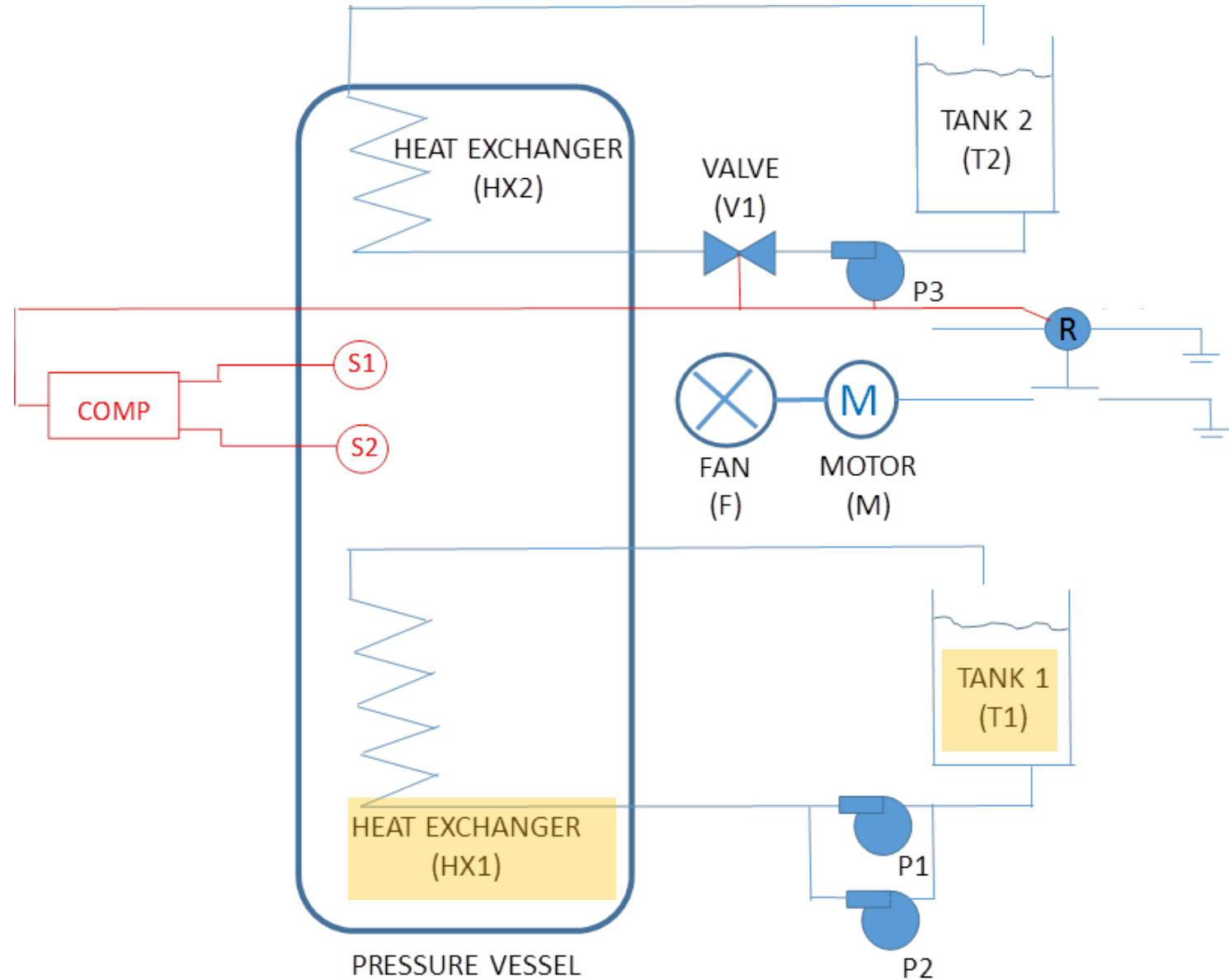
```

COMPONENTS - Notepad
File Edit Format View Help
HX1
FAIL
weibull,3,6.6227e+03
REPAIR
0.0417

T1
FAIL
weibull,2,4.1792e+05
REPAIR
lognormal,8,4.125

P1
FAIL
8.0e-4
REPAIR
0.1250

P2
FAIL
8.0e-4
REPAIR
0.1250
    
```



# Step 1: Component Reliability

```

COMPONENTS - Notepad
File Edit Format View Help
HX1
FAIL
weibull,3,6.6227e+03
REPAIR
0.0417

T1
FAIL
weibull,2,4.1792e+05
REPAIR
lognormal,8,4.125

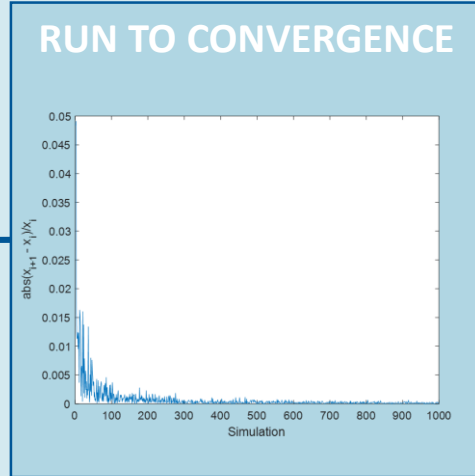
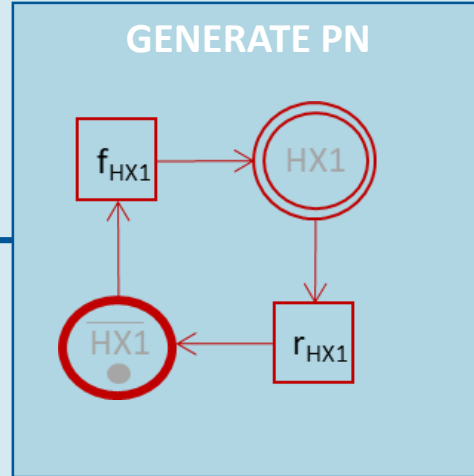
P1
FAIL
8.0e-4
REPAIR
0.1250
    
```

Exponentially Distributed?

N

Y

## NON-CONSTANT FAILURE/REPAIR RATES



STORE OUTPUT

HX1	
Unavailability	3.92e <sup>-3</sup>
Failure Frequency [h <sup>-1</sup> ]	1.63e <sup>-4</sup>

## CONSTANT FAILURE/REPAIR RATES

- IDENTIFY MODEL
- Non-Repairable
  - Corrective Maintenance
  - Scheduled Maintenance

COMPUTE RELIABILITY

$$q(P1) = \frac{\lambda}{\lambda + \nu}$$

$$f(P1) = \lambda * (1 - q(P1))$$

[ λ = failure rate, ν = repair rate]

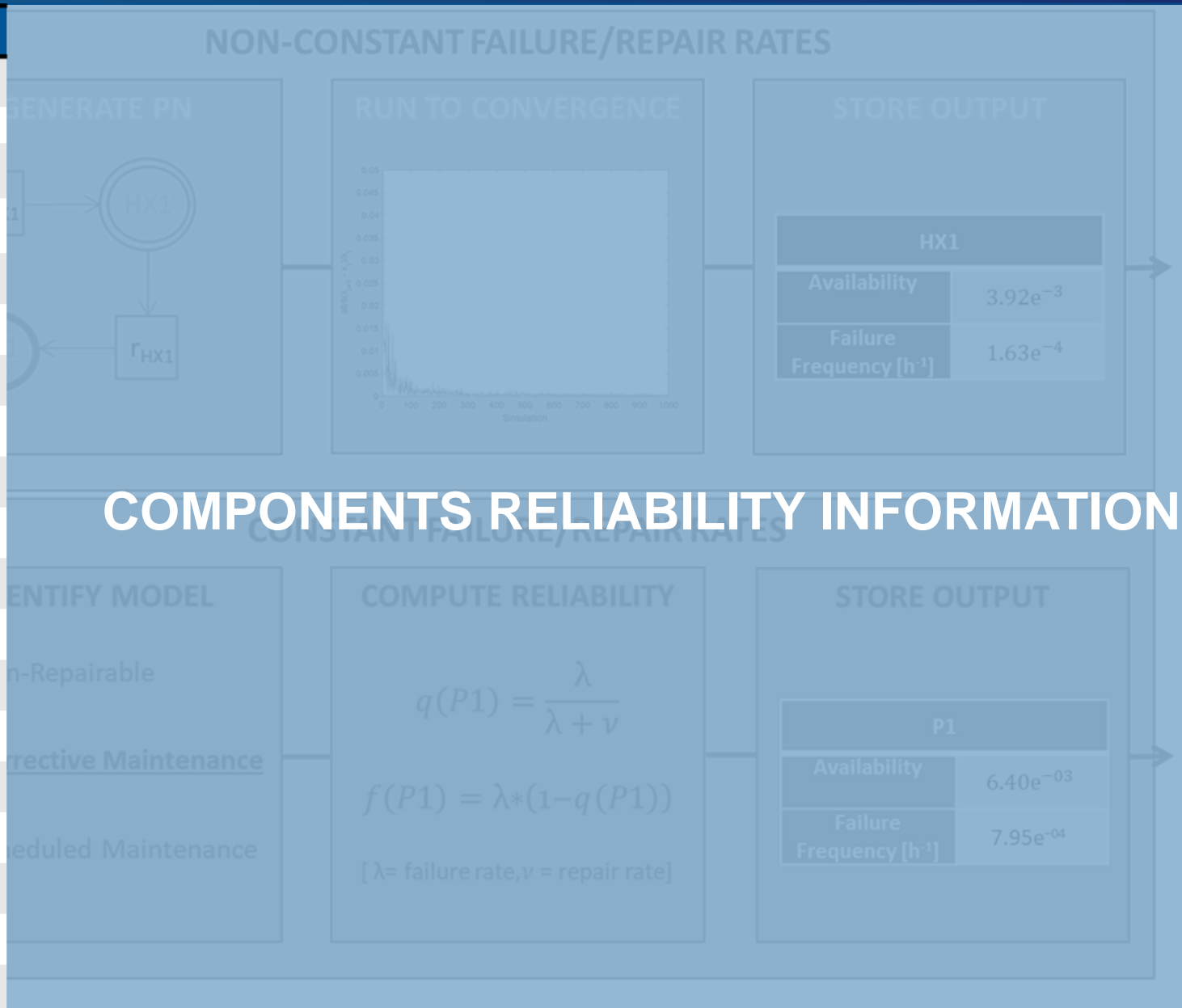
STORE OUTPUT

P1	
Unavailability	6.40e <sup>-03</sup>
Failure Frequency [h <sup>-1</sup> ]	7.95e <sup>-04</sup>



# Step 1: Component Reliability

COMPONENT	UNAVAILABILITY	FAILURE FREQUENCY [h <sup>-1</sup> ]
P1	6.40e <sup>-03</sup>	7.95e <sup>-04</sup>
P2	6.40e <sup>-03</sup>	7.95e <sup>-04</sup>
HX1	3.92e <sup>-03</sup>	1.63e <sup>-04</sup>
T1	5.29e <sup>-03</sup>	4.87e <sup>-07</sup>
HX2	2.38e <sup>-05</sup>	1.70e <sup>-06</sup>
T2	2.16e <sup>-07</sup>	2.70e <sup>-08</sup>
V1	1.35e <sup>-06</sup>	2.70e <sup>-07</sup>
P3	6.40 e <sup>-03</sup>	7.95e <sup>-04</sup>
TC	2.13e <sup>-06</sup>	7.10e <sup>-07</sup>
PGA	9.4e <sup>-03</sup>	3.1e <sup>-03</sup>
ADC	6.90e <sup>-05</sup>	2.30e <sup>-05</sup>
DF	3.50e <sup>-03</sup>	1.2e <sup>-03</sup>
RTD	6.80e <sup>-06</sup>	1.70e <sup>-06</sup>
FT	3.60e <sup>-06</sup>	1.20e <sup>-06</sup>
CMP	4.80e <sup>-06</sup>	1.20e <sup>-06</sup>
PLC	3.67e <sup>-05</sup>	3.06e <sup>-06</sup>
R1	1.02e <sup>-06</sup>	3.40e <sup>-07</sup>
M	1.2e <sup>-03</sup>	7.99e <sup>-06</sup>
F	1.42e <sup>-04</sup>	3.50e <sup>-06</sup>



## COMPONENTS RELIABILITY INFORMATION

# Step 2: Independent FTs Definition

## INPUT FTs

## INDEPENDENT ?

## MERGE DEPENDENT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

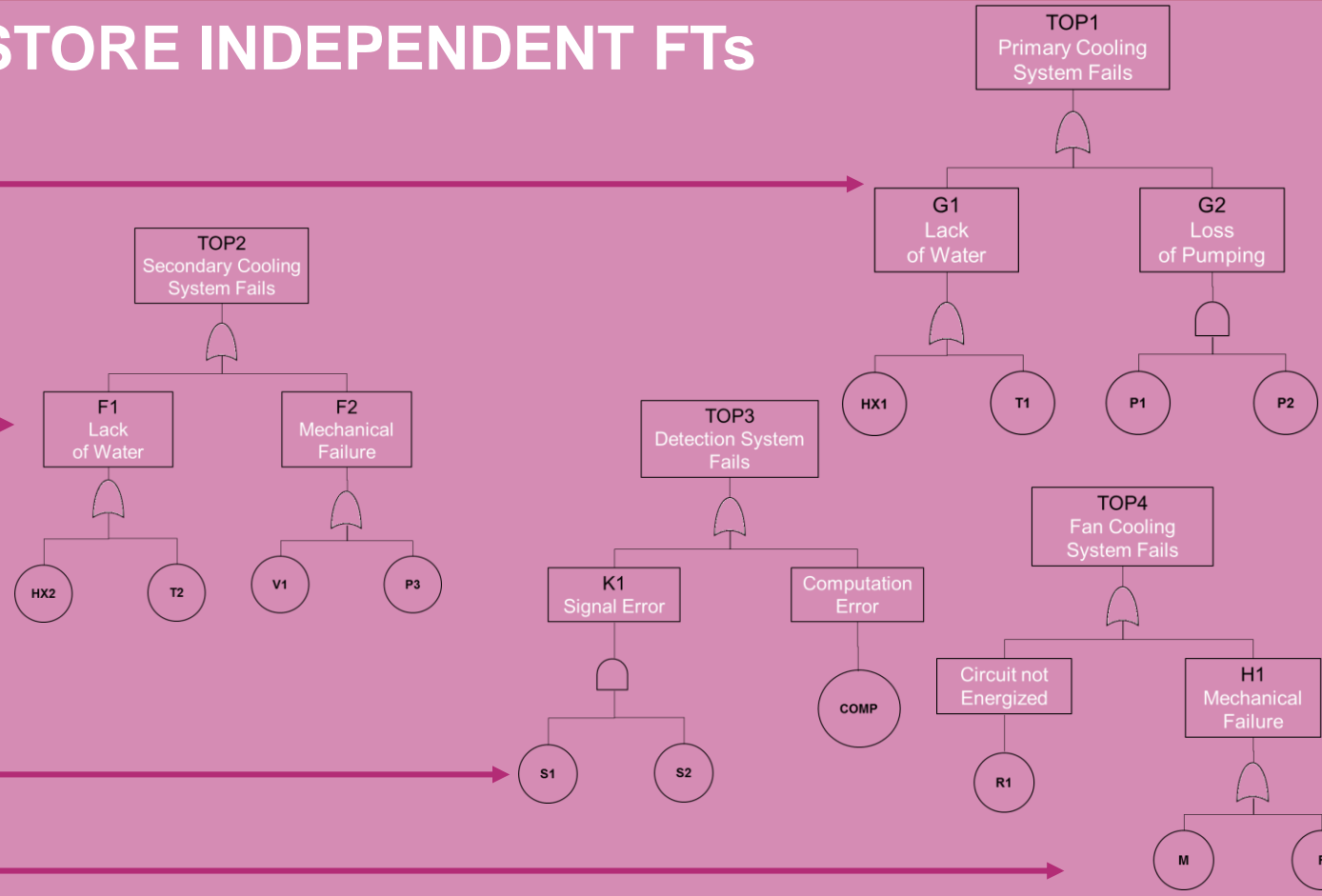
DEPENDENCIES - Notepad  
File Edit Format View Help

SECONDARY - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P3  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

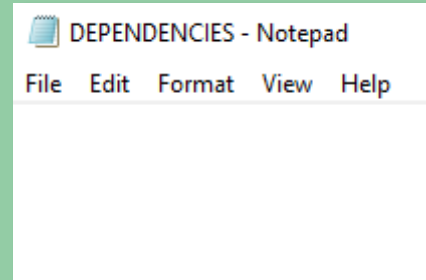
## STORE INDEPENDENT FTs





## Step 3: Dependency Groups Computation

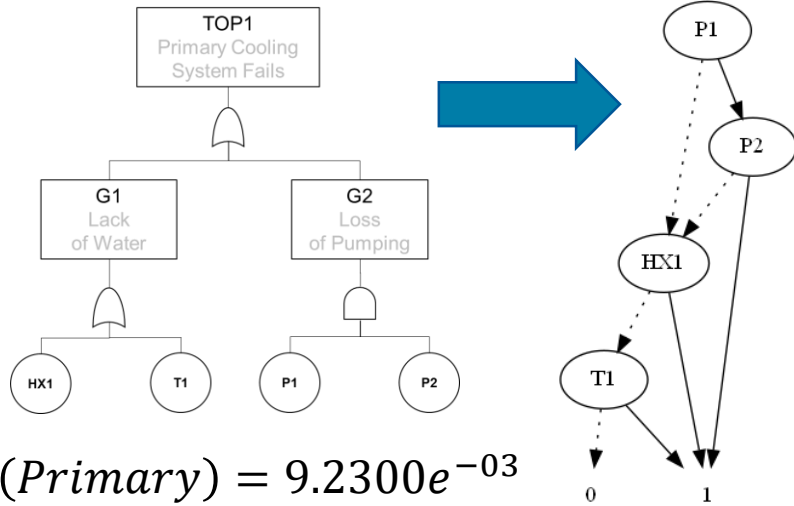
INDEPENDENT



Since Case A assumes full independence, there are no dependency groups

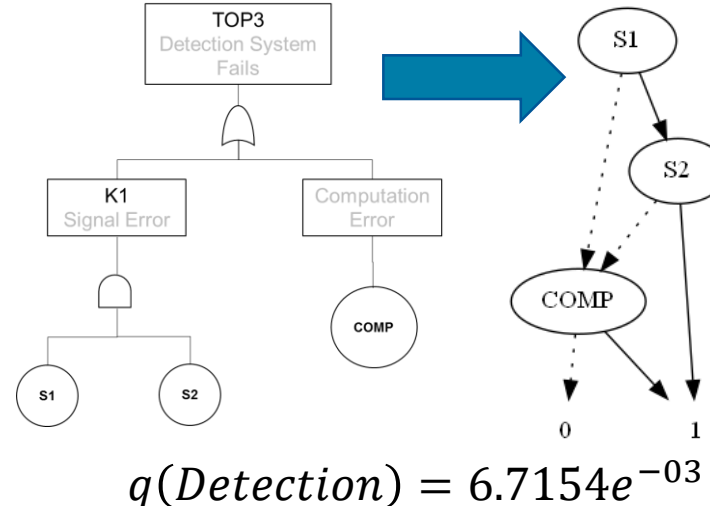
→ SKIP!

# Step 4: FTs Computation

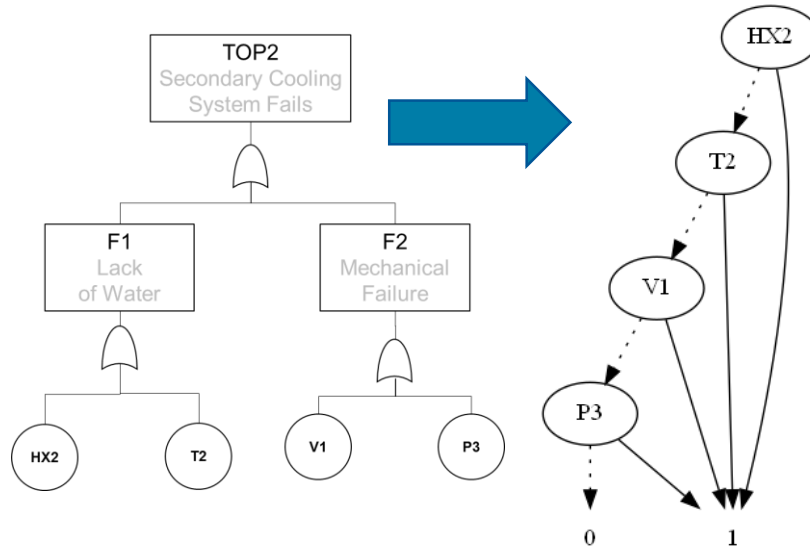


$$q(\text{Primary}) = 9.2300e^{-03}$$

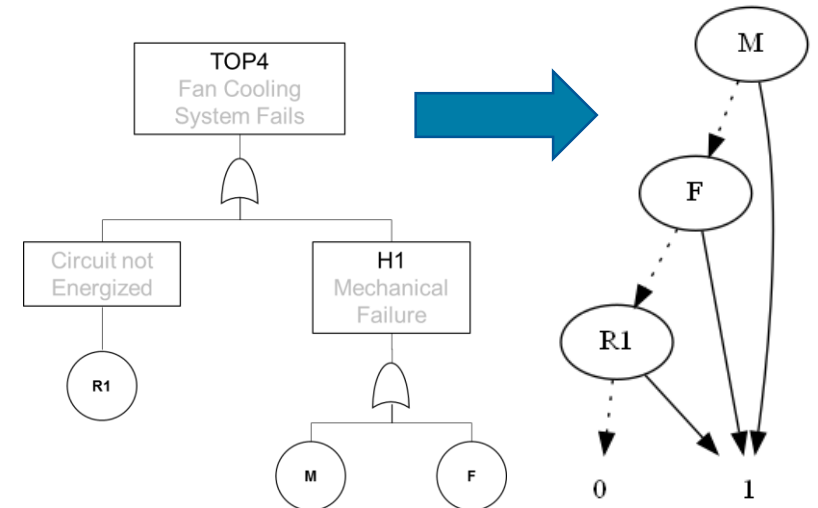
$$f(\text{Primary}) = 1.2257e^{-05} h^{-1}$$



$$q(\text{Detection}) = 6.7154e^{-03}$$



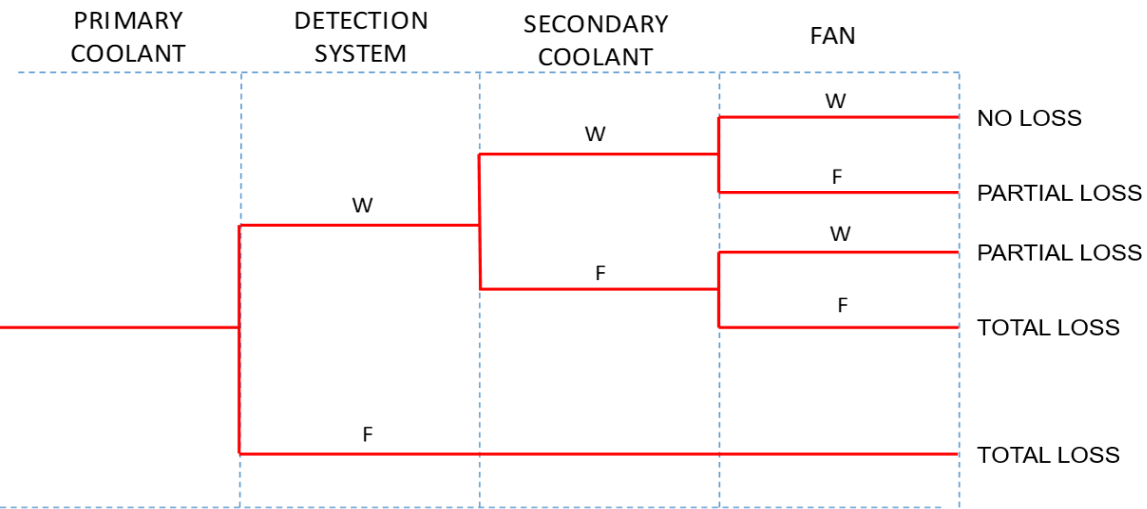
$$q(\text{Secondary}) = 5.4615e^{-03}$$



$$q(\text{Fan}) = 1.2747e^{-02}$$



# Step 5: ET Computation



## CONSEQUENCE FREQUENCIES

$$F_{NoLoss} = 1.1954e^{-05} h^{-1}$$

$$F_{PartialLoss} = f_{PartialLoss1} + f_{PartialLoss2} = 2.1999e^{-07} h^{-1}$$

$$F_{TotalLoss} = f_{TotalLoss1} + f_{TotalLoss2} = 8.3158 e^{-08} h^{-1}$$





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# Case Study B

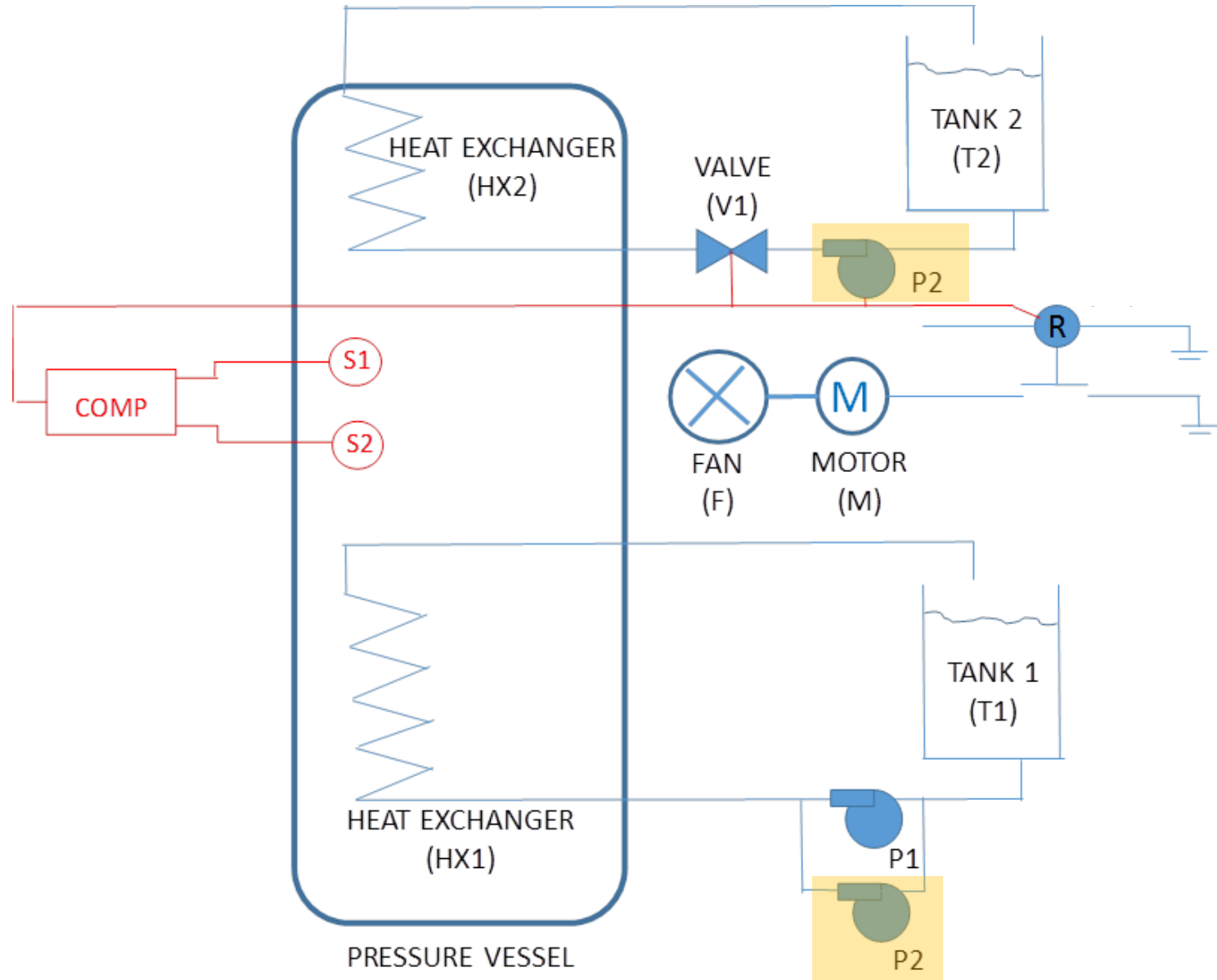
Hard Dependency

# Case Study C: Hard Dependency

```
DEPENDENCY -...  
File Edit Format View Help  
COMMON COMPONENTS  
P2: PRIMARY, SECONDARY
```

```
PRIMARY_FT - ...  
File Edit Format View Help  
PRIMARY, 1, G1, G2  
G2, 0, P1, P2  
G1, 1, HX1, T1
```

```
SECONDARY_F...  
File Edit Format View Help  
SECONDARY, 1, F2, F1  
F2, 1, V1, P2  
F1, 1, HX2, T2
```



# Step 1: Component Reliability

COMPONENTS ...

File Edit Format View Help

HX1  
FAIL  
1.7e-6  
REPAIR  
0.0417

T1  
FAIL  
2.7e-8  
REPAIR  
0.1250

P1  
FAIL  
8.0e-4  
REPAIR  
0.1250

P2  
FAIL  
8.0e-4  
REPAIR  
0.1250

HX2  
FAIL  
1.7e-6  
REPAIR  
0.0714  
INSPECTION  
4380

Exponentially Distributed?

### NON-CONSTANT FAILURE/REPAIR RATES

#### GENERATE PN

#### RUN TO CONVERGENCE

#### STORE OUTPUT

HX1	
Unavailability	3.92e <sup>-3</sup>
Failure Frequency [h <sup>-1</sup> ]	1.63e <sup>-4</sup>

### CONSTANT FAILURE/REPAIR RATES

#### IDENTIFY MODEL

- Non-Repairable
- Corrective Maintenance
- Scheduled Maintenance

#### COMPUTE RELIABILITY

$$q(P1) = \frac{\lambda}{\lambda + \nu}$$

$$f(P1) = \lambda * (1 - q(P1))$$

[ λ = failure rate, ν = repair rate]

#### STORE OUTPUT

P1	
Unavailability	6.40e <sup>-03</sup>
Failure Frequency [h <sup>-1</sup> ]	7.95e <sup>-04</sup>

# Step 2: Independent FTs Definition

## INPUT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

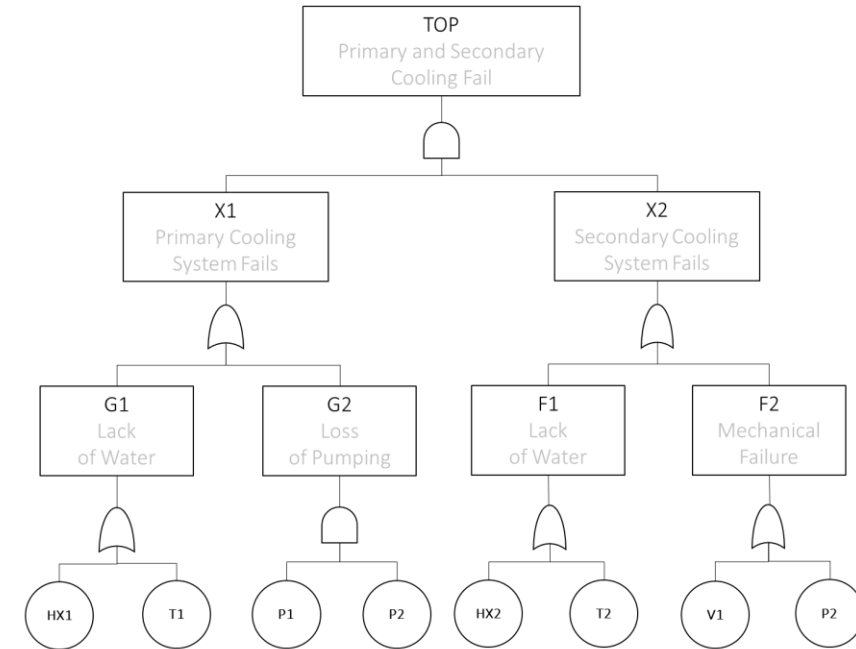
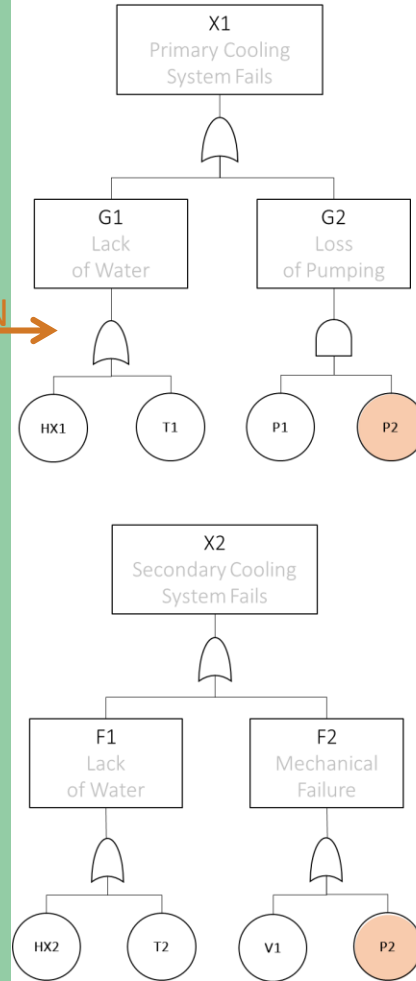
SECONDARY\_FT - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P2  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

## INDEPENDENT ?

DEPENDENCY - ...  
File Edit Format View Help  
COMMON COMPONENTS  
P2:PRIMARY,SECONDARY



# Step 2: Independent FTs Definition

## INPUT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

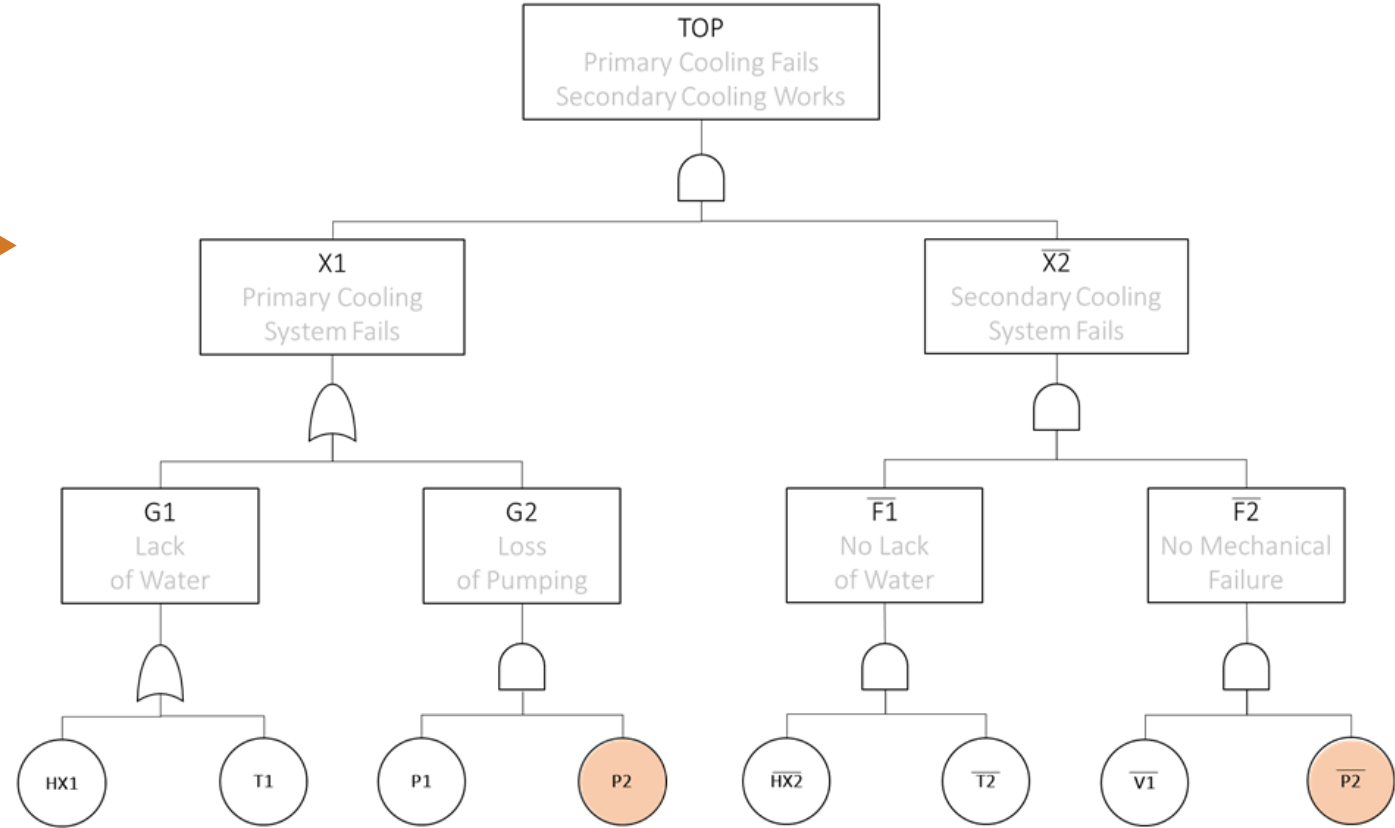
SECONDARY\_FT - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P2  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

## INDEPENDENT ?

DEPENDENCY -...  
File Edit Format View Help  
COMMON COMPONENTS  
P2:PRIMARY,SECONDARY



# Step 2: Independent FTs Definition

## INPUT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

SECONDARY\_FT - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P2  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

## INDEPENDENT ?

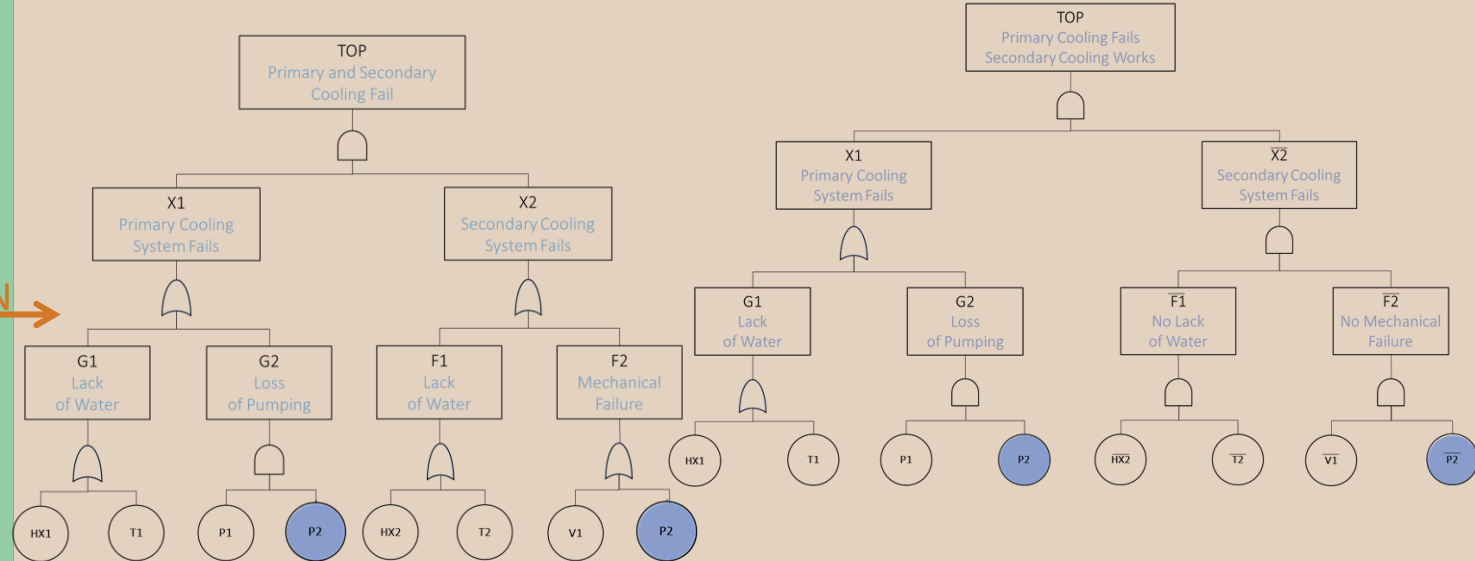
DEPENDENCY - ...  
File Edit Format View Help  
COMMON COMPONENTS  
P2:PRIMARY,SECONDARY

?

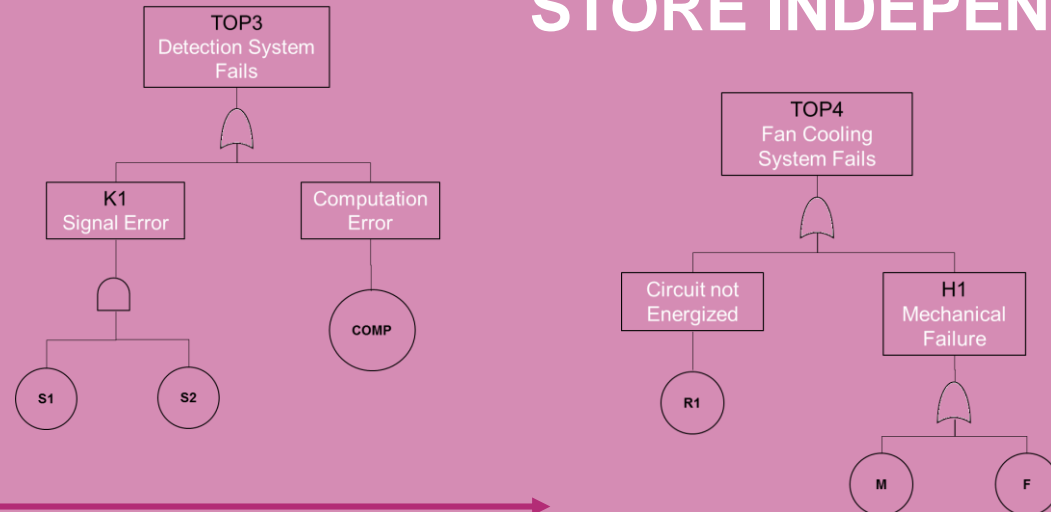
Y

Y

## MERGE DEPENDENT FTs



## STORE INDEPENDENT FTs



# Step 2: Independent FTs Definition

## INPUT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

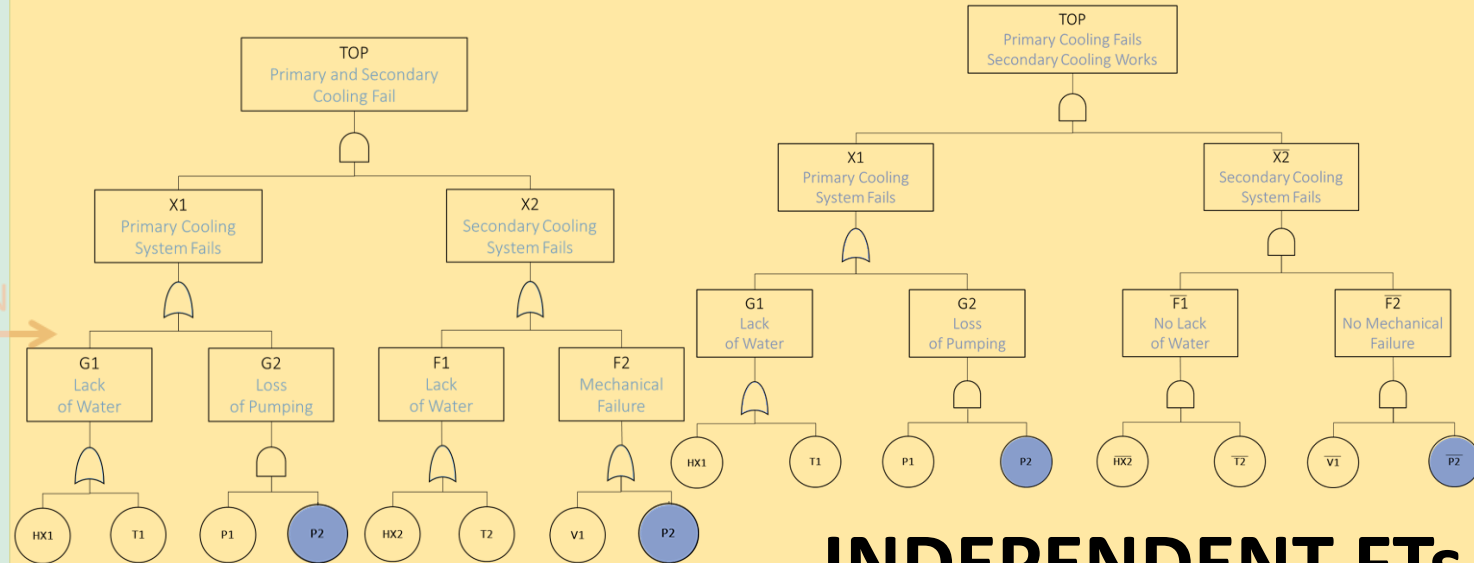
SECONDARY\_FT - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P2  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

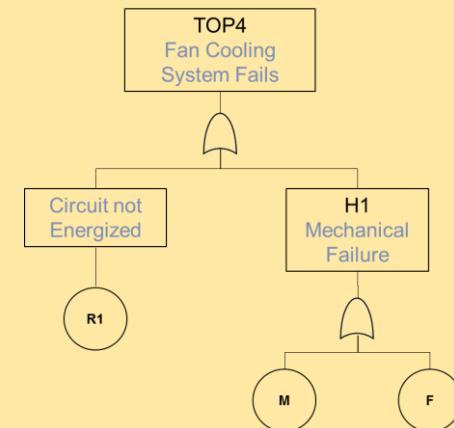
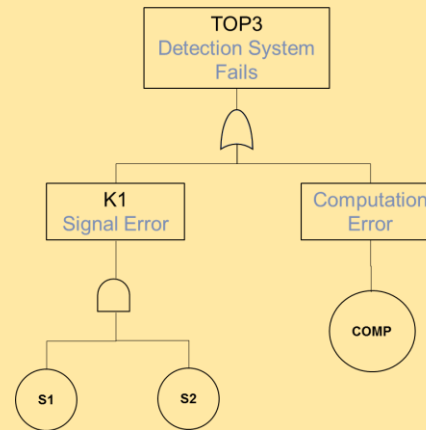
FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

## INDEPENDENT ?

DEPENDENCY - ...  
File Edit Format View Help  
COMMON COMPONENTS  
P2: PRIMARY, SECONDARY



## INDEPENDENT FTs



N

Y

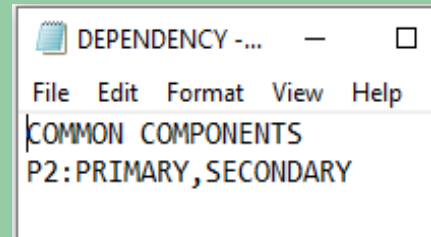
Y



## Step 3: Dependency Groups Computation

INDEPENDENT

!



The only dependency associated with the case study is between FTs

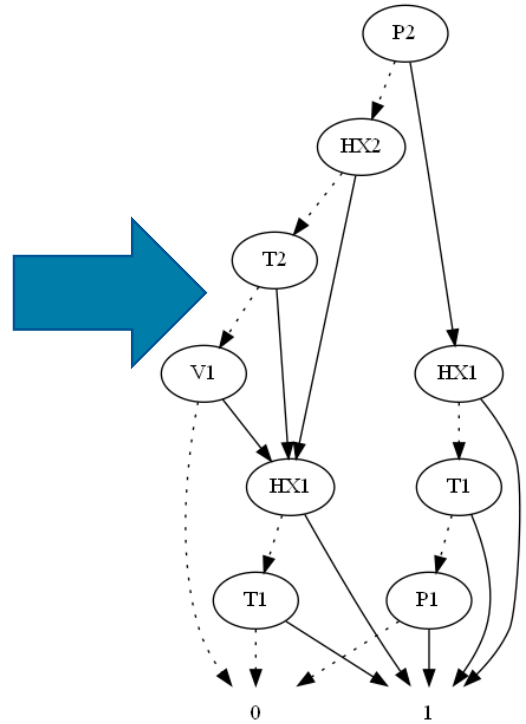
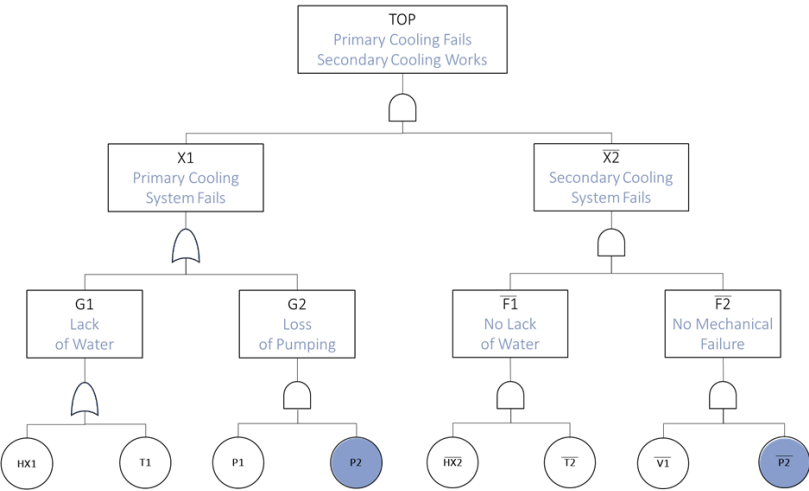
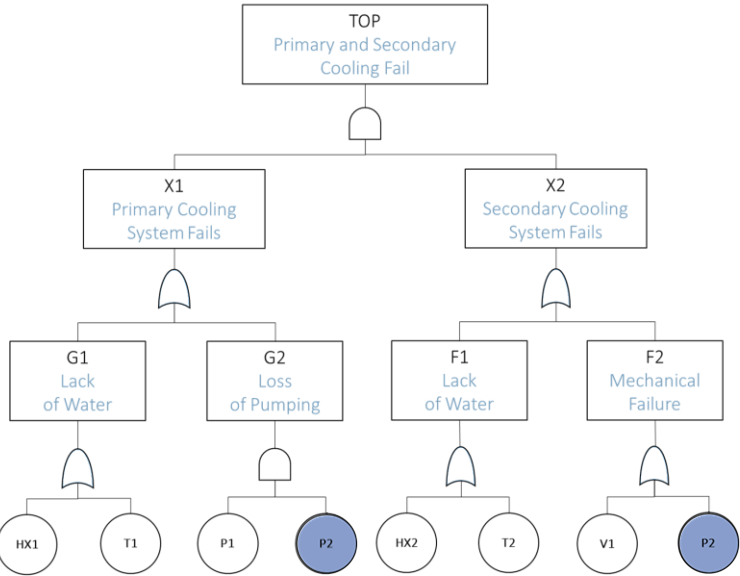


Since Case B assumes full independence among components, there are no dependency groups to be computed

→ SKIP!

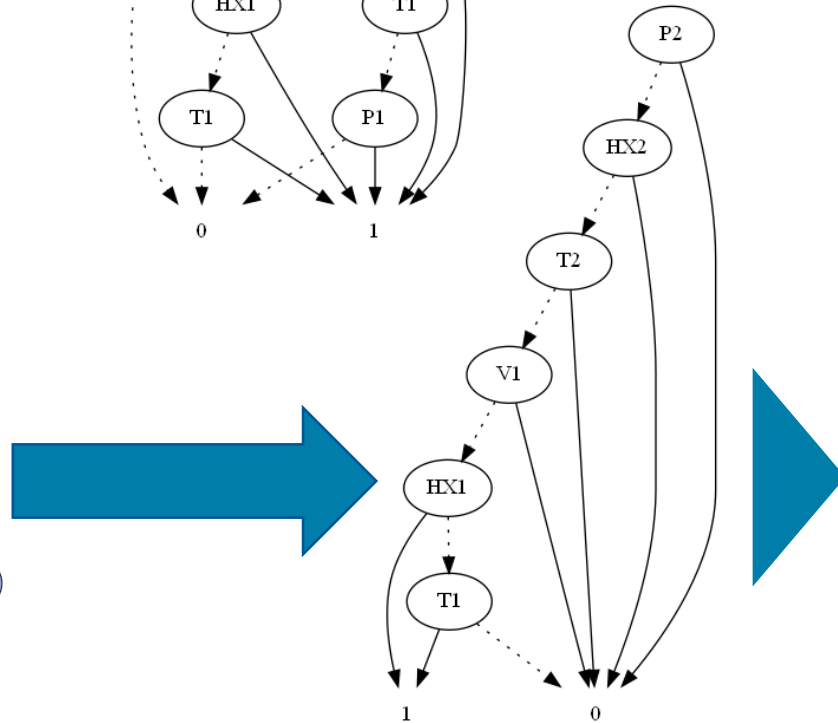


# Step 4: FTs Computation



$$q(\text{Primary, Secondary}) = 4.1399e^{-05}$$

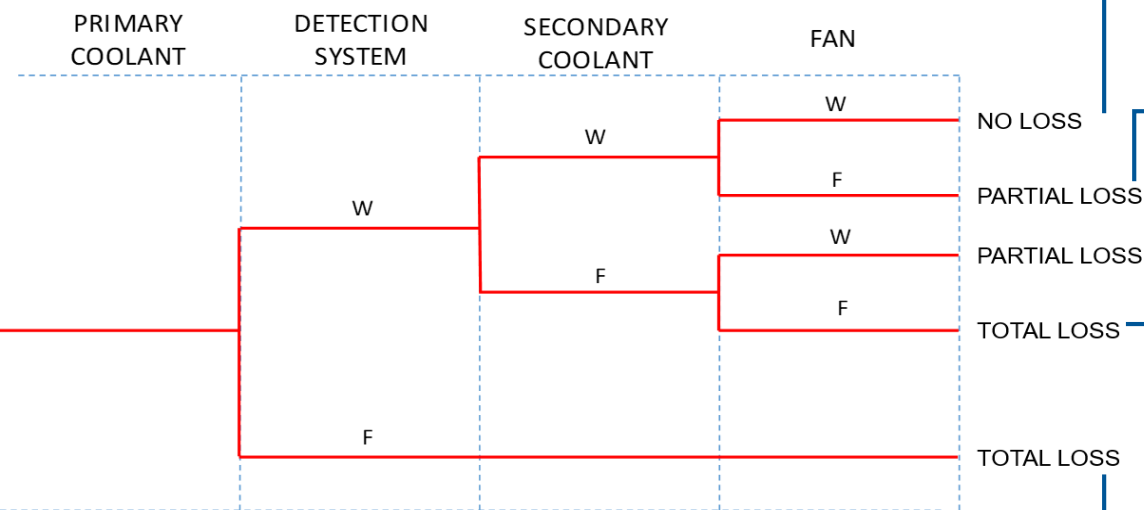
$$[f(\text{Primary}) = 1.2257e^{-05} h^{-1}]$$



$$q(\text{Primary, } \overline{\text{Secondary}}) = 8.1942e^{-05}$$



# Step 5: ET Computation



$$f_{NoLoss} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(\overline{Fan})$$

$$f_{PartialLoss1} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(Fan)$$

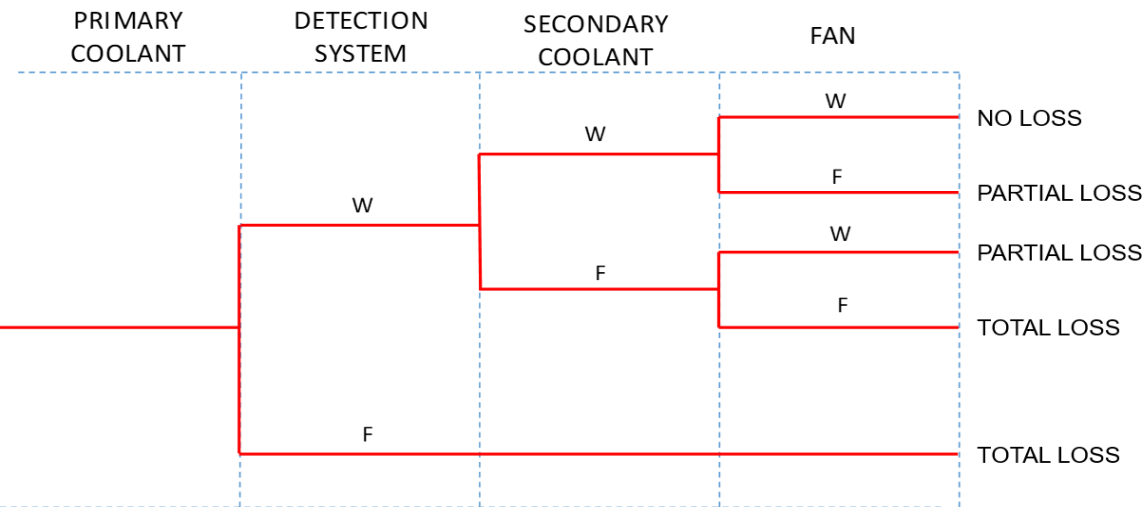
$$f_{PartialLoss2} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(\overline{Fan})$$

$$f_{TotalLoss1} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(Fan)$$

$$f_{TotalLoss2} = f_{primary} \cdot Q(Detection)$$



# Step 5: ET Computation



## TRIGGER RELIABILITY INFO

→  $Q(\text{Primary})$

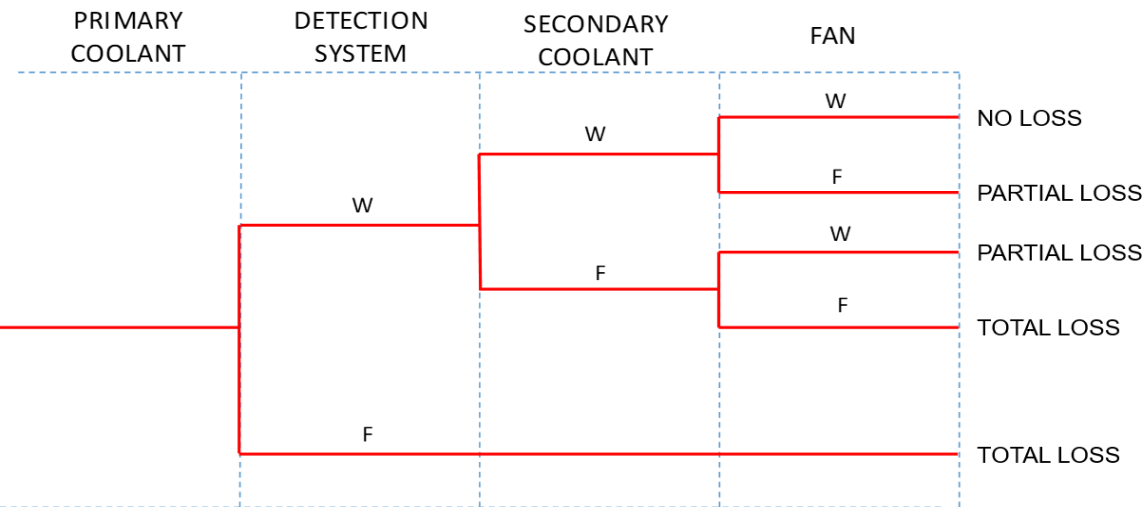
$$= Q(\text{Primary, Secondary}) + Q(\text{Primary, } \overline{\text{Secondary}})$$

$$\rightarrow Q(\text{Secondary}|\text{Primary}) = \frac{Q(\text{Primary, Secondary})}{Q(\text{Primary})}$$

$$\rightarrow Q(\overline{\text{Secondary}}|\text{Primary}) = \frac{Q(\text{Primary, } \overline{\text{Secondary}})}{Q(\text{Primary})}$$



# Step 5: ET Computation



## CONSEQUENCE FREQUENCIES

$$F_{NoLoss} = 1.4415e^{-05} h^{-1}$$

$$F_{PartialLoss} = f_{PartialLoss1} + f_{PartialLoss2} = 7.4687 e^{-06} h^{-1}$$

$$F_{TotalLoss} = f_{TotalLoss1} + f_{TotalLoss2} = 2.4262 e^{-07} h^{-1}$$



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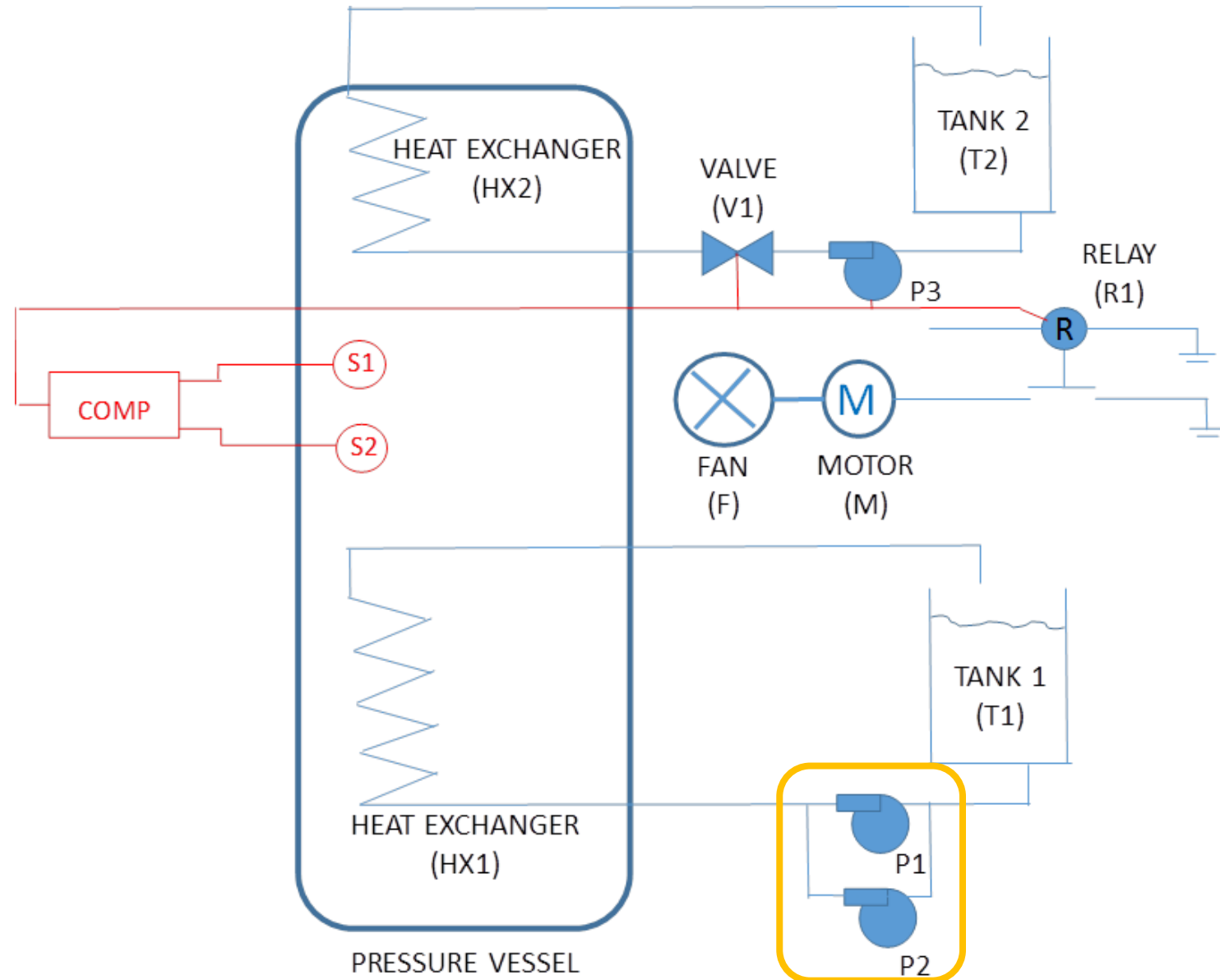
# Case Study D

Soft Dependency

# Case Study D: Soft Dependency

P1 and P2 stochastically dependent

The failure of P1 (P2) causes the increase of P2 (P1) failure probability due to the larger load processed by the working pump



# Case Study D: Soft Dependency

## BUILT-IN GENERATION

```
DEPENDENCIES - Notepad
File Edit Format View Help
LOAD
P1|P2:exponential,14.0e-4
P2|P1:exponential,14.0e-4
```

```
COMPONENTS ...
File Edit Format View Help
HX1
FAIL
1.7e-6
REPAIR
0.0417

T1
FAIL
2.7e-8
REPAIR
0.1250

P1
FAIL
8.0e-4
REPAIR
0.1250

P2
FAIL
8.0e-4
REPAIR
0.1250
```

## IMPORTED MM

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP

P2
DEP

HX2
FAIL
1.7e-6
REPAIR
```

```
DEPENDENCY - Notepad
File Edit Format View Help
MMS
P1P2_MM
```

```
P1P2_MM - Notepad
File Edit Format View Help
STATES
P1_W,P2_W
P1,P2_W
P1_W,P2
P1,P2

TRANSITION MATRIX
-1,0.5,0.5,0
12,-13,0,1
12,0,-13,1
6,0,0,-6
```

## IMPORTED PN

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP

P2
DEP

HX2
FAIL
1.7e-6
REPAIR
```

```
DEPENDENCY - Notepad
File Edit Format View
PNS
P1P2_PN
```

```
P1P2_PN - Notepad
File Edit Format View Help
PLACES
P1requested,1
P1
P1_W
P2_W
P2

TRANSITIONS
P1requested->P1_W,P1:P1start,probability,0.981,0.019
P1_W->P1:P1fails,exponential,8.0e-4
P1->P1_W:P1repair,exponential,0.1250
P1->P1,P2_W,P2:P2start,probability,0.981,0.019
P2->P2_W:P2repair,exponential,0.1250
P2_W->P2:P2fails,exponential,8.0e-4
P1_W,P2_W->P1_W:P2toSleep,instant,0

INHIBITORS
P2->P2start
```

## IMPORTED DATA

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP

P2
DEP

HX2
FAIL
1.7e-6
REPAIR
```

```
DEPENDENCY - Notepad
File Edit Format View Help
DATA
DG1_DATA
```

```
DG1_DATA - Notepad
File Edit Format View Help
PROBABILITY
P1_W,P2_W:9.8749e-01
P1,P2_W:6.1863e-03
P1_W,P2:6.1863e-03
P1,P2:1.3362e-04

FREQUENCY
P1_W,P2_W:1.5799e-03
P1,P2_W:7.8999e-04
P1_W,P2:7.8999e-04
P1,P2:3.3406e-05
```

# Case Study D: Soft Dependency

## BUILT-IN GENERATION

```
DEPENDENCIES - Notepad
File Edit Format View Help
LOAD
P1|P2:exponential,14.0e-4
P2|P1:exponential,14.0e-4
```

```
COMPONENTS ... - [ ] [X]
File Edit Format View Help
HX1
FAIL
1.7e-6
REPAIR
0.0417

T1
FAIL
2.7e-8
REPAIR
0.1250

P1
FAIL
8.0e-4
REPAIR
0.1250

P2
FAIL
8.0e-4
REPAIR
0.1250
```

## IMPORTED MM

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP

P2
DEP

HX2
FAIL
1.7e-6
REPAIR
```

```
DEPENDENCY - Notepad
File Edit Format View Help
MMS
P1P2_MM
```

```
P1P2_MM - Notepad
File Edit Format View Help
STATES
P1_W,P2_W
P1,P2_W
P1_W,P2
P1,P2

TRANSITION MATRIX
-1,0.5,0.5,0
12,-13,0,1
12,0,-13,1
6,0,0,-6
```

## IMPORTED PN

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP

P2
DEP

HX2
FAIL
1.7e-6
REPAIR
```

```
DEPENDENCY - Notepad
File Edit Format View
PNS
P1P2_PN
```

```
P1P2_PN - Notepad
File Edit Format View Help
PLACES
P1requested,1
P1
P1_W
P2_W
P2

TRANSITIONS
P1requested->P1_W,P1:P1start,probability,0.981,0.019
P1_W->P1:P1fails,exponential,8.0e-4
P1->P1_W:P1repair,exponential,0.1250
P1->P1,P2_W,P2:P2start,probability,0.981,0.019
P2->P2_W:P2repair,exponential,0.1250
P2_W->P2:P2fails,exponential,8.0e-4
P1_W,P2_W->P1_W:P2toSleep,instant,0

INHIBITORS
P2->P2start
```

## IMPORTED DATA

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP

P2
DEP

HX2
FAIL
1.7e-6
REPAIR
```

```
DEPENDENCY - Notepad
File Edit Format View Help
DATA
DG1_DATA
```

```
DG1_DATA - Notepad
File Edit Format View Help
PROBABILITY
P1_W,P2_W:9.8749e-01
P1,P2_W:6.1863e-03
P1_W,P2:6.1863e-03
P1,P2:1.3362e-04

FREQUENCY
P1_W,P2_W:1.5799e-03
P1,P2_W:7.8999e-04
P1_W,P2:7.8999e-04
P1,P2:3.3406e-05
```



# Step 1: Component Reliability

COMPONENTS - Notepad

File Edit Format View Help

HX1  
FAIL  
1.7e-6  
REPAIR  
0.0417

T1  
FAIL  
2.7e-8  
REPAIR  
0.1250

P1  
DEP

P2  
DEP

HX2  
FAIL  
1.7e-6  
REPAIR  
0.0714  
INSPECTION  
4380

T2  
FAIL  
2.7e-8  
REPAIR  
0.1250  
INSPECTION  
4380

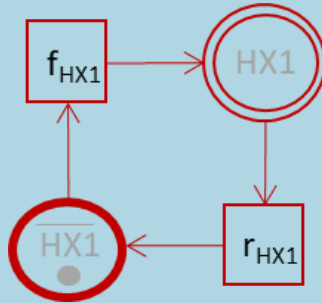
Exponentially Distributed?

N

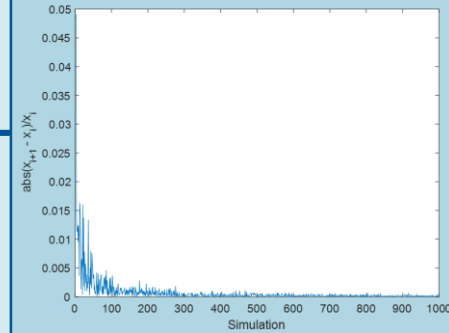
Y

## NON-CONSTANT FAILURE/REPAIR RATES

### GENERATE PN



### RUN TO CONVERGENCE



### STORE OUTPUT

HX1	
Unavailability	3.92e <sup>-3</sup>
Failure Frequency [h <sup>-1</sup> ]	1.63e <sup>-4</sup>

## CONSTANT FAILURE/REPAIR RATES

### IDENTIFY MODEL

- Non-Repairable
- Corrective Maintenance
- Scheduled Maintenance

### COMPUTE RELIABILITY

$$q(P1) = \frac{\lambda}{\lambda + \nu}$$

$$f(P1) = \lambda * (1 - q(P1))$$

[ λ = failure rate, ν = repair rate]

### STORE OUTPUT

P1	
Unavailability	6.40e <sup>-03</sup>
Failure Frequency [h <sup>-1</sup> ]	7.95e <sup>-04</sup>

# Step 2: Independent FTs Definition

## INPUT FTs

## INDEPENDENT ?

## MERGE DEPENDENT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

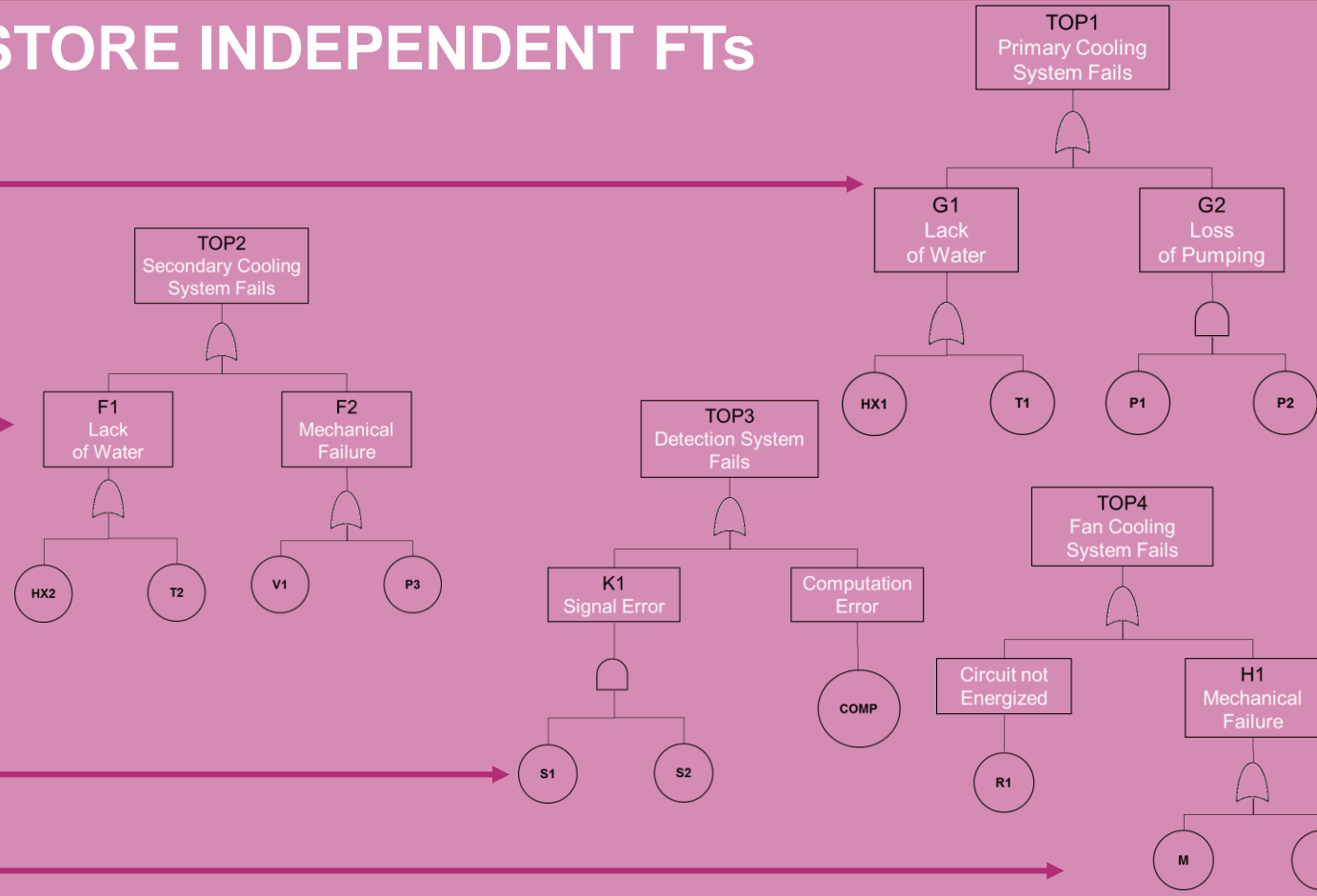
SECONDARY - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P3  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

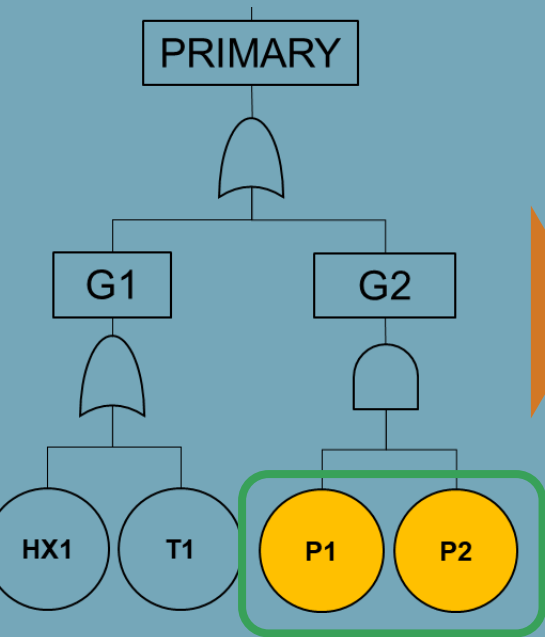
DEPENDENCY - Notepad  
File Edit Format View Help  
MMS  
P1P2\_MM

## STORE INDEPENDENT FTs

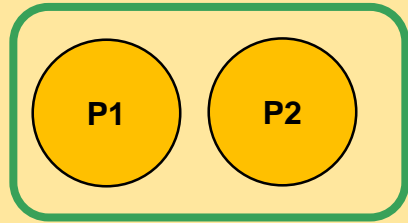


# Step 3: Dependency Group Computation

## FT 1



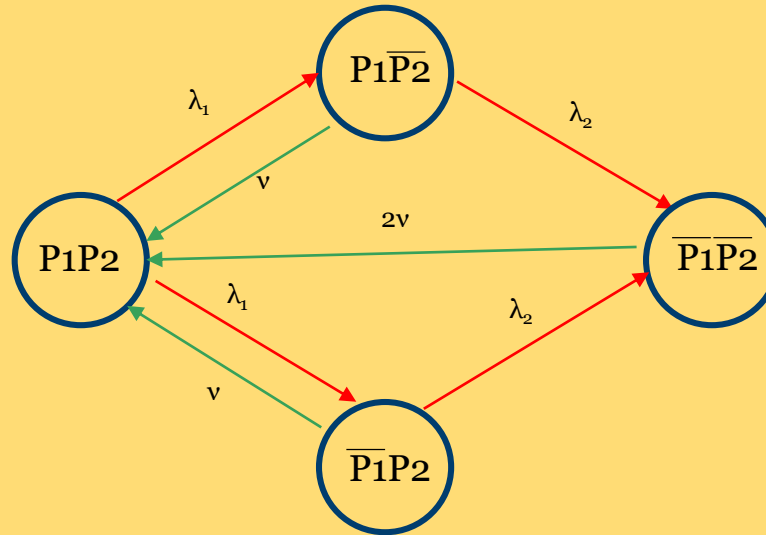
## DEPENDENCY GROUPS



```

P1P2_MM - Notepad
File Edit Format View Help
STATES
P1_W,P2_W
P1,P2_W
P1_W,P2
P1,P2
TRANSITION MATRIX
-1,0.5,0.5,0
12,-13,0,1
12,0,-13,1
6,0,0,-6
    
```

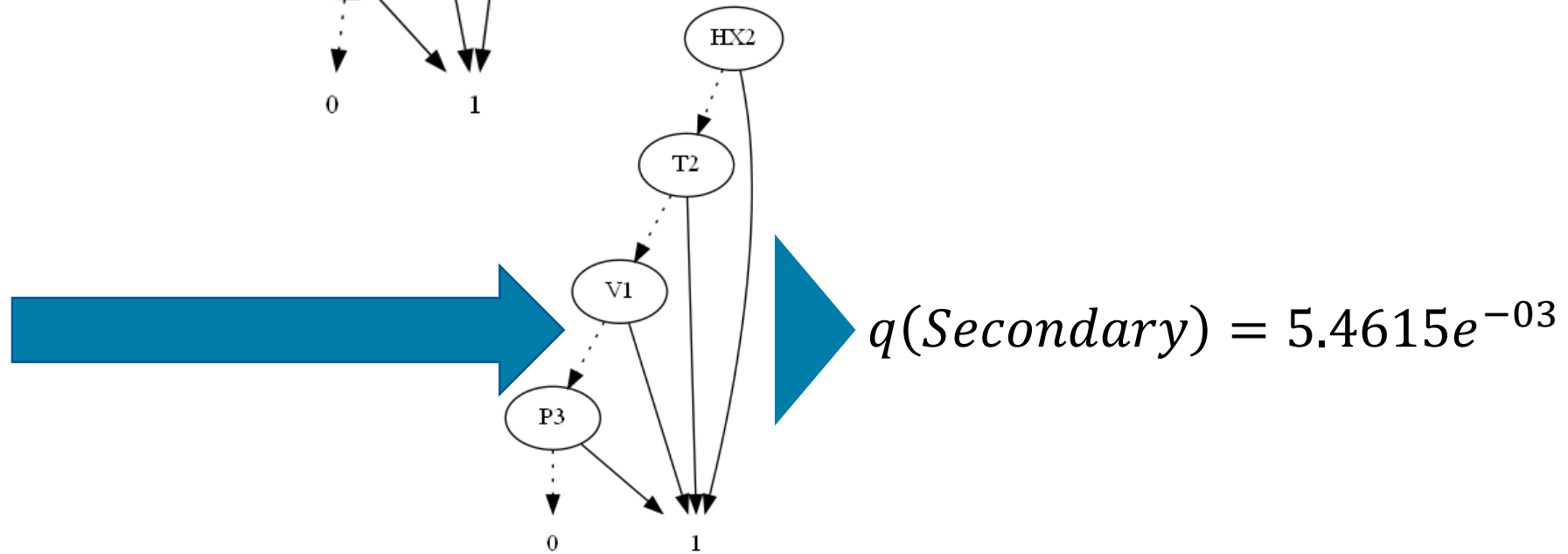
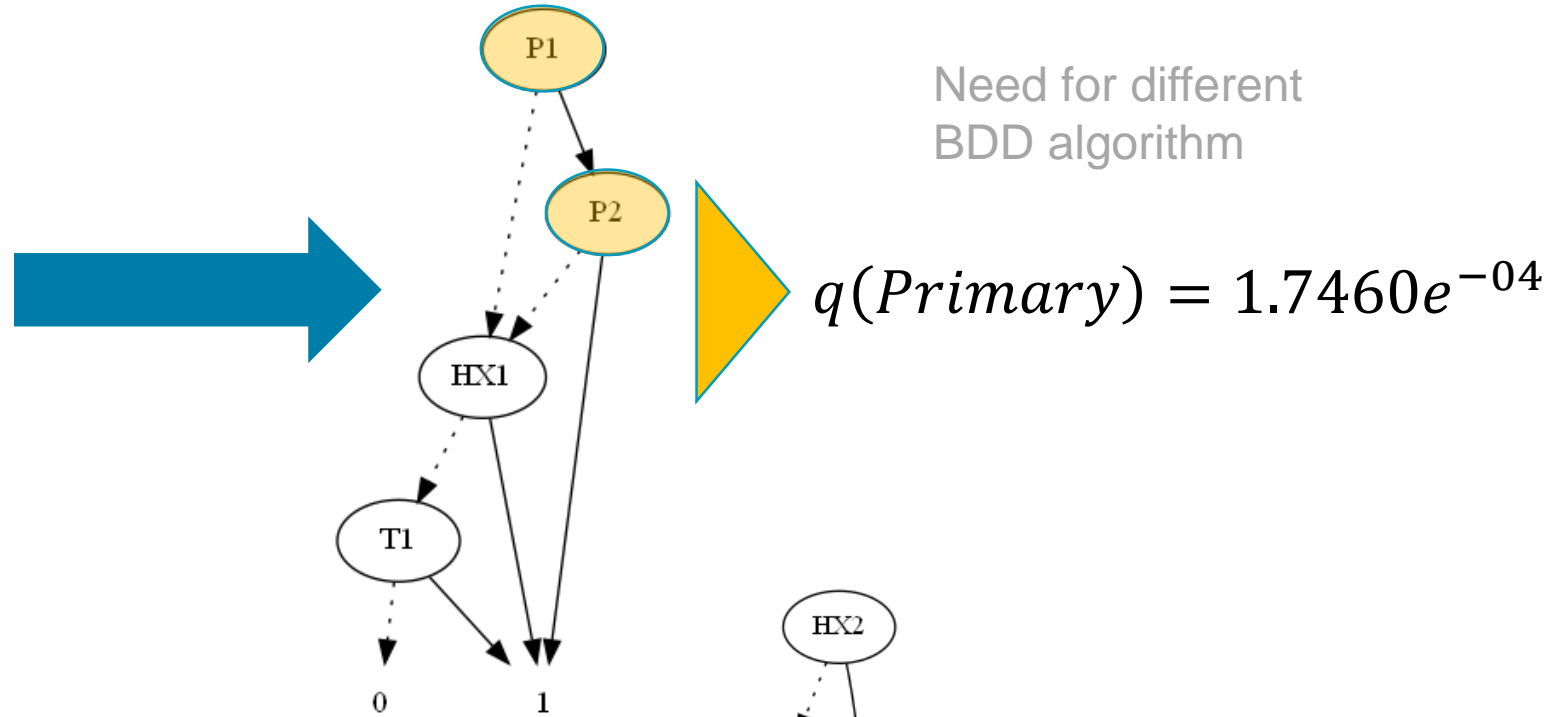
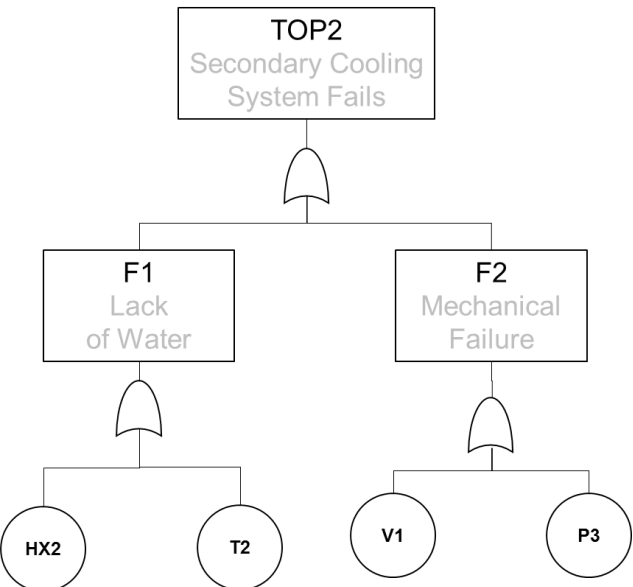
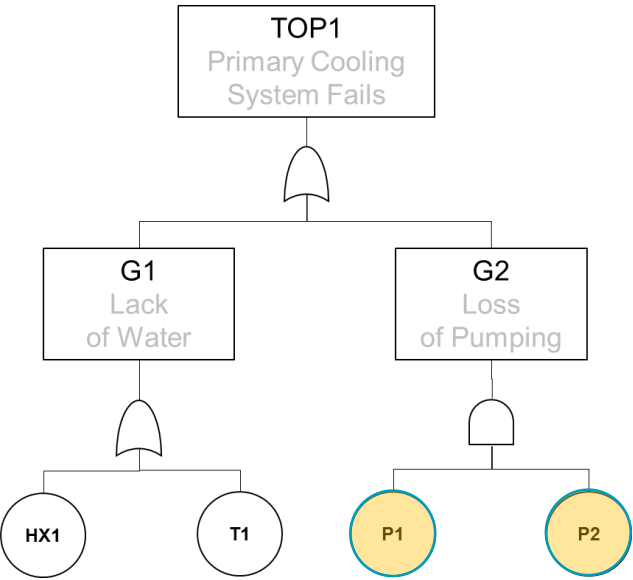
## MM GENERATION



## MM CALCULATION

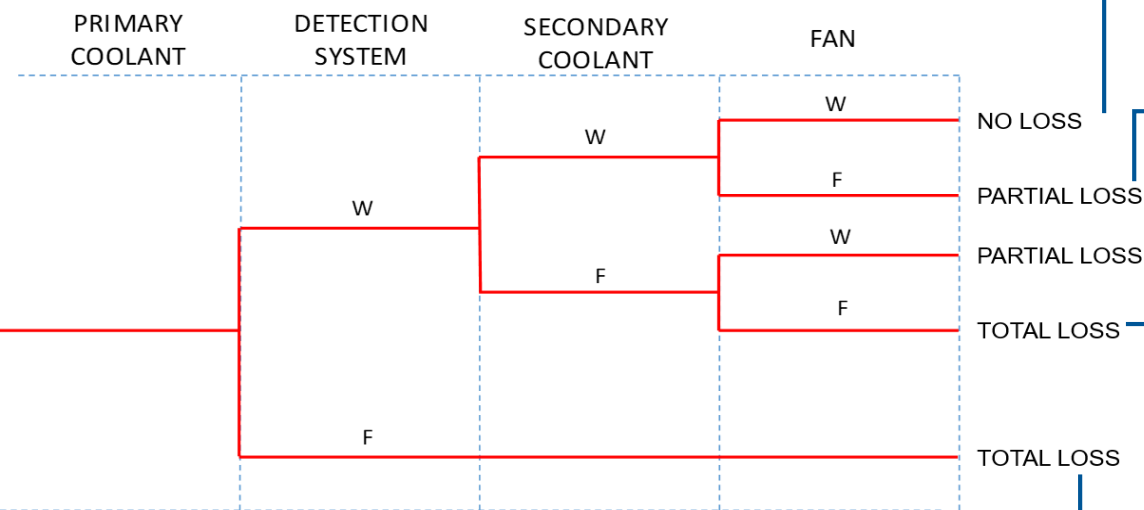
STATE	PROBABILITY	FREQUENCY
$P1, P2$	$1.3362e^{-04}$	$3.3406e^{-05}$
$P1, \overline{P2}$	$6.1863e^{-03}$	$7.8999e^{-04}$
$\overline{P1}, P2$	$6.1863e^{-03}$	$7.8999e^{-04}$
$\overline{P1}, \overline{P2}$	$9.8749e^{-01}$	$1.5799e^{-03}$

# Step 4: FTs Computation





# Step 5: ET Computation



$$f_{NoLoss} = f_{primary} \cdot q(\overline{Secondary}) \cdot q(\overline{Detection}) \cdot q(\overline{Fan})$$

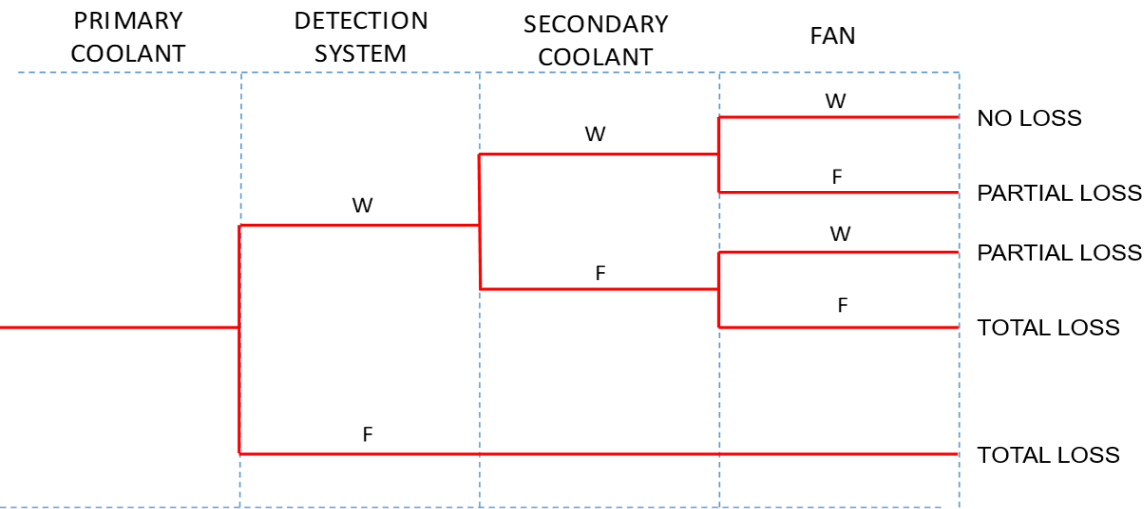
$$f_{PartialLoss1} = f_{primary} \cdot q(\overline{Secondary}) \cdot q(\overline{Detection}) \cdot q(Fan)$$

$$f_{PartialLoss2} = f_{primary} \cdot q(Secondary) \cdot q(\overline{Detection}) \cdot q(\overline{Fan})$$

$$f_{TotalLoss1} = f_{primary} \cdot q(Secondary) \cdot q(\overline{Detection}) \cdot Q(Fan)$$

$$f_{TotalLoss2} = f_{primary} \cdot q(Detection)$$

# Step 5: ET Computation



## CONSEQUENCE FREQUENCIES

$$F_{NoLoss} = 3.5639 e^{-05} h^{-1}$$

$$F_{PartialLoss} = f_{PartialLoss1} + f_{PartialLoss2} = 6.5588 e^{-07} h^{-1}$$

$$F_{TotalLoss} = f_{TotalLoss1} + f_{TotalLoss2} = 2.4793 e^{-08} h^{-1}$$



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# Case Study D

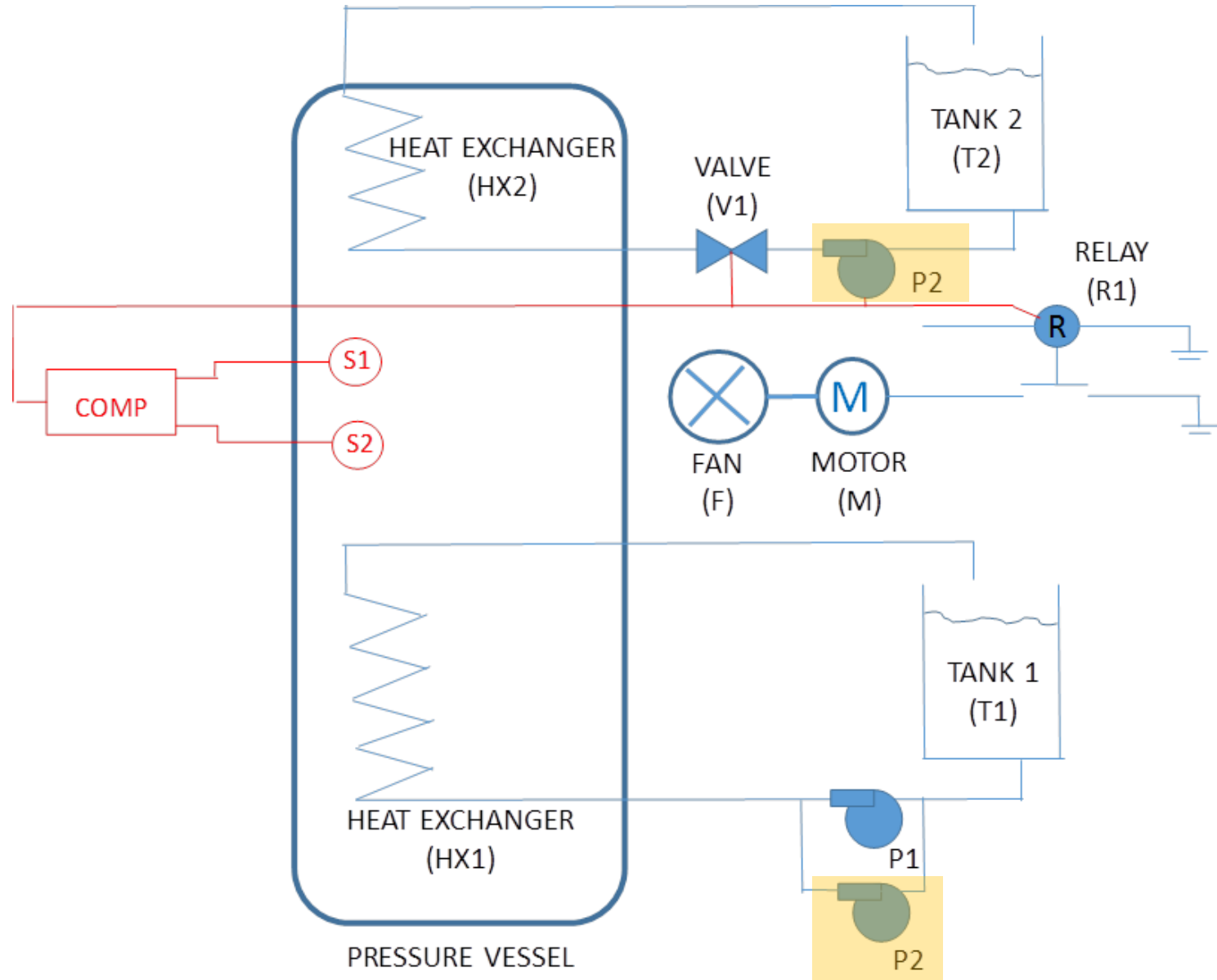
A bit of everything

# Complex Dependency

```
COMPONENTS - Notepad
File Edit Format View Help
P1
DEP
P2
DEP
HX2
FAIL
1.7e-6
REPATR
```

```
DEPENDENCY - Notepad
File Edit Format View Help
MMs
P1P2_MM
COMMON COMPONENTS
P2: PRIMARY, SECONDARY
```

```
P1P2_MM - Notepad
File Edit Format View Help
STATES
P1_W, P2_W
P1, P2_W
P1_W, P2
P1, P2
TRANSITION MATRIX
-1, 0.5, 0.5, 0
12, -13, 0, 1
12, 0, -13, 1
6, 0, 0, -6
```





# Step 1: Component Reliability

COMPONENTS - Notepad

File Edit Format View Help

HX1  
FAIL  
1.7e-6  
REPAIR  
0.0417

T1  
FAIL  
2.7e-8  
REPAIR  
0.1250

P1  
DEP

P2  
DEP

HX2  
FAIL  
1.7e-6  
REPAIR  
0.0714  
INSPECTION  
4380

T2  
FAIL  
2.7e-8  
REPAIR  
0.1250  
INSPECTION  
4380

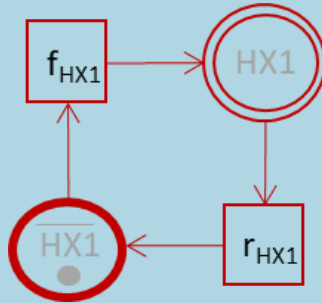
Exponentially Distributed?

N

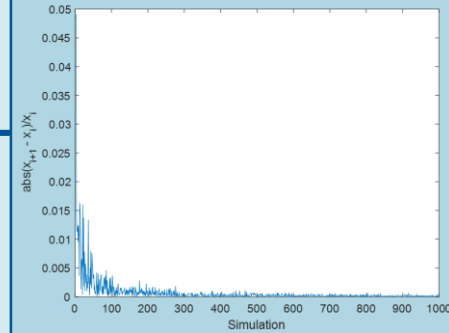
Y

## NON-CONSTANT FAILURE/REPAIR RATES

### GENERATE PN



### RUN TO CONVERGENCE



### STORE OUTPUT

HX1	
Unavailability	$3.92e^{-3}$
Failure Frequency [ $h^{-1}$ ]	$1.63e^{-4}$

## CONSTANT FAILURE/REPAIR RATES

### IDENTIFY MODEL

- Non-Repairable
- Corrective Maintenance
- Scheduled Maintenance

### COMPUTE RELIABILITY

$$q(P1) = \frac{\lambda}{\lambda + \nu}$$

$$f(P1) = \lambda * (1 - q(P1))$$

[  $\lambda$  = failure rate,  $\nu$  = repair rate ]

### STORE OUTPUT

P1	
Unavailability	$6.40e^{-03}$
Failure Frequency [ $h^{-1}$ ]	$7.95e^{-04}$

# Step 2: Independent FTs Definition

## INPUT FTs

PRIMARY - Notepad  
File Edit Format View Help  
PRIMARY,1,G1,G2  
G2,0,P1,P2  
G1,1,HX1,T1

SECONDARY\_FT - Notepad  
File Edit Format View Help  
SECONDARY,1,F2,F1  
F2,1,V1,P2  
F1,1,HX2,T2

DETECTION\_FT - Notepad  
File Edit Format View Help  
DETECTION,1,K1,COMP  
K1,0,S1,S2

FAN - Notepad  
File Edit Format View Help  
FAN,1,R1,H1  
H1,1,M,F

## INDEPENDENT ?

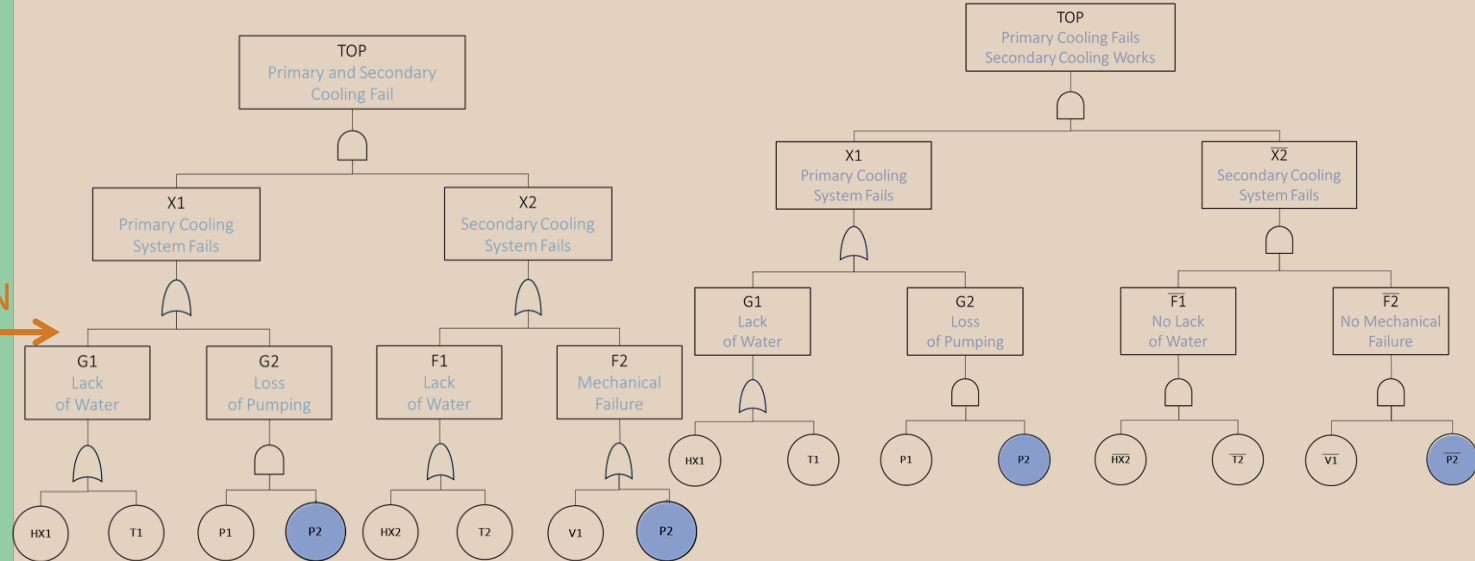
DEPENDENCY - Notepad  
File Edit Format View Help  
MMs  
P1P2\_MM  
**COMMON COMPONENTS  
P2:PRIMARY,SECONDARY**

?

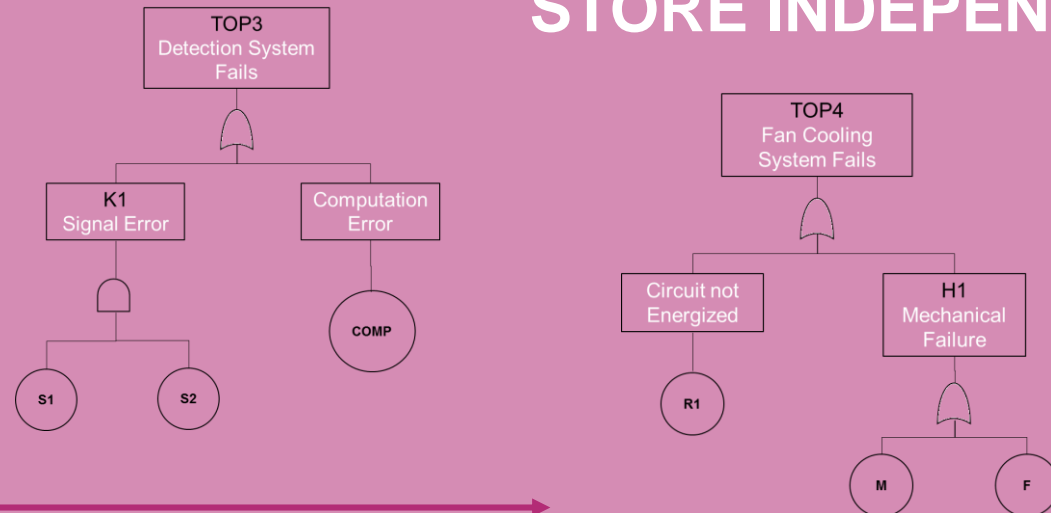
Y

Y

## MERGE DEPENDENT FTs

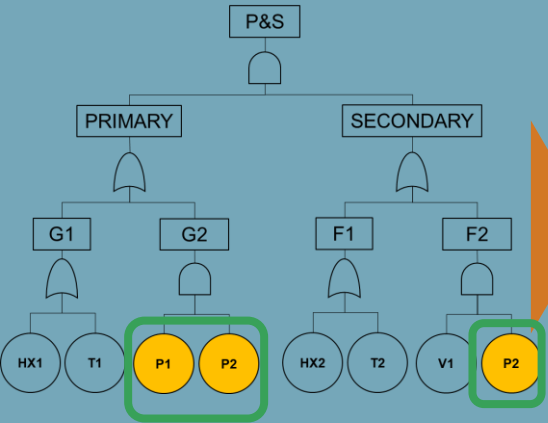


## STORE INDEPENDENT FTs

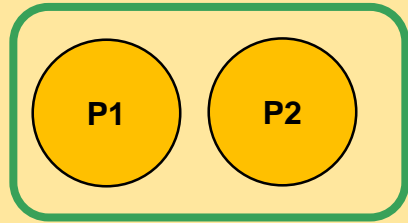


# Step 3: Dependency Group Computation

## FT 1



## DEPENDENCY GROUPS

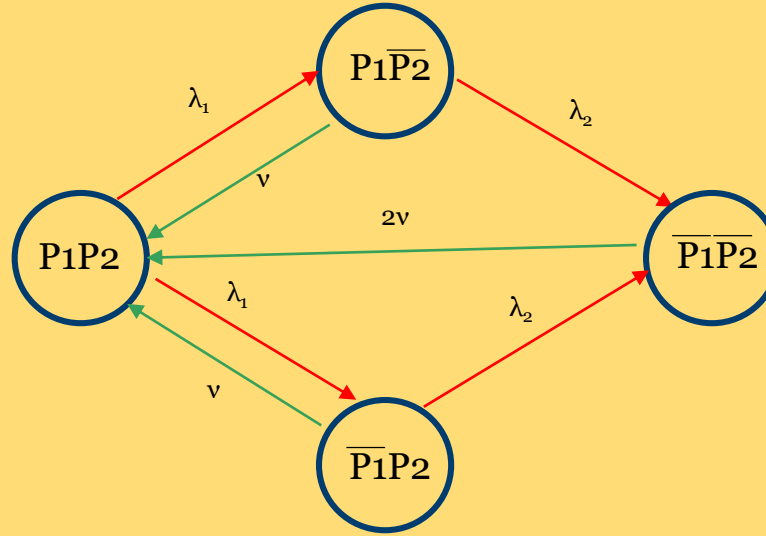


```

P1P2_MM - Notepad
File Edit Format View Help
STATES
P1_W,P2_W
P1,P2_W
P1_W,P2
P1,P2

TRANSITION MATRIX
-1,0.5,0.5,0
12,-13,0,1
12,0,-13,1
6,0,0,-6
    
```

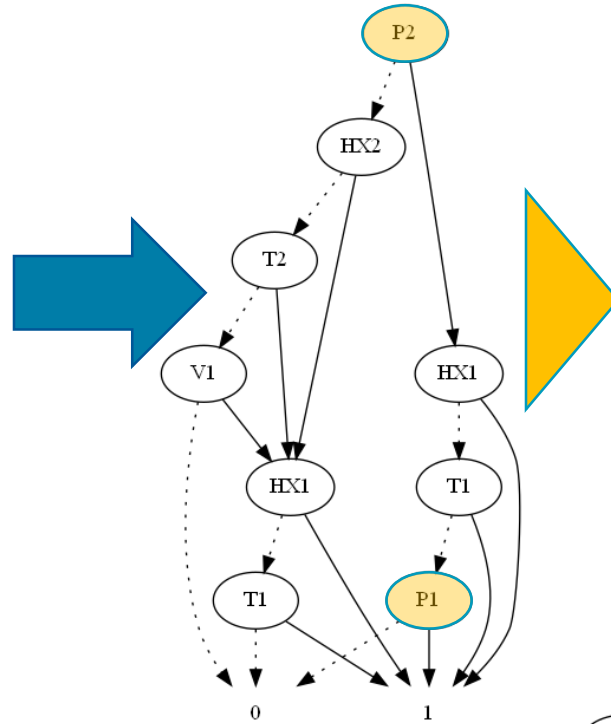
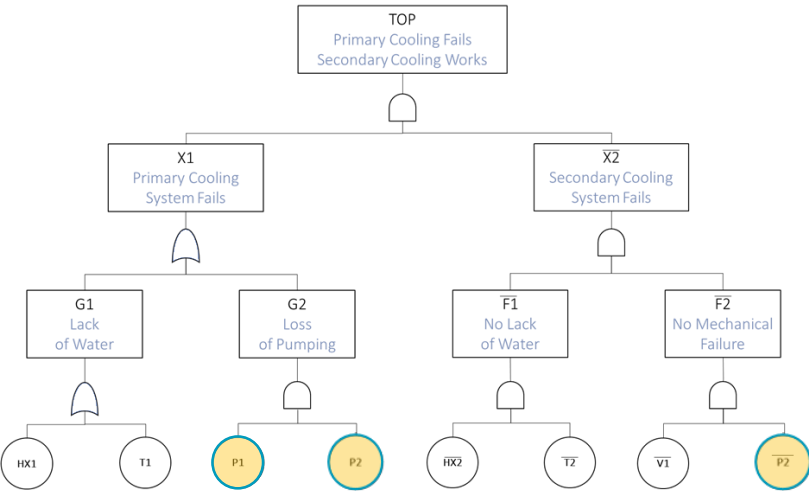
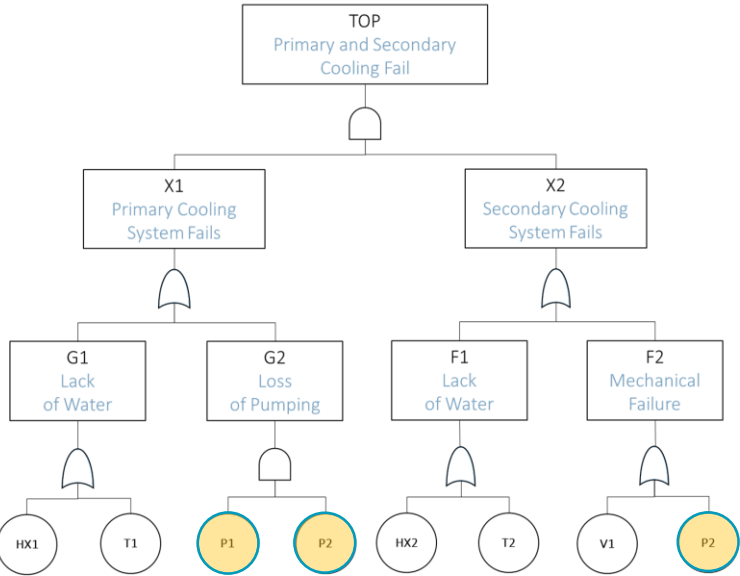
## MM GENERATION



## MM CALCULATION

STATE	PROBABILITY	FREQUENCY
$P1, P2$	$1.3362e^{-04}$	$3.3406e^{-05}$
$P1, \overline{P2}$	$6.1863e^{-03}$	$7.8999e^{-04}$
$\overline{P1}, P2$	$6.1863e^{-03}$	$7.8999e^{-04}$
$\overline{P1}, \overline{P2}$	$9.8749e^{-01}$	$1.5799e^{-03}$

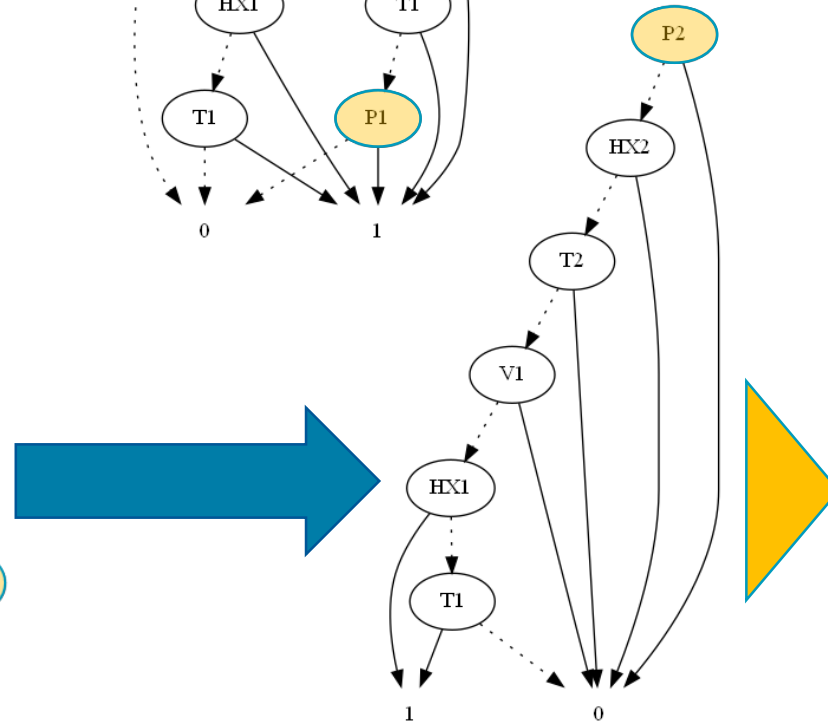
# Step 4: FTs Computation



Need for different BDD algorithm

$$q(\text{Primary, Secondary}) = 1.3405e^{-04}$$

[was  $4.1399e^{-05}$  in case C]

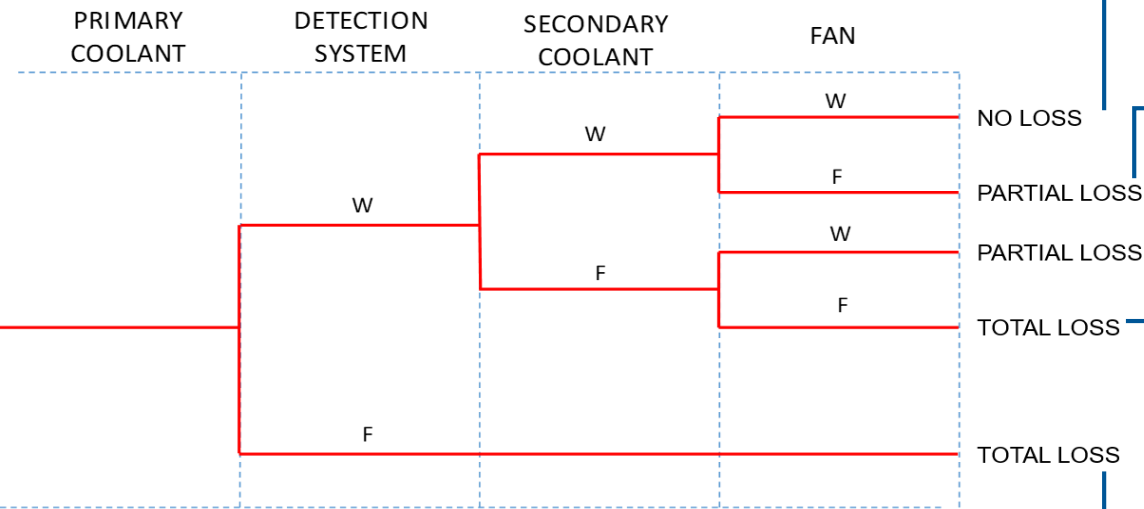


Need for different BDD algorithm

$$q(\text{Primary, } \overline{\text{Secondary}}) = 1.7459e^{-05}$$

[was  $8.1942e^{-05}$  in case C]

# Step 5: ET Computation



$$f_{NoLoss} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(\overline{Fan})$$

$$f_{PartialLoss1} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(Fan)$$

$$f_{PartialLoss2} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(\overline{Fan})$$

$$f_{TotalLoss1} = f_{primary} \cdot q(\overline{Secondary|Primary}) \cdot q(\overline{Detection}) \cdot q(Fan)$$

$$f_{TotalLoss2} = f_{primary} \cdot q(Detection)$$



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# Challenges and Current Work

Conclusions



- BDD computation algorithm considering dependencies more computational demanding than traditional solutions
  - need to minimise the use of the algorithm to the smallest section of the model containing dependencies
  - **Faunet reduction and modularisation** (already implemented)

- BDD computation algorithm considering dependencies more computational demanding than traditional solutions
  - need to minimise the use of the algorithm to the smallest section of the model containing dependencies
  - **Faunet reduction and modularisation** (already implemented)
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- BDD merging (instead of FT merging for dependent FTs)